# 15 SECONDS TO ALPHA: HIGHER FREQUENCY RISK PRICING FOR COMMERCIAL REAL ESTATE SECURITIES

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#### Abstract

This paper introduces a generalizable method to estimate reduced form risk decompositions at daily and intraday frequencies applied to CMBX. We estimate partitions for the risks of default, liquidity, excess liquidity, and interest rate volatility at daily and intraday frequencies. Our new estimation technique combines previously simulated risk partitions with current market data using principal components and OLS methods. We find liquidity and excess liquidity risk partitions are significant in explaining daily effective bid-ask spreads historically, from 11/2007-4/2019, and in 20-day forecasts. During the Covid pandemic, we extend the model from daily to intraday frequency, estimating intraday in 15 second intervals over the period 4/2020-4/2021. During Covid, we find regular patterns of risk partition volatility in the cross-section and exploit those insights in the related, and more frequently traded, REIT sector in automated trading strategies. In our 54 long/short day trading strategies, 96% showed significant alphas, and 63% produced abnormal cumulative returns between 0.73% and 48.74%. These results support pricing risk with risk partitioning at higher frequencies for commercial real estate securities.

 $\label{thm:continuous} \mbox{Key Words: High Frequency Trading, Liquidity, Microstructure, REITs, Securitization}$ 

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# Introduction

Microstructure bid-ask spread estimation is not the only theoretical measure of liquidity. The reduced form theoretical liquidity and excess liquidity partitions of commercial mortgage backed securities (CMBS), first introduced in Christopoulos (2017) and then indexed in Christopoulos and Jarrow (2018), also provide rich insights into CMBS liquidity. By extending the frequency of risk partition estimation in the previous work from monthly to daily and then to intraday frequencies with a new technique, we disclose new insights into the liquidity of commercial mortgage backed securities indexed credit default swaps (CMBX) and Real Estate Investment Trusts (REITs).

Related work in the area of Corporate bonds can be found in Longstaff, Mithal and Neis (2005), Bao, Pan and Wang (2011) and Gilchrist and Zakrajsek (2012), among others, who identified compensation within observable risk premia apart from default risk. Extending the earlier work, Christopoulos (2017) introduced the technique to project fair value prices onto observed risk premia in the market in basis points (bps) for CMBX classes. In Christopoulos (2017) the reduced form simulations used in that study first allowed, and then restricted, simulation of default. This allowed for isolation of theoretical compensation for default and interest rate risks which were both explicitly modelled. Since the model used in Christopoulos (2017) and then indexed in Christopoulos and Jarrow (2018) was well specified, the pricing of residual risk premia not associated with default and interest rate risks is interpreted theoretically as liquidity availability. Additionally, because fair value pricing is risk neutral, there are indeed instances empirically where fair value pricing so exceeds the market price, that an additional risk premia, in excess of observed risk premia, is required for reconciliation of fair value to market prices in the transformations. This additional compensation above observable risk premia is interpreted as excess liquidity availability. Excess liquidity (in excess of observed market risk premia) indicates the amounts in bps by which market risk premia could instantaneously increase (widen) before the security experienced deterioration in regular liquidity availability determined in the reduced form simulation. Since reduced form liquidity and excess liquidity partitions for CMBX are residual measures, they provide valuable insights into CMBX liquidity pricing apart from the idiosyncratic risks modelled explicitly at the loan and bond levels. Importantly, these risk partition measures provide insights into the expectations process of investors apart from the risks of default and rate volatility captured through the model implementation. Thus, the presence of liquidity and excess liquidity, enhance comparisons of 'rich' and 'cheap' securities relative to their underlying risks and provide insights into the mind of the market.

In the two earlier studies focusing on CMBX risk partitioning, the frequency of capture is monthly. In this work we resolve to increase the frequency of risk partitioning for CMBX to daily, and then to intraday pacing, in keeping with the pace of more developed markets. We do this to inquire into the nature of CMBX risks and their price formation. In so doing, we are able to leverage the earlier work and disclose new insights with our approach. We first consider, daily, the liquidity of CMBX from two perspectives: microstructure and risk partitions. We then advance the literature with the intraday risk assessments of CMBX and REITs. Both perspectives on liquidity we bring from classical microstructure and novel estimated reduced form partitions are new to the literature concerning CMBX and REITs. This study provides some reconciliation between the two views of liquidity.

We begin by establishing daily liquidity assessments for CMBX using the classical microstructure models of Roll (1984), Thompson and Waller (1987) and variants suggested by Harris (1990), Hasbrouck (2009), Foucault, Pagano and Roell (2013), and Christopoulos (2020). Construction of effective bid-ask spreads for CMBX establishes one perspective on CMBX liquidity. CMBX is an over-the-counter (OTC) product and is not traded on electronic exchanges. This contrasts with Corporate bonds, which are increasingly traded electronically and which are required to post execution prices and volumes on the Trade Reporting and Compliance Engine (TRACE). In an effort to improve the flow of information as noted in Hollified, Nekyudov and Spatt (2017) there is recording of day-end mark-to-market values since 2007 for CMBX through Markit which collects, and then aggregates, such reported values from all dealers. Nevertheless, the CMBX market still does not provide reliable intraday recorded bid-ask spreads, mid-market spreads, corresponding trade executions prices, or transaction volumes. As such, the data over the sample period 11/2007-4/2019 we use is restricted to end of day mid-market CMBX spreads. Since these classes of microstructure models provide insights into liquidity for instruments limited to end of day mark to market values, they are well suited to CMBX liquidity assessment, from a microstructure perspective.

Next, we develop the alternative perspective on CMBX liquidity by estimating daily the reduced form liquidity and excess liquidity partitions. We use these risk partitions of liquidity to compare to the microstructure perspective on liquidity articulated in effective bid-ask spreads. Re-simulating and re-partitioning with the prior techniques of Christopoulos (2017) and Christopoulos and Jarrow (2018), relies on access to costly data and computation that is not currently available. Instead, we construct a linear estimation model (the 'Daily Model') using principal component and OLS techniques with the training data the monthly market variables of the VIX, interest rates, and REIT prices which represent the economy and the monthly simulated values of risk partitions from Christopoulos and Jarrow (2018) the dependent variables. With two perspectives on CMBX liquidity established (classical microstructure and estimated reduced form), we then test their relationships to validate the Daily Model. Our testing of the Daily Model gives us our first two main results.

First, liquidity risk partitions play a significant role in CMBX price formation for AAA and BBB credits over 2828 daily observations from 11/2007 - 4/2019. We establish this result through the use of multivariate OLS of risk premia changes regressed onto changes in the macroeconomy for observed market risk premia over 5-day rolling estimation periods to assess whether estimates of reduced form liquidity and excess liquidity measures are being communicated in effective bid-ask spreads.

Second, estimated reduced form liquidity measures have a significant effect on future observed CMBX liquidity (as measured by effective bid-ask spreads) over 20 day forecast periods. We establish this result in time-series analyses using vector autoregression (VAR) and Granger causality techniques. The significant results in those tests motivate the use of impulse response functions (IRF) to project effective bid-ask spreads in response to shocks of liquidity and excess liquidity.

In conjunction, the first two main results and supporting evidence validate the Daily Model and provide new insights into the nature of liquidity for CMBX from both microstructure and risk partition perspectives. This allows us to move forward with the Intraday Model for risk partition estimation across 240 trading days during the Covid-19 pandemic period between 4/2020-4/2021. The Intraday Model increases the speed of risk partitioning assessment by increasing the frequency of polling of market data to 15 second intervals intraday for the explanatory variables (VIX, rates, and REITs) and using their changes to

estimate risk partitions, intraday.

Since CMBX and CMBS do not trade electronically, the frequency of CMBX risk partition generation in this study exceeds the market's pace of trading in CMBS and CMBX. That is interesting because it means that our intraday proxies of CMBX risk neutral risk partitions have no corresponding intraday CMBX market price for comparison. In this sense, the intraday risk partitions are empirical renderings of purely theoretical price changes. This observation invites testing of the Intraday Model, which gives rise to our third main result.

Third, during the pandemic, we find considerably greater volatility in risk partition pricing at the start of each trading day for all risk partitions compared to the end of each trading day. We establish this result by conducting a cross-sectional evaluation of millions of cumulative intraday changes in CMBX risk partitions in 15 second intervals for 240 trading days. The phenomena observed in our third main result invites further testing. We note that REITs, like CMBX, are also exposed to commercial real estate risks. Additionally, REIT trading frequency more closely matches the frequency of estimation of the risk partitions. With these insights we are able to establish our fourth main result.

Fourth, well constructed intraday trading strategies using CMBX risk partitions applied to the REIT market can result in substantial extraordinary returns and bring insights into the relative pricing of liquidity in both CMBX and REIT sectors. We establish our fourth main result by fusing the cross-sectional insights into CMBX risk partition volatility with the more frequently traded REIT sector in a set of 54 long/short day trading strategies during the Covid pandemic for each of the investment grade credit rating classes (AAA, AJ/AS, AA, A, BBB and BBB-). The strategies exploit regular and systematic aberrations in volatility in both CMBX risk partitions and REIT pricing. Using use the Intertemporal Capital Asset Pricing Model (ICAPM) of Merton (1990) we find 96% of the strategies produced positive and statistically significant  $\alpha's$ . 65% of those strategies also exhibited positive cumulative returns over the Covid-19 crisis period ranging from 0.73% to 48.74% with generally solid Sharpe ratios. In conjunction, the third and fourth results and their supporting evidence validate the Intraday Model and, like the Daily Model, also provide new insights into the nature of liquidity for CMBX.

The size of the CMBX and CMBS sectors stands at approximately \$600 billion while the US REIT sector stands at approximately \$1.3 trillion. Our paper establishes that CMBX risk

partitions at daily and intraday frequencies provide new insights into the liquidity for CMBX and REIT sectors which have a combined value of about \$2 trillion. As such, we provide a new perspective on the pricing of liquidity risks for two large and related sectors within real estate capital markets. The remainder of this paper is organized as follows: Section 1 discusses the data used in this study. Section 2 provides a literature review of a few existing models used to assess CMBX liquidity. Section 3 introduces the Daily Model and discusses the various statistical methods and results used for its validation. Section 4 introduces the Intraday Model implemented during the Covid-19 pandemic which uses cross-sectional visualizations, trading strategies, and ICAPM results for its validation. Section 5 summarizes with suggestions for future work. The Appendix provides supplementary information.

# 1 Data

In this section we discuss the data used throughout this study. The study uses data from three time frames: the training period, the daily period, and the intraday period.

- 1. The training period consists of 92 monthly observations from 11/2007-6/2015 in which training data is used to train the Daily Model in <u>Section 3</u>.
- 2. The daily period consists of 2828 daily observation in which data are used to produce risk partition estimates with the Daily Model in Section 3 from 11/2007-4/2019 and are used in OLS, VAR, Granger and IRF analyses.
- 3. The intraday period consists of 246 dates during the Covid-19 pandemic in which time stamped intraday data are used to produce estimates of risk partitions with the Intraday Model in Section 4 from 4/2020-4/2021 which are used in cross-sectional analyses and ICAPM trading tests at the open and close of the trading days.

Tables and figures summarizing the data and results are introduced in the relevant sections throughout the paper where the data are used.

# 1.1 Private data - CMBX risk premia

The private data was generously donated to us by one of the largest asset managers for our research. Like CMBS, CMBX trade on a 'Spread' basis, where Spreads are mid-market risk premia  $S_t$ , in excess of US Treasury swap spreads. These Spreads are contributed

by dealers to Markit at the close of each trading day. For all daily observation dates, t, the risk premium,  $S_t$ , captures the drivers of uncertainty on CMBX derivatives in excess of the relevant risk-free rate. The underlying collateral tranches securing CMBX used in this study represent approximately \$400 billion (bn) of the ~\$600 bn CMBS market. As a securitized credit default swap, as described in Driessen and Van Hemert (2012) and Christopoulos and Jarrow (2018), series of CMBX classes (or tranches) capture the cashflows of 25 reference asset CMBS tranches for corresponding credit ratings. A Bloomberg post and primer discussion of CMBX bid-ask spreads is provided in Appendix Section A.1. To our knowledge, such indications of CMBX liquidity are only available as sporadic posts by dealers to clients and are not regularly recorded and verified with time stamps intraday.

# 1.2 Public data

#### 1.2.1 Monthly

We use prices for 25 representative publicly traded REITs obtained from Yahoo! Finance that we use for the estimation of the Daily Model in Section 3 and the estimation of the Intraday Model in Section 4, through RapidAPI. We select these REITs due to their similarity to CMBX on a few dimensions. Table 1 lists the names of the 25 REITs used in this study along with their property type, ticker, factor name (proptype\_ticker), and market capitalization as of 6/27/2021. The market capitalization of these 25 REITs selected total \$478.45 billion. According to the National Association of Real Estate Investment Trusts (NAREIT), the total market capitalization (market cap) of US REITs was \$1249.19 billion as of December 31, 2020<sup>1</sup>, and so our sample captures about 38% of the US REIT sector by market cap. NAREIT also states that the total number of US REITs is 223, and so by counts, our sample represents about 11% of the US REIT sector. These REITs also are well distributed across multiple property types as shown in a further summary of the REIT sample in our study broken down by property type in Table 2. Our estimated economy also captures most of the REITs used in the prior study of Christopoulos and Jarrow (2018) and for continuity with the simulation, we also use these REITs. Finally, as the CMBX in our sample represent approximately \$400 billion of CMBS underlying, the size of our REIT sample and our CMBX

<sup>&</sup>lt;sup>1</sup>See https://www.reit.com/data-research/reit-market-data/us-reit-industry-equity-market-cap

sample are of similar market magnitude.

Table 1: Sample REITs

PropType	Ticker	Factor Name	REIT Name	Market Cap (\$bn)
Industrial (IN)	DRE FR PLD SELF	IN_DRE IN_FR IN_PLD IN_SELF	Duke Realty First Industrial Realty Trust Prologis, Inc. Global Self Storage, Inc.	\$18.04 \$6.90 \$90.25 \$54.28
Hotel (LO)	HST MAR WH MGM	LO_HST LO_MAR LO_WYND LO_MGM	Host Hotels & Resorts, Inc. Marriott International, Inc. Wyndam Hotels & Resorts, Inc. MGM Resorts International	\$12.41 \$45.64 \$6.82 \$21.53
Multifamily (MF)	AVB ELS EQR UDR	MF_AVB MF_ELS MF_EQR MF_UDR	Avalon Bay Communities, Inc. Equity LifeStyle Properties, Inc. Equity Residential UDR, Inc.	\$29.87 \$13.81 \$29.39 \$14.80
Office (OF)	BXP CLI HIW SLG VNO	OF_BXP OF_CLI OF_HIW OF_SLG OF_VNO	Boston Properties, Inc. Mack-Cali Realty Corporation Highwoods Properties, Inc. SL Green Realty Corp. Vornado Realty Trust	\$18.70 \$1.55 \$4.85 \$5.72 \$9.24
Mixed Use/Other (OT)	BKD NNN PSB WPC	OT_BKD OT_NNN OT_PSB OT_WPC	Brookdale Senior Living Inc. National Retail Properties, Inc. PS Business Parks, Inc. W.P. Carey Inc.	\$1.54 \$8.41 \$4.15 \$13.93
Retail (RT)	KIM REG SPG TCO	RT_KIM RT_REG RT_SPG RT_TCO	KIMCO Realty Corporation Regency Centers Corporation Simon Property Group Taubman Centers Inc.	\$9.14 \$11.05 \$43.06 \$3.40

This table summarizes the 25 REITs used in this study. The market capitalization of the REITs are \$478.45 billion as of 6/27/2021. The first column provides the property type and groups the REITs by property type separated by borders. The six property types are Industrial (IN), Hotel (LO), Multifamily (MF), Office (OF), Mixed Use/Other (OT), and Retail (RT). The second column provides the stock market ticker symbol. The third column provides the factor name composite of the property type with the ticker. The fourth column provides the name of the REIT, while the fifth column the market capitalization.

Table 2: Aggregate Summary of Sample REITs

Property Type	Market Cap (\$bn)	% Market Cap	Count	US Count	Sample $\%$ of US
Industrial (IN)	\$169.47	35.42%	4	13	30.77%
Hotel (LO)	\$86.39	18.06%	4	13	30.77%
Multifamily (MF)	\$87.86	18.36%	4	20	20.00%
Office (OF)	\$40.06	8.37%	5	19	26.32%
Mixed Use/Other (OT)	\$28.02	5.86%	4	126	3.17%
Retail (RT)	\$66.65	13.93%	4	32	12.50%
Total	\$478.45	100.00%	25	223	100.00%

This table aggregates values related to the 25 REITs used in this study. The first column gives the property type and total labels. The six property types are Industrial (IN), Hotel (LO), Multifamily (MF), Office (OF), Mixed Use/Other (OT), and Retail (RT). The second column provides the market capitalization (Market Cap). The third column provides proportion of each property type Market Cap compared to the total Market Cap in the sample. The fourth column provides the counts of the REITs by property type in the sample. The fifth column the number of REITs by property type in the US. The sixth column captures the proportion of the sample count to the US count of REITs.

While no sample selection is perfect, we feel our selection is broadly representative of the US REIT sector. The 25 REITs are included in the training data and then used in the Daily and Intraday Models to estimate CMBX risk partitions.

#### 1.2.2 Daily

For the period 11/2007-4/2019, we also have public daily time series from the Federal Reserve Bank of St. Louis FRED system. These data include benchmark corporate bond credits spreads for AAA and BBB ratings, the VIX volatility index, constant maturity (CMT) US Treasury yields to maturity. Following the estimation of the Daily Model, we also provide summary statistics for the public, private and estimated data of CMBX bid-ask spreads and CMBX risk partitions later in Section 3 Table 9. Finally, for the trading strategies and related ICAPM testing conducted during the Covid-19 pandemic period (246 days between 4/2020-4/2021) we obtain daily values of the market portfolio (Mkt-Rf, which consists of all NYSE, AMEX, and NASDAQ firms), small minus big (SMB), high minus low (HML), and momentum (MOM) indices from Ken French's website.<sup>2</sup>

### 1.2.3 Intraday

During the Covid-19 pandemic period of 4/2020-4/2021 we captured the daily values of the VIX, US Treasuries, and REITs during this period using the RapidAPI application with Yahoo! Finance. These data are summarized later in Section 4 Tables 14 and 15 at the start and at the end of the trading days during this period. We poll the data in 15 second intervals and the average delay over this period is about 1.15 seconds. The data is always 'most-recent' and reflective of updates driven by trading in the marketplace. The data polling for each day starts at approximately 9:30:15am EST and ends at approximately 4:15:00pm EST. There were some delays in reporting due to electronic communication lags on the internet in the application of up to 2 seconds. Additionally, some delays in reporting can take of up to 15 minutes for the VIX at the start of each trading day. All Federal holidays and are excluded with trading only taking place on days when both bond and stock markets are open. Reporting terminates early with early market closings market circuit breaker triggers.

# 2 Literature review

This section discusses some of the relevant literature in the domain of pricing liquidity.

<sup>&</sup>lt;sup>2</sup>See https://mba.tuck.dartmouth.edu/pages/faculty/ken.french/.

# 2.1 Bid-ask measures of liquidity

Bid-ask spreads represent the difference between the quotes of where market-makers stand ready to buy (bid-side) and sell (ask-side aka 'offered-side') securities at a specific point in time. While bid-ask spreads provide a rich measure of a security's liquidity, it stands to reason, that infrequently traded securities (where bid-ask spreads are less frequently observable) may present investors with greater opacity with respect to trading information which may, in turn, compound their illiquidity as noted in Hasbrouck (2009) and Fong, Holden and Trzcinka (2017).

Many of the classical microstructure models that investigate into issues of illiquidity are based on price and volume information content, as introduced in Kyle (1985), Easley, et al (1996), and O'Hara (1997) and more recently Abdi and Ranaldo (2017). As a result, most studies in microstructure focus on products such as publicly traded equities where price and volume data is available for empirical evaluation. However, this rich data is simply unavailable for many credit sensitive fixed income instruments, particularly in the securitized sector. Despite their size relative to equities, US fixed income markets can suffer from considerable illiquidity, particularly during times of stress as noted in Bao, Pan and Wang (2011) and Bao, O'Hara and Zhou (2018). This may be due to the over-the-counter (OTC) trading mechanism as discussed in Campello, Chen and Zhang (2008) and the comparatively less frequently traded characteristic for much of credit sensitive fixed income compared with equities as noted in Goldstein, Jiang and Ng (2017).

One sector with such limited pricing information is the CMBS sector and its indexed derivatives, CMBX. CMBX is an OTC indexed credit default swap which does not trade on electronic exchanges. Communication between market makers (dealers) and investors is done principally through Bloomberg terminal posts and sporadically.<sup>3</sup> Some data improvement in the area of Corporates has helped to advance the fixed income microstructure literature <sup>4</sup> and there have also been some advances in data and analysis for securitizations as discussed in Hollified, Nekyudov and Spatt (2017). At the same time, limited information for dealers on weekly trading volumes and inventories with lags under the Securities and Exchange Com-

<sup>&</sup>lt;sup>3</sup>See Appendix Section A.1.

<sup>&</sup>lt;sup>4</sup>See Hotchkiss and Ronen (2002), Bao, Pan and Wang (2011), Han and Zhou (2016), and Haddad, Moreira and Muir (2020) among others.

mission (SEC) embargo of 90 days and sporadic trading in the credit sensitive fixed income instruments, such as CMBX, still leave pockets of uncertainty regarding liquidity. Since end of day quotes reported to Markit by dealer are reliable, the technology to estimate bid-ask spreads for CMBX from a microstructure perspective is restricted to Roll (1984), Harris (1990), Hasbrouck (2009), Thompson and Waller (1987) and, most recently, Christopoulos (2020) which we implement. We then compare these microstructure estimates of liquidity in effective bid-ask spreads to estimates of reduced form theoretical liquidity to validate our daily estimation model of risk partitions.

The seminal work on bid-ask spreads derived from closing end-of-day prices is found in Roll (1984). As discussed in Lo and Wang (2000), solving for the effective bid-ask spread, s

$$-\frac{s^2}{4} = \text{COV} (\Delta P_t, \Delta P_{t+1})$$

$$s^2 = -4 \text{COV} (\Delta P_t, \Delta P_{t+1})$$

$$\sqrt{s^2} = \sqrt{-4 \text{COV} (\Delta P_t, \Delta P_{t+1})}$$

$$s = 2\sqrt{-\text{COV} (\Delta P_t, \Delta P_{t+1})}$$
(1)

yields a complex number when the first order autocovariance COV  $(\Delta P_t, \Delta P_{t+1}) > 0$ .

Roll (1984) and Harris (1990) address this problem by treating the value of s differently in different domains. Following Harris (1990), values for  $s^+$  apply to instances of positive autocovariance, while values for  $s^-$  apply to instances of negative autocovariance, such that:

$$s = \begin{cases} s^{+} = -2\sqrt{\text{COV}(\Delta P_{t}, \Delta P_{t+1})} & \text{for COV}(\Delta P_{t}, \Delta P_{t+1}) > 0\\ s^{-} = 2\sqrt{-\text{COV}(\Delta P_{t}, \Delta P_{t+1})} & \text{for COV}(\Delta P_{t}, \Delta P_{t+1}) \le 0 \end{cases}$$
(2)

This has the effect, as noted in Lo and Wang (2000) of 'preserving the sign of the covariance' in keeping with the empirical analyses of Roll (1984) and Harris (1990). However this preservation of sign also results in negative effective bid-ask spread estimates, s, as shown in Eq. (2). Negative bid-ask spreads imply market-makers inverting markets; standing ready to buy securities at *higher* prices than where they would sell them which would be ruinous to market makers. Additionally, since empirical observations of positive autocovariance in prices are frequently observed between 28% and 50% of observations in prior studies, reliance on Roll (1984) faces well known limitations.

Christopoulos (2020) addresses these limitations differently through the development of the Absolute Roll Measure. Our derivation of Christopoulos (2020) is more succinct. Consider the identities<sup>5</sup> for the complex number i

$$\sqrt{x} = i\sqrt{-x} \,\forall \, x \in \mathbb{R} \tag{3}$$

and

$$|ix| = |x| \ \forall \ x \in \mathbb{R} \tag{4}$$

Since the effective bid-ask spread, s, in Eq. (1) is undefined on the set of real numbers whenever  $t \in \mathbb{R}$ :  $COV(\Delta P_t, \Delta P_{t+1}) > 0$ , we resolve with Eqs. (3) and (4). Motivated by Harris (1990), we partition the domain of Eq. (1) into instances of positive and negative autocovariance,  $s^+$  and  $s^-$ , respectively. This allows us to propose a new alternative measure to estimate the bid-ask spread, the *Absolute Roll Measure*,  $\hat{s}$ , defined as

$$\hat{s} = |s| = \begin{cases} s^{+} = \left| 2i\sqrt{\text{COV}(\Delta P_{t}, \Delta P_{t+1})} \right| & t \in \mathbb{R}: \text{COV}(\Delta P_{t}, \Delta P_{t+1}) \geq 0 \\ s^{-} = \left| 2\sqrt{-\text{COV}(\Delta P_{t}, \Delta P_{t+1})} \right| & t \in \mathbb{R}: \text{COV}(\Delta P_{t}, \Delta P_{t+1}) < 0 \end{cases}$$

$$= \begin{cases} s^{+} = 2\sqrt{\text{COV}(\Delta P_{t}, \Delta P_{t+1})} & t \in \mathbb{R}: \text{COV}(\Delta P_{t}, \Delta P_{t+1}) \geq 0 \\ s^{-} = 2\sqrt{\text{COV}(\Delta P_{t}, \Delta P_{t+1})} & t \in \mathbb{R}: \text{COV}(\Delta P_{t}, \Delta P_{t+1}) < 0 \end{cases}$$
Since  $s^{+} = s^{-}$   $\therefore |s| = 2\sqrt{|\text{COV}(\Delta P_{t}, \Delta P_{t+1})|} \ \forall \ \mathbb{R}, \forall \ t$ 
But  $2\sqrt{|\text{COV}(\Delta P_{t}, \Delta P_{t+1})|} = 2\sqrt{|-\text{COV}(\Delta P_{t}, \Delta P_{t+1})|} \ \forall \ \mathbb{R}, \forall \ t$ 

$$\therefore \hat{s} = 2\sqrt{|-\text{COV}(\Delta P_{t}, \Delta P_{t+1})|} \ \forall \ \mathbb{R}, \forall \ t \blacksquare$$

This Absolute Roll Measure,  $\hat{s}$ , guarantees a strictly non-negative bid-ask spread observable for all price changes in all traded asset markets. For observations where  $COV(\Delta P_t, \Delta P_{t+1}) \geq 0$ , the interpretation is the corresponding effective bid-ask spread is the magnitude of s, regardless of whether s is real or imaginary, as found in Christopoulos (2020).

Finally, an alternative bid-ask spread estimator model we consider is the model of <sup>5</sup>See Simon and Blume (1994) for example.

Thompson and Waller (1987). This model also uses end-of-day prices to estimate bid-ask spreads from the absolute value of 5-day moving averages of changes in end-of-day closing prices,  $(|\overline{\Delta p_t}| = \frac{1}{5} \sum_{t=1}^{5} |\Delta p_t|)$ . The model is practical in that it guarantees a strictly non-negative bid-ask estimator result. It is also actively utilized in policy and by practitioners, as discussed in He and Mizrach (2017).

# 2.2 Reduced form measures of liquidity

While bid-ask spreads represent one measure of securities liquidity, there are others. For example, Amihud (2002) and Gilchrist and Zakrajsek (2012) each identify measures of liquidity for credit sensitive fixed income securities. In particular, certain areas of the literature are focused on disclosing default and liquidity components. Longstaff, Mithal and Neis (2005) find substantial concentration of default risk in corporate bond spreads that vary across credit ratings informed by implementing a theoretical model similar in class to Christopoulos and Jarrow (2018). Bao, Pan and Wang (2011) for example isolate factors apart from credit risk to be attributable to overall risk premia for that sector. They find illiquidity in Corporate bonds to increase with volatility and to be highly time varying. Gilchrist and Zakrajsek (2012) reveal statistically the excess bond premia in excess of default risk estimated using firm specific variables and the distance to default framework of Merton (1974). Their results indicate significant explanatory power for both the isolated default partition and the excess bond risk premia for several economic indicators including the civilian unemployment rate (UER). Broto and Lamas (2016) use principal component analysis (PCA) to construct liquidity indices for US fixed income demonstrating the use of PCA in this domain.

While similar in motivation to the earlier work, Christopoulos (2017) takes a different modelling approach and has a different focus on CMBS. The reduced form modelling approach in Christopoulos (2017) and Christopoulos and Jarrow (2018) simulated an economy consisting of 11 forward interest rates, 48 NCREIF property x regional property indices, and 6 property specific REIT indices under risk neutral conditions. The interest rate process used a simulation using high performance computing which consisted of forward rates following Heath, Jarrow and Morton (1992) and correlated Brownian Motion for all 65 factors. The simulation implemented loan-level credit state transitions using the Cox Process as mo-

tivated by Lando (1998). The state transitions of the loans reflected the historical state transitions of 1.92 million loan life observations over the period November 2007 to December 2014.

The risk adjusted loan level cashflows were first aggregated to the trust level and then allocated to the bond classes. This resulted in the capture of risk adjusted bond level cashflows. Prepayment risk was reasonably omitted in the asset pricing model due to the prepayment restrictions for commercial real estate loans which serve as collateral for CMBS. Since the simulation of the economy was conducted under risk neutral conditions, the valuation of the bond classes were also risk neutral, generating fair value prices, independent of market prices.

Christopoulos (2017) articulates risk components for CMBS and CMBX transforming simulated risk-neutral pricing into observable market pricing of default risk, rate risk, liquidity availability and excess liquidity availability. Sector specific innovations embedded within market pricing as found in Jarrow and Protter (2012) motivate Christopoulos and Jarrow (2018) to construct a set of common risk factors for the CMBX sector from Christopoulos (2017) risk partitions. These values are then indexed in Christopoulos and Jarrow (2018) giving rise to the statistical rejection of the weak form of CMBS market efficiency with findings based on assessment of extraordinary returns using the ICAPM of Merton (1990). As such, those sector indexed risk partitions are well-suited to comparison with bid-ask spread measures of liquidity as estimated in this study. However, the simulated values in both prior studies were limited to monthly frequency between 2007 and 2015. This is insufficient to the task of liquidity comparison in the microstructure context in this paper. With prohibitive costs of simulation and data we secure daily risk partition risk measures corresponding to Christopoulos (2017) and Christopoulos and Jarrow (2018) by estimating from the earlier primitives as described below.

# 3 Daily Model

This section introduces and validates the Daily Model of risk partition estimation. The Daily Model is based on findings of the reduced form technique in the prior literature applied to CMBX that is then fused with daily market information. We then validate the Daily Model

with data generated from four bid-ask microstructure models we implement.

# 3.1 Indices of CMBX

Christopoulos and Jarrow (2018) create indices of CMBX market spreads and the CMBX risk partitions introduced in Christopoulos (2017) for tractability. These indices of CMBX serve as sector-wide risk benchmarks for the CMBX sector. In Christopoulos and Jarrow (2018), for each of the six investment grade credit tranches  $k \in \{AAA, AJ/AS, AA, A, BBB, BBB-\}$  there were seven different issued CMBX series,  $l \in \{1, ..., 7\}$  (ie. CMBX Series 1, CMBX Series 2, ...CMBX Series 7). The prior work computed six average tranched CMBX market spreads (one for each of the six credit ratings) aggregated across seven CMBX Series,  $S_k(t)$ , as

$$S_k(t) = \frac{1}{7} \sum_{l=1}^{7} S_{kl}(t). \tag{6}$$

plus a sector level indexed CMBX market spread benchmark across all k credit ratings, computed as

$$\mathbb{S}(t) = \sum_{k=1}^{6} w_k \mathbb{S}_k(t) \tag{7}$$

where  $w_k$  is the weight of the  $k^{th}$  credit rating tranche determined by its subordination level. The weights based on subordination levels across all indices are  $\omega_{AAA} = 0.8222$ ,  $\omega_{AJ/AS} = 0.0514$ ,  $\omega_{AA} = 0.0514$ ,  $\omega_{A} = 0.0514$ ,  $\omega_{A} = 0.0257$ ,  $\omega_{BBB} = 0.0339$  and  $\omega_{BBB-} = 0.0154$ .

In this paper we take a different approach with the construction of a set of 'on-the-run' CMBX time series. In fixed income parlance, the most recent new issue security is considered the 'on-the-run' security and is also referred to as the 'current-coupon' as is typical in fixed-income sectors. The terminology borrows from the US Treasury vocabulary as discussed in Fleming (2001) and the residential mortgage market as discussed in Bhattacharjee and Hayre (2006). The on-the-run security is typically the most liquid of all outstanding similar issues within a sector, and coupons on securities for individual bonds (Treasuries) or tranches (within securitized capital structures) will be closest to the benchmark par/new-issue pricing for the sector. Additionally, loans underlying CMBS (which, in turn, collateralize CMBX) have interim principal payments (and sometimes losses of principal) prior to maturity as

discussed in Christopoulos (2017). This is due to principal amortization and manifestations of default in the form of loss and as well as default driven prepayments. They also may exhibit restricted prepayments of principal subject to prepayment lockout and prepayment penalties. It is well-known that default and prepayment of mortgage collateral exhibit statistically positive relationships with loan age early on in the life of the loan with loans exhibiting less frequency of default or prepayment the closer they are to the origination date. As such, on-the-run issues are less likely to exhibit idiosyncratic changes in promised payment profiles the more recent the issue is to its origination date.

The selection date for the on-the-run risk premium, S, with series classification, l, for credit rating class (aka 'tranche'),  $k \in [AAA, AJ/AS, AA, A, BBB, BBB-]$ , for all daily observation dates, t, is defined as follows:

$$S_{lkt} = \begin{cases} l = \text{Series } 4, & t \in [11/1/2007, 5/22/2008] \\ l = \text{Series } 5, & t \in [5/23/2008, 1/24/2013] \\ l = \text{Series } 6, & t \in [1/25/2013, 1/26/2014] \\ l = \text{Series } 7, & t \in [1/27/2014, 1/25/2015] \\ l = \text{Series } 8, & t \in [1/26/2015, 1/24/2016] \\ l = \text{Series } 9, & t \in [1/25/2016, 1/24/2017] \\ l = \text{Series } 10, & t \in [1/25/2017, 1/29/2018] \\ l = \text{Series } 11, & t \in [1/30/2018, 1/28/2019] \\ l = \text{Series } 12, & t \in [1/29/2019, 1/31/2020] \end{cases}$$

$$(8)$$

For on-the-run schedule dates, the differences in observations across tranches are due to normal amortization, maturity and default driven prepayments and losses from underlying loan collateral underlying the bonds, as well as different timing of series new issuance. For example, the AAA tranches for CMBX Series 1 paid off in late 2015, while CMBX Series 12 was not issued until 1/29/2019.

As noted, unlike Christopoulos and Jarrow (2018) we do not have the underlying loan and bond cashflow data which precludes us from simulating directly. We only have CMBX credit spreads, their changes and dates of observation. As such, resulting effective bid-ask spreads based on the microstructure models may introduce some noise and be misspecified relative to the underlying fundamental health of the collateral and market sentiment pricing. During the Great Financial Crisis, for example, over the period 5/23/2008-2/7/2013, CMBX Series

<sup>&</sup>lt;sup>6</sup>See for example Hayre, et al (1995, 2000), Christopoulos and Jarrow (2018), and Bond Market Association (2017) among others.

5 served as the on-the-run issue for 5 consecutive years. This is an unavoidable artefact of the market itself (and corresponding data) as no new CMBX Series were issued over this period.

As such, our choice to construct 'on-the-run' time series of Spreads seems appropriate. We use Eq. (8) to create the time series of CMBX market spreads and select  $S_{kl}(t)$  values noted in Eq. (6) from the previous work.

Additionally, each of the credit rated tranches also has a spread risk partition,  $S_{kl}^j$ , associated with each of the four CMBS risk factors  $j \in \{\text{default, rates, reglq, xslq}\}$ . The four indexed risk partitions indices,  $\mathbb{S}_k^j(t)$ , across all CMBX series, are given by

$$\mathbb{S}_k^j(t) = \frac{1}{7} \sum_{l=1}^7 S_{kl}^j(t). \tag{9}$$

This gives us 24 indexed risk partitions, one for each of the  $k \in \{1, ..., 6\}$  credit rating classes for each of  $j \in \{1, ..., 4\}$  risk factors.

To create the composite CMBX sector level risk factor indices, we take the weighted sum across all credit ratings

$$\mathbb{S}^{j}(t) = \sum_{k=1}^{6} w_k \mathbb{S}_k^{j}(t) \tag{10}$$

where  $w_k$  is the weight of the  $k^{th}$  credit rating tranche determined by its subordination level. As with CMBX market spreads, we also create 'on-the-run' time series risk partitions which use Eq. (8) to select the time series of CMBX risk partition values,  $S_{kl}^j(t)$  in Eq. (6).

# 3.2 Reduction of dimension

Table 3: Summary of Daily Model PCA training data

$type\_ticker$	mean	median	min	max	variance	stdev	count
VIX	22.1251	19.3000	10.7300	69.9600	115.4094	10.7429	92
IN_DRE	15.5298	14.3950	5.6200	32.6700	25.1089	5.0109	92
IN FR	14.4922	12.7050	2.0900	40.5800	73.8958	8.5963	92
IN_PLD	34.9227	35.5300	10.8800	64.8000	117.6452	10.8464	92
$IN\_SELF$	3.7005	3.7800	2.3800	4.4500	0.1826	0.4273	92
LO_HST	15.6474	16.2642	3.5732	23.7400	20.1085	4.4843	92
LO_MAR	38.7738	35.6409	12.8553	82.8000	285.1512	16.8864	92
LO_WYND	18.8808	15.4538	1.5214	41.0384	125.1303	11.1862	92
LO_MGM	19.9279	13.7750	2.6200	91.7100	297.1436	17.2379	92
MF_AVB	115.1334	122.1300	43.7600	173.2800	1013.2613	31.8318	92
$MF\_ELS$	15.9899	15.8763	6.8750	27.3750	23.7395	4.8723	92
$MF\_EQR$	50.1745	53.9450	17.9100	77.7000	210.1242	14.4957	92
$MF\_UDR$	22.8744	24.2100	7.9700	32.9900	32.5518	5.7054	92
OF_BXP	94.9709	101.1400	34.0400	142.2200	577.5131	24.0315	92
$OF\_CLI$	27.6958	28.0650	14.6800	40.6800	40.0223	6.3263	92
OF_HIW	33.5559	33.2700	17.8200	46.3100	34.6371	5.8853	92
$OF\_SLG$	76.3286	80.6000	11.1900	127.8500	809.1747	28.4460	92
OF_VNO	61.5884	61.5832	22.9945	91.3581	186.2377	13.6469	92
OT_BKD	22.6844	22.4500	3.0100	38.7200	73.2452	8.5583	92
$OT_NNN$	27.3768	26.4400	10.5300	42.0900	49.3787	7.0270	92
$OT\_PSB$	62.3994	58.9550	32.3200	86.5300	175.0194	13.2295	92
OT_WPC	43.4868	38.5000	18.3400	71.2900	272.3761	16.5038	92
RT_KIM	20.9846	19.4900	7.4900	42.0900	59.1813	7.6929	92
$RT\_REG$	47.7711	46.8450	24.3900	71.5700	124.9783	11.1794	92
RT SPG	114.7762	108.8476	27.2503	196.5700	1909.6103	43.6991	92
RT_TCO	57.3334	58.6900	15.6000	86.9500	349.8780	18.7050	92
TSY_3MO	0.3285	0.0700	0.0050	3.8400	0.5240	0.7239	92
$TSY\_5YR$	1.7756	1.6805	0.6140	4.0350	0.6180	0.7862	92
$TSY_10YR$	2.8003	2.7190	1.5040	4.3890	0.5643	0.7512	92
$TSY\_30YR$	3.7164	3.6970	2.5560	4.7630	0.4430	0.6656	92
rizes the 92 month	ly observation	s of training	lata used in	the Daily Mod	lel for the princ	rinal compon	ent analys

This table summarizes the 92 monthly observations of training data used in the Daily Model for the principal component analysis. The VIX is the CBOE volatility index. This is followed by the 25 REITs with the ticker a composite of the 6 property types industrial (IN), hotel/lodging (LO), multifamily (MF), mixed use/other (OT), office (OF) and retail (RT). Following the REITs are US Treasury yields with ticker representing the 4 maturities of 3 month, 5 year, 10 year and 30 year.

Table 3 provides a summary of the 92 training observations of the variables proxying for the simulated economy over the period 11/2007 thru 6/2015 that make up the economy in the Daily Model. They are used for the Daily Model estimation. From the training data summarized in Table 3 we estimate the risk partitions daily with the Daily Model, over the sample period of 11/2007-4/2019. The Daily Model uses a standard linear regression on the logs of the risk partitions reported in the monthly training set of Christopoulos and Jarrow (2018) against a digest of market data (25 REITs, 4 US Treasuries, and the VIX volatility index). Throughout the estimation of the Daily Model and (later the Intraday Model), for arithmetic reasons, we use the logarithm of these values as our starting point. Although the number of observations for the training set (92) is limited, these variables have a high degree of correlation among them. It is thus possible to create a lower-dimensional set of factors which contain enough information to explain most of the variance in the original set of 30.

To remove the cointegration we perform a principal components analysis (PCA), retaining enough factors to preserve 96% of the total variance at the observed dates.

For PCA in general form, let  $x_q(t)$  be the value of the q-th explanatory variable at time t. For PCA loadings  $p_{iq}$ ,  $i \in [1, 5], q \in [1, 30]$ . Assuming, we have all 30 factors, then the elements of the  $i \ge q$  matrix of principal components of the observed explanatory variables  $x_q(t)$  for all observed t, there exists a set of factors  $f_i(t)$  such that

$$x_q(t) = \sum_{i=1}^{30} p_{iq} f_i(t) \tag{11}$$

with each explanatory variable a linear combination of the factors  $f_i$  at all times t. But we want to reduce dimension because we have only 92 observations. And so when we reduce the number of components below 30 observable variables, to 5 variables, we determine the factors with matrix multiplication as

$$f_i(t) = \sum_{q=1}^{30} p_{iq} x_q(t), \ i \in \{1...5\}$$
 (12)

The factors  $f_i(t)$  are uncorrelated<sup>7</sup>, such that the partial sum is an unbiased estimator of  $x_q(t)$ ,

$$x_q(t) = \sum_{i=1}^{5} p_{iq} f_i(t) + \varepsilon_n(t), \quad \mathbb{E}[\varepsilon_n] = 0$$
 (13)

where the error term  $\mathbb{E}[\varepsilon_n] = \sum_{i=6}^{30} p_{iq} f_i(t)$ , which is the minimal possible error that can be introduced in a 1:1 transformation with the technique. For highly correlated series of variables  $x_q(t)$ , the proportion of their internal variance explained by even small partial sums can be large. From the covariance matrix of the explanatory variables we calculate the (30x30) matrix of eigenvectors and their corresponding eigenvalues. In <u>Table 4</u>, we report the eigenvalues all 30 principal components. Since none of the eigenvalues are less than zero, the variance covariance matrix is said to be positive semi-definite. As the first five eigenvalues have cumulative variance of 96.11%, we are comfortable with restricting our model to these first five principal components.

We transform our 30 variables into a digest of just 5 variables with  $x_q(t)$  the value of the

<sup>&</sup>lt;sup>7</sup>See the proof of this in <u>Section Appendix A.3</u>.

Table 4: Eigenvalues

Principal Components (1:30)	eigenvalue	variance (%)	cumulative variance (%)
Dim.1	18.1849	60.6163	60.6163
Dim.2	7.0359	23.4529	84.069
Dim.3	1.7472	5.8239	89.8932
Dim.4	1.2534	4.1778	94.0711
Dim.5	0.6139	2.0463	96.1174
$_{ m Dim.6}$	0.3176	1.0588	97.1762
Dim.7	0.2173	0.7243	97.9005
Dim.8	0.1257	0.4190	98.3196
Dim.9	0.1012	0.3374	98.6571
Dim.10	0.0853	0.2842	98.9413
Dim.11	0.0647	0.2155	99.1568
Dim.12	0.0444	0.1481	99.3049
Dim.13	0.0387	0.1288	99.4338
Dim.14	0.0341	0.1136	99.5475
Dim.15	0.0223	0.0744	99.6219
Dim.16	0.0174	0.0580	99.6800
Dim.17	0.0154	0.0514	99.7314
Dim.18	0.0132	0.0438	99.7752
Dim.19	0.0122	0.0406	99.8159
Dim.20	0.0115	0.0382	99.8541
Dim.21	0.0105	0.0349	99.8890
Dim.22	0.0080	0.0267	99.9158
Dim.23	0.0061	0.0202	99.9361
Dim.24	0.0044	0.0145	99.9507
Dim.25	0.0043	0.0144	99.9651
Dim.26	0.0035	0.0116	99.9768
Dim.27	0.0028	0.0093	99.9861
Dim.28	0.0024	0.0078	99.9940
Dim.29	0.0012	0.0039	99.9979
Dim.30	0.0006	0.0020	100.0000

This table summarizes the eigenvalues associated with the covariance matrix and eigenvectors.

Table 5: Eigenvectors of five principal components

Type	PropType	Ticker	Factor Name	PC1	PC2	PC3	PC4	PC5
VIX	NA	VIX	VIX	0.1748	0.0107	-0.3148	-0.2332	-0.4369
REIT	Industrial	DRE	IN_DRE	-0.1406	-0.2886	-0.097	-0.0937	$\begin{array}{c} -0.0245 \\ 0.1269 \\ 0.1225 \\ 0.1507 \end{array}$
REIT	Industrial	FR	IN_FR	-0.1334	-0.2833	-0.1556	-0.1863	
REIT	Industrial	PLD	IN_PLD	-0.1622	-0.2605	0.0067	-0.1089	
REIT	Industrial	SELF	IN_SELF	-0.1163	-0.0726	0.5916	-0.1331	
REIT	Hotel	HST	LO_HST	-0.2184	-0.0537	0.0704	$\begin{array}{c} 0.1801 \\ 0.2272 \\ 0.107 \\ -0.1244 \end{array}$	-0.0047
REIT	Hotel	MAR	LO_MAR	-0.2091	0.0519	-0.1853		-0.1395
REIT	Hotel	WYND	LO_WYND	-0.2161	0.1097	-0.122		0.1364
REIT	Hotel	MGM	LO_MGM	-0.0578	-0.3335	-0.1355		0.1721
REIT	Multifamily	AVB	MF_AVB	-0.2207	0.0755	0.1151	-0.0826	-0.1916
REIT	Multifamily	ELS	MF_ELS	-0.2157	0.1168	-0.0943	0.0968	-0.0964
REIT	Multifamily	EQR	MF_EQR	-0.2135	0.1001	0.1302	-0.0469	-0.3028
REIT	Multifamily	UDR	MF_UDR	-0.2201	-0.0111	0.0938	-0.0807	-0.3541
REIT REIT REIT REIT REIT	Office Office Office Office	BXP CLI HIW SLG VNO	OF_BXP OF_CLI OF_HIW OF_SLG OF_VNO	-0.2296 0.0629 -0.2195 -0.2249 -0.2131	-0.0055 -0.2369 -0.0137 -0.0927 -0.0941	0.0615 0.514 0.0278 -0.0024 0.0421	-0.0646 -0.0331 0.2056 0.0316 0.1063	-0.1693 -0.1139 -0.089 -0.068 -0.3489
REIT	Mixed/Other	BKD	OT_BKD	-0.2124	-0.0833	-0.0401	0.2277	0.1163
REIT	Mixed/Other	NNN	OT_NNN	-0.2213	0.0892	-0.0338	0.0709	0.1337
REIT	Mixed/Other	PSB	OT_PSB	-0.2124	0.0861	-0.0613	0.1464	0.2303
REIT	Mixed/Other	WPC	OT_WPC	-0.2079	0.1098	-0.1229	0.0496	0.3096
REIT	Retail	KIM	RT_KIM	-0.116	-0.3012	-0.0986	-0.2131	-0.0795
REIT	Retail	REG	RT_REG	-0.1783	-0.2091	-0.1494	-0.1061	-0.0406
REIT	Retail	SPG	RT_SPG	-0.2247	0.0994	-0.0166	-0.0345	0.0524
REIT	Retail	TCO	RT_TCO	-0.2183	0.0611	0.1079	-0.1874	0.1506
Treasury	NA	3MO	TSY_3MO	0.0137	-0.347	-0.0736	-0.2146	0.1305
Treasury	NA	5YR	TSY_5YR	0.0803	-0.311	-0.1406	0.3288	-0.1094
Treasury	NA	10YR	TSY_10YR	0.1142	-0.2744	-0.0077	0.4121	-0.0729
Treasury	NA	30YR	TSY_30YR	0.1228	-0.2373	0.1884	0.4231	0.0084

This table summarizes the principal component loadings (rotations). The first column indicates the type of the variable (REIT, VIX, or Treasury). The second column indicates the property type which is indicated for REITs and not applicable (NA) for the other variables. The third column provides the ticker symbol for the REITs and indication of VIX or the maturity for the Treasuries. The fourth column is the internal data name of the variable. The fifth through ninth columns (PCA1, ... PCA5) indicates the principal component loadings determined from the eigenvalues and eigenvectors.

q-th economic variable at time t. The eigenvectors consisting of the principal component loadings (aka 'rotations') are summarized in <u>Table 5</u>. This five-dimensional digest is used to construct our factor volatility explanatory variables (described below) for the risk component estimates. To expand on Eq. (12), the factor volatilities  $f_{it}$  are a function of the PCA loadings in Table 5 and the explanatory variables observed at time t.

Table 6: Summary of market spreads and simulated risk partitions as dependent variables

type_ticker	mean	median	min	max	variance	$\operatorname{stdev}$	count
market spread AAA market spread AJ market spread AA market spread A market spread BBB market spread BBB	118.1295 473.0770 981.0831 1555.3875 3053.6276 4252.5810	99.9420 390.9575 1000.9948 1609.9502 2703.6012 3952.0150	25.0000 55.1621 76.1364 89.0328 162.1271 207.4319	550.7100 1703.7300 2525.8600 3667.6336 10491.7654 14720.7284	8084.8459 81736.2628 261721.8298 604157.4778 3845199.4134 8199398.1483	89.9158 285.8955 511.5876 777.2757 1960.9180 2863.4591	92 92 92 92 92 92
def_AAA rates_AAA reglq_AAA xslq_AAA	8.0555 $52.8702$ $57.2037$ $134.1662$	1.6607 37.4083 44.8207 134.5824	$\begin{array}{c} 0.0277 \\ 1.6727 \\ 6.7286 \\ 0.0000 \end{array}$	195.8856 263.6903 262.8916 294.3972	790.1596 2712.6277 2294.4850 8930.3539	28.1098 52.0829 47.9008 94.5005	92 92 92 92
$\begin{array}{c} \operatorname{def}\_\operatorname{AJ} \\ \operatorname{rates}\_\operatorname{AJ} \\ \operatorname{reglq}\_\operatorname{AJ} \\ \operatorname{xslq}\_\operatorname{AJ} \end{array}$	56.0297 211.9356 200.6518 0.5256	3.3434 164.1067 221.3317 0.0000	0.0488 0.5000 0.0000 0.0000	1146.3424 1251.9229 432.8215 22.5208	42838.9678 37946.1184 10881.9687 9.9243	206.9758 194.7976 104.3167 3.1503	92 92 92 92
$egin{array}{l} \operatorname{def}_{-}\operatorname{AA} \\ \operatorname{rates}_{-}\operatorname{AA} \\ \operatorname{reglq}_{-}\operatorname{AA} \\ \operatorname{xslq}_{-}\operatorname{AA} \end{array}$	284.7420 561.9648 134.3763 0.0000	159.6041 617.7424 123.8860 0.0000	30.4583 0.0000 0.0000 0.0000	1735.0750 1506.2897 385.7624 0.0000	$107892.5071 \\ 111677.9404 \\ 13602.5250 \\ 0.0000$	328.4699 334.1825 116.6299 0.0000	92 92 92 92
$\begin{array}{c} \operatorname{def}_{-}A \\ \operatorname{rates}_{-}A \\ \operatorname{reglq}_{-}A \\ \operatorname{xslq}_{-}A \end{array}$	577.6416 721.9083 255.8375 0.0000	535.7316 708.1810 0.0000 0.0000	3.2881 $0.0000$ $0.0000$ $0.0000$	1959.6544 1788.8356 2564.8621 0.0000	$\begin{array}{c} 170249.2845 \\ 293804.1400 \\ 210292.7394 \\ 0.0000 \end{array}$	$\begin{array}{c} 412.6128 \\ 542.0370 \\ 458.5769 \\ 0.0000 \end{array}$	92 92 92 92
def_BBB rates_BBB reglq_BBB xslq_BBB	965.0640 1180.3222 908.2413 0.0000	740.0350 920.4655 0.0000 0.0000	7.5201 0.0000 0.0000 0.0000	2687.1501 5171.6783 5811.4664 0.0000	710113.0550 1298837.7798 1878471.1005 0.0000	842.6821 1139.6656 1370.5733 0.0000	92 92 92 92
def_BBBm rates_BBBm reglq_BBBm xslq_BBBm	2583.6984 527.5114 1141.3713 0.0000	2682.1252 0.0000 0.0000 0.0000	207.4319 0.0000 0.0000 0.0000	4683.3151 6610.2034 7660.1845 0.0000	1266031.2743 1342570.6397 4407188.9990 0.0000	1125.1806 1158.6935 2099.3306 0.0000	92 92 92 92

This table summarizes the 92 monthly observations of the markets spreads (mktsprd) and the simulated risk partitions indexed in Christopoulos and Jarrow (2018) in spread (bps) form. As noted in Eq. (15), the market spreads in this table serve as independent variables while the simulated risk partitions serves as dependent variables. The ticker is a composite of the 4 types of risk partitions default (def), interest rates (rates), liquidity (reglq) and excess liquidity (xslq) combined with the credit rating class names of AAA, AJ, AA, BBB and BBB- (BBBm).

Let  $R^T$  be the 5x30 PCA loadings matrix, and  $E^T$  the 30x92 matrix of the 30 variables over 92 observation dates, whose elements are  $x_q(t)$ . Then the factor matrix, F, calculated using matrix multiplication as the product of  $R^T$  and  $E^T$ , is

$$\mathbf{F} = \mathbf{R}^T \mathbf{E}^T = \begin{bmatrix} f_{1,1} & \cdots & f_{t,5} \\ \vdots & \ddots & \vdots \\ f_{92,1} & \cdots & f_{92,5} \end{bmatrix}$$
(14)

which yields a 92x5 matrix, the elements of which are the factors,  $f_{ti}$  that we use to capture the volatility in our model. We switch the notation  $f_{ti} \equiv f_{it}$  for the remaining calculations.

The factor volatility we determine from the PCA is  $v_i(t) \equiv [f_i(t) - f_i(t-1)]^2$ . For each month, t, to estimate the risk partition we begin with an opening value based on the previous two one-month volatilities of the variables  $v_i(t)$  and  $v_i(t-1)$  and the CMBX indexed market spread  $\mathbb{S}_k(t)$  for each credit rating class, as these are the values available to us for training purposes. Table 6 provides a summary of the market spreads used as independent variables and the risk partitions used as dependent variables for the OLS. The risk partitions are the proportional results from the 92 monthly simulations and indexing of Christopoulos and Jarrow (2018) over the period 11/2007 thru 6/2015. The initial risk component  $y_{jk}(t_0)$ ,  $j \in \{\text{def}, \text{rate}, ...\}$ ,  $k \in \{\text{AAA}, \text{AJ/AS}, ...\}$ , is given by

$$y_{jk}(t) = \alpha_{jk} + \sum_{i=1}^{5} \beta_{ijk} v_i(t) + \gamma_{ijk} v_i(t-1) + \delta_{ijk} \left[ v_i(t) - v_i(t-1) \right]^2 + \psi_k \mathbb{S}_k(t) + \varepsilon_{jk}(t) \quad (15)$$

The coefficients  $\{\alpha_{jk}, \beta_{ijk}, \gamma_{ijk}, \delta_{ijk}, \psi_k\}$  are determined through OLS by minimizing the sum of the squared error  $\sum_t \varepsilon_{jk}(t)$  with t indexed in months with  $\mathbb{E}[\varepsilon_{jk}(t)] = 0$ . In total, 16 coefficients are estimated, one for each of the 15 separate volatility components, and one for the indexed market spread corresponding to the credit rating class. Tables 7 and 8 capture the results of the 28 OLS in Eq (15). The OLS capture 90 monthly observations over the period 12/2007 - 6/2015. The panels in each table are organized by j-th risk partition and capture k = 6 investment grade ratings classes and the indexed aggregation across all credit ratings classes. 26 of 28 regressions are significant as measured by the F-test. Adjusted Rsquared values range from -0.11 to 0.95. Generally, the market spread is highly significant, but not always. The volatility factors also exhibit instances of significance from 0.10% to 10.00\% as well as many instances of insignificance. The third principal component for all three volatilities  $v_i(t)$ ,  $v_i(t-1)$ , and  $[v_i(t) - v_i(t-1)]^2$  appears to be consistently more significant across all regressions compared with other principal components. Interestingly, looking back to the third principal component in Table 5 we note the VIX is the largest value suggesting a large influence on the third principal component. Our purpose in this portion of the paper is to synthetically increase the frequency of risk partitions. These results are acceptable to that task and are next used to estimate the risk partitions, daily.

Table 7: OLS of default and rate risk partitions

Panel A, default	defAAA	defAJ	defAA	defA	defBBB	defBBBm	defALL
alpha	-10.7767*	-61.8278.	22.6571	590.1731***	993.1729**		50.5395*
	(4.1368)	(35.8692)	(74.1767)	(108.5017)	(102.68)	(115.3387)	(12.9274)
vPC1	6.5726**	43.0815**	26.1433	2.574	40.8001	86.041*	10.6503
	(2.2568)	(14.8203)	(25.8927)	(36.5177)	(30.0269)	(34.8689)	(4.4446)
vPC2	-10.9708.	-45.7803	-26.6861	-26.8434	-209.1309*	-210.8679*	-20.9231
	(6.3299)	(41.1619)	(72.0341)	(103.1963)	(86.2198)	(99.733)	(12.3307
vPC3	12.4146	145.5318	540.8874***	901.7894***	682.7787**		111.771*
	(13.7431)	(90.7345)	(146.2545)	(196.6739)	(161.0751)		(24.0677
vPC4	-12.5255	-140.2799*	-116.8911	37.1549	140.519	-140.3293	-20.232
	(10.4518)	(68.8229)	(118.749)	(166.813)	(137.3145)		(20.0894
vPC5	-9.6894	21.136	201.2984	-91.5091	-327.7452		-14.928
	(19.4001)	(127.7155)	(221.7927)	(311.7747)	(259.3555)		(37.4276
vm1PC1	5.7167*	25.5661	6.1495	3.3371	27.5806	61.3883	7.0571
	(2.4355)	(16.0857)	(28.2306)	(39.6899)	(32.4783)	(37.6898)	(4.8548
vm1PC2	-1.9859	11.382	66.1957	15.3863	-129.5663.		0.3806
VIII11 02	(5.7632)	(37.0799)	(65.329)	(93.4886)	(77.6678)		(11.1128
vm1PC3	-28.6259**	-59.0789	271.0683*	504.6081***	331.9641**		22.4011
VIIIII CO	(10.0256)	(63.9269)	(103.9853)	(145.0704)		(139.1512)	(17.4612
1DC4					(119.445)		
vm1PC4	-13.4965	-80.9366	-77.608	88.963	104.68	-96.5376	-16.964
100	(10.9315)	(71.8723)	(124.0292)	(174.2153)	(143.3167)		(20.9625
vm1PC5	5.2977	68.0332	307.9458	77.2959	-316.3798		11.1588
	(22.9842)	(150.0821)	(258.6374)	(363.3975)	(300.6296)		(43.7195
vvm1PC1	0.1493	0.9124	1.6063	3.2727.	3.2997*	2.1411	0.5178*
	(0.1067)	(0.7051)	(1.2157)	(1.702)	(1.4014)	(1.6201)	(0.2048)
vvm1PC2	0.6574	-3.3348	-10.3103	-13.4763	0.9685	4.0089	-0.8307
	(1.0164)	(6.5063)	(11.1916)	(15.8043)	(13.0475)	(15.1449)	(1.8922
vvm1PC3	-1.2238	-16.1888	-65.566**	-115.4626***	-86.9145**		-13.729*
	(1.8167)	(12.0746)	(19.4756)	(26.1569)	(21.416)	(24.7358)	(3.1985)
vvm1PC4	4.6921	81.5522*	76.0035	20.7611	57.2081	174.8484*	17.5748
	(4.9887)	(32.829)	(56.7403)	(79.8132)	(65.7941)	(76.3209)	(9.6051
vvm1PC5	-27.798	-179.6284	-526.2122*	-607.3429.	-58.3076	-413.3655	-88.5667
	(22.5853)	(144.9092)	(245.7735)	(344.6383)	(285.52)	(331.9571)	(41.4507
mktsprd_k	0.1318***	0.1184*	0.051	-0.0474	0.1798***		0.1496**
mkespra_k	(0.0258)	(0.0501)	(0.0464)	(0.0382)	(0.0215)	(0.0196)	(0.0298
F-test	13.46	7.108	5.59	3.91	13.76	36.07	12.94
	0	0	0	0	0	0	0
Adj. Rsq					0 0.6964	0 0.8631	0 0.6822
Adj. Rsq	0	0	0	0			
	0 0.6914	0 0.5234 ratesAJ	0 0.4521	0 0.3435	0.6964	0.8631	0.6822
Panel B, rates	0 0.6914 ratesAAA 0.7599	0 0.5234 ratesAJ 14.7093	0 0.4521 ratesAA -56.8643	0 0.3435 ratesA -610.7355***	0.6964 ratesBBB -1370***	0.8631 ratesBBBm -727.7179***	0.6822 ratesALL -37.0003***
Panel B, rates	0 0.6914 ratesAAA 0.7599 (2.3686)	0 0.5234 ratesAJ 14.7093 (27.5605)	0 0.4521 ratesAA -56.8643 (75.5302)	0 0.3435 ratesA -610.7355*** (117.5056)	0.6964 ratesBBB -1370*** (151.7)	0.8631 ratesBBBm -727.7179*** (154.6173)	0.6822 ratesALL -37.0003*** (7.4369)
Panel B, rates	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523.	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219	0 0.3435 ratesA -610.7355*** (117.5056) 12.529	0.6964 ratesBBB -1370*** (151.7) -8.244	0.8631 ratesBBBm -727.7179*** (154.6173) -24.0701	0.6822 ratesALL -37.0003*** (7.4369) -4.5644.
Panel B, rates alpha vPC1	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873)	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652)	0 0.3435 ratesA -610.7355*** (117.5056) 12.529 (39.5481)	0.6964 ratesBBB -1370*** (151.7) -8.244 (44.38)	0.8631 ratesBBBm -727.7179*** (154.6173) -24.0701 (46.7435)	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569)
Panel B, rates	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221**	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849	0 0.3435 ratesA -610.7355*** (117.5056) 12.529 (39.5481) -19.3482	0.6964 ratesBBB -1370*** (151.7) -8.244 (44.38) 151.7	0.8631  ratesBBBm -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575	0.6822 ratesALL -37.0003*** (7.4369) -4.5644. (2.5569) 1.9126
Panel B, rates alpha vPC1 vPC2	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272)	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485)	0 0.3435 ratesA -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971)	0.6822 ratesALL -37.0003*** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936)
Panel B, rates alpha vPC1	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734**	0 0.3435 ratesA -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238***	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019***	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521***	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539**
Panel B, rates alpha vPC1 vPC2 vPC3	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169)	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232)	0 0.3435 ratesA -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849)	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.9036) -50.3539** (13.8457)
Panel B, rates alpha vPC1 vPC2	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372*	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707.	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9	0.8631  ratesBBBm -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) 15.5986
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809)	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158)	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749)	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) 15.5986 (11.557)
Panel B, rates alpha vPC1 vPC2 vPC3	0 0.6914 ratesAAA 0.7599 (2.3886) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278	0 0.3435 ratesA -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650.	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 -50.3539** (13.8457) 15.5986 (11.557) -2.5607
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316)	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397)	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612)	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) 15.5986 (11.557) -2.5607 (21.5314)
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) -15.5986 (11.557) -2.5607 (21.5314) -3.0305
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597)	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457)	0 0.3435  rates A  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525)	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) 15.5986 (11.557) -2.5607 (21.5314) -3.0305 (2.7929)
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769*	0 0.5234 ratesAJ 14,7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 -50.3539** (13.8457) 15.5986 (11.557) -2.5607 (21.5314) -3.0305 (2.7929) -3.653
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907)	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521)	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743)	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393)
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544**	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478**	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4**	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405*	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) 1.55986 (11.557) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991*
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119)	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827)	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392)	0.6822  ratesALL  -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 -50.3539** (13.8457) 1.55986 (11.557) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451)
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) 6.1253
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239)	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923)	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (502.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928)	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) 15.5986 (11.557) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) 6.1253 (12.0593)
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.55544** (105.8827) 73.4133 (126.2923) -197.0646	0 0.3435  rates A  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) 6.1253
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC2 vm1PC3 vm1PC4	0 0.6914 rates AAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173)	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566)	0 0.3435  ratesA  -610.7355**** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137)	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (2.5569) 1.9126 (11.557) 15.5986 (11.557) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) 6.1253 (12.0593) -15.0279 (25.151)
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16) 0.0954	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173) -0.3552	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566) -1.4311	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539) -3.043	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3) -4.396*	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137) -3.5722	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) 6.1253 (12.0593) -15.0279 (25.151) -0.1345
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC2 vm1PC3 vm1PC4	0 0.6914 rates AAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173)	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566)	0 0.3435  ratesA  -610.7355**** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137)	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (2.5569) 1.9126 (13.8457) 15.5986 (11.557) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) 6.1253 (12.0593) 15.0279 (25.151)
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC2 vm1PC3 vm1PC4	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16) 0.0954	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173) -0.3552	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566) -1.4311	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539) -3.043	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3) -4.396*	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137) -3.5722	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) 6.1253 (12.0593) -15.0279 (25.151) -0.1345
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vvm1PC1	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16) 0.0954 (0.0611)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173) -0.3552 (0.5418)	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566) -1.4311 (1.2379)	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539) -3.043 (1.8433) 15.4617 (17.1159)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (502.9) (550. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3) -4.396* (2.071) 5.816 (19.28)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137) -3.5722 (2.1719) 3.5045 (20.3025)	0.6822  ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) 6.1253 (12.0593) -15.0279 (25.151) -0.1345 (0.1178) 1.1716 (1.0885)
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vvm1PC1	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16) 0.0954 (0.0611) 0.5601	0 0.5234 ratesAJ 14,7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173) -0.3552 (0.5418) 3.7786	0 0.4521 ratesAA -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566) -1.4311 (1.2379) 14.6394	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539) -3.043 (1.8433) 15.4617 (17.1159)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3) -4.396* (2.071) 5.816	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137) -3.5722 (2.1719) 3.5045 (20.3025)	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 -50.3539** (13.8457) 15.5986 (11.557) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) 6.1253 (12.0593) -15.0279 (25.151) -0.1345 (0.1178)
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vvm1PC1 vvm1PC5	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16) 0.0954 (0.0611) 0.5601 (0.5819) -0.1488	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173) -0.3552 (0.5418) 3.7786 (4.9992) 2.6962	0 0.4521  ratesAA  -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566) -1.4311 (1.2379) 14.6394 (11.3958) 63.071**	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539) -3.043 (1.8433) 15.4617 (17.1159) 109.5375***	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (502.9) (650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3) -4.396* (2.071) 5.816 (19.28) 132***	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137) -3.5722 (2.1719) 3.5045 (20.3025) 131.8938***	0.6822  ratesALL  -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) 15.5986 (11.557) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) 6.1253 (12.0593) -15.0279 (25.151) -0.1345 (0.1178) 1.1716 (1.0885) 6.3621****
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vvm1PC1 vvm1PC5 vvm1PC1 vvm1PC2 vvm1PC1	0 0.6914  ratesAAA  0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16) 0.0954 (0.0611) 0.5601 (0.5819) -0.1488 (1.0402)	0 0.5234 ratesAJ 14,7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173) -0.3552 (0.5418) 3.7786 (4.9992) 2.6962 (9.2776)	0 0.4521  ratesAA  -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566) -1.4311 (1.2379) 14.6394 (11.3958) 63.071** (19.8309)	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539) -3.043 (1.8433) 15.4617 (17.1159) 109.5375*** (28.3275)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3) -4.396* (2.071) 5.816 (19.28) 132*** (31.65)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137) -3.5722 (2.1719) 3.5045 (20.3025) 131.8938*** (33.1596)	0.6822  ratesALL  -37.0003** (7.4369) 1.9126 (7.0936) -50.3539** (13.8457) 1.55986 (11.557) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) 6.1253 (12.0593) -15.0279 (25.151) -0.1345 (0.1178) 1.1716 (1.0885) 6.3621*** (1.84)
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vvm1PC1 vvm1PC5	0 0.6914  rates AAA  0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16) 0.0954 (0.0611) 0.5601 (0.5819) -0.1488 (1.0402) -5.9098*	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173) -0.3552 (0.5418) 3.7786 (4.9992) 2.6962 (9.2776) -54.4616*	0 0.4521  ratesAA  -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566) -1.4311 (1.2379) 14.6394 (11.3958) 63.071** (19.8309) -50.1199	0 0.3435  ratesA  -610.7355**** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539) -3.043 (1.8433) 15.4617 (17.1159) 109.5375*** (28.32275) -33.0714	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3) -4.396* (2.071) 5.816 (19.28) 132*** (31.65) -78.64	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137) -3.5722 (2.1719) 3.5045 (20.3025) 131.8938*** (33.1596) -116.4152	0.6822  ratesALL  -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) -6.1253 (12.0593) -15.0279 (25.151) -0.1345 (0.1178) 1.1716 (1.0885) 6.3621****
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vvm1PC1 vvm1PC5 vvm1PC1 vvm1PC2 vvm1PC1	0 0.6914 ratesAAA 0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16) 0.0954 (0.0611) 0.5601 (0.5819) -0.1488 (1.0402) -5.9098* (2.8564)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173) -0.3552 (0.5418) 3.7786 (4.9992) 2.6962 (9.2776) -54.4616* (25.2245)	0 0.4521  ratesAA  -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566) -1.4311 (1.2379) 14.6394 (11.3958) 63.071** (19.8309) -50.1199 (57.7756)	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539) -3.043 (1.8433) 15.4617 (17.1159) 109.5375*** (28.3275) -33.0714 (86.4365)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (502.9) (650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3) -4.396* (2.071) 5.816 (19.28) 132*** (31.65) -78.64 (97.24)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137) -3.5722 (2.1719) 3.5045 (20.3025) 131.8938*** (33.1596) -116.4152 (102.312)	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) 15.5986 (11.557) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) -6.1253 (12.0593) -15.0279 (25.151) -0.1345 (0.1178) 1.1716 (1.0885) 6.3621*** (1.84) -14.7355** (5.5256)
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vvm1PC1 vvm1PC5 vvm1PC1 vvm1PC2	0 0.6914  ratesAAA  0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16) 0.0954 (0.0611) 0.5601 (0.5819) -0.1488 (1.0402) -5.9098* (2.8564) 10.0181	0 0.5234 ratesAJ 14,7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173) -0.3552 (0.5418) 3.7786 (4.9992) 2.6962 (9.2776) -54.4616* (25.2245) 95.6128	0 0.4521  ratesAA  -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566) -1.4311 (1.2379) 14.6394 (11.3958) 63.071** (19.8309) -50.1199 (57.7756) 498.4666.	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539) -3.043 (1.8433) 15.4617 (17.1159) 109.5375*** (28.3275) -33.0714 (86.4365) 518.6177	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (502.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3) -4.396* (2.071) 5.816 (19.28) 132*** (31.65) -78.64 (97.24) 131.5	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137) -3.5722 (2.1719) 3.5045 (20.3025) 131.8938*** (33.1596) -116.4152 (102.312) 561.9252	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) -6.1253 (12.0593) -15.0279 (25.151) -0.1345 (0.1178) 1.1716 (1.0885) 6.3621*** (1.84) -14.7355** (5.5256) 40.7162.
Panel B, rates  alpha  vPC1  vPC2  vPC3  vPC4  vPC5  vm1PC1  vm1PC2  vm1PC3  vm1PC4  vm1PC5  vvm1PC1  vvm1PC1  vvm1PC1  vvm1PC2  vvm1PC1  vvm1PC2  vvm1PC1  vvm1PC2  vvm1PC3  vvm1PC3  vvm1PC4  vvm1PC3	0 0.6914  rates AAA  0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16) 0.0954 (0.0611) 0.5601 (0.5819) -0.1488 (1.0402) -5.9098* (2.8564) 10.0181 (12.9316)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173) -0.3552 (0.5418) 3.7786 (4.9992) 2.6962 (9.2776) -54.4616* (25.2245) 95.6128 (111.3426)	0 0.4521  ratesAA  -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566) -1.4311 (1.2379) 14.6394 (11.3958) 63.071** (19.8309) -50.1199 (57.7756) 498.4666 (250.2581)	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539) -3.043 (1.8433) 15.4617 (17.1159) 109.5375*** (28.3275) -33.0714 (86.4365) 518.6177 (373.238)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3) -4.396* (2.071) 5.816 (19.28) 132*** (31.65) -78.64 (97.24) 131.5 (422)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137) -3.5722 (2.1719) 3.5045 (20.3025) 131.8938*** (33.1596) -116.4152 (102.312) 561.9252 (445.0051)	0.6822  ratesALL  -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) -6.1253 (12.0593) -15.0279 (25.151) -0.1345 (0.1178) 1.1716 (1.0885) 6.3621*** (1.844) -14.7355** (5.5256) 40.7162. (23.8458)
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vvm1PC1 vvm1PC5 vvm1PC1 vvm1PC2 vvm1PC1	0 0.6914  ratesAAA  0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16) 0.0954 (0.0611) 0.5601 (0.5819) -0.1488 (1.0402) -5.9098* (2.8564) 10.0181 (12.9316) 0.3738***	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173) -0.3552 (0.5418) 3.7786 (4.9992) 2.6962 (9.2776) -54.4616* (25.2245) 95.6128 (111.3426) 0.4311****	0 0.4521  ratesAA  -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566) -1.4311 (1.2379) 14.6394 (11.3958) 63.071** (19.8309) -50.1199 (57.7756) 498.4666. (250.2581) 0.6047***	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539) -3.043 (1.8433) 15.4617 (17.1159) 109.5375*** (28.3275) -33.0714 (86.4365) 518.6177 (373.238) 0.7357***	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (550. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3) -4.396* (2.071) 5.816 (19.28) 132*** (31.65) -78.64 (97.24) 131.5 (422) 0.6704***	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137) -3.5722 (2.1719) 3.5045 (20.3025) 131.8938*** (33.1596) -116.4152 (102.312) 561.9252 (445.0051) 0.5004***	0.6822  ratesALL  -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) -0.1345 (0.1178) 1.1716 (1.0885) 6.3621*** (1.84) -14.7355** (5.5256) 40.7162. (23.8458) 0.5991***
Panel B, rates alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vvm1PC1 vvm1PC1 vvm1PC2 vvm1PC1 vvm1PC2 vvm1PC3 vvm1PC4 vvm1PC3 vvm1PC4 vvm1PC3 vvm1PC4	0 0.6914  rates AAA  0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16) 0.0954 (0.0611) 0.5601 (0.5819) -0.1488 (1.0402) -5.9098* (2.8564) 10.0181 (12.9316) 0.3738*** (0.0148)	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173) -0.3552 (0.5418) 3.7786 (4.9992) 2.6962 (9.2776) -54.4616* (25.2245) 95.6128 (111.3426) 0.4311**** (0.0385)	0 0.4521  ratesAA  -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566) -1.4311 (1.2379) 14.6394 (11.3958) 63.071** (19.8309) -50.1199 (57.7756) 498.4666 (250.2581) 0.6047*** (0.0473)	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539) -3.043 (1.8433) 15.4617 (17.1159) 109.5375*** (28.3275) -33.0714 (86.4365) 518.6177 (373.238) 0.7357*** (0.0413)	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (202.9) 650. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3) -4.396* (2.071) 5.816 (19.28) 132*** (31.65) -78.64 (97.24) 131.5 (422) 0.6704*** (0.0318)	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137) -3.5722 (2.1719) 3.5045 (20.3025) 131.8938*** (33.1596) -116.4152 (102.312) 561.9252 (445.0051) 0.5004*** (0.0262)	0.6822  ratesALL  -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) -6.1253 (12.0593) -15.0279 (25.151) -0.1345 (0.1178) 1.1716 (1.0885) 6.3621*** (1.84) -14.7355** (5.5256) 40.7162. (23.8458) 0.5991*** (0.0172)
Panel B, rates  alpha  vPC1  vPC2  vPC3  vPC4  vPC5  vm1PC1  vm1PC2  vm1PC3  vm1PC4  vm1PC5  vvm1PC1  vvm1PC1  vvm1PC1  vvm1PC2  vvm1PC1  vvm1PC2  vvm1PC1  vvm1PC2  vvm1PC3  vvm1PC3  vvm1PC4  vvm1PC3	0 0.6914  ratesAAA  0.7599 (2.3686) 1.2789 (1.2922) -11.0221** (3.6243) 3.5193 (7.8689) 12.9372* (5.9844) -8.1576 (11.1079) 1.0172 (1.3945) -6.8769* (3.2998) -0.9608 (5.7403) 4.9163 (6.259) -14.7768 (13.16) 0.0954 (0.0611) 0.5601 (0.5819) -0.1488 (1.0402) -5.9098* (2.8564) 10.0181 (12.9316) 0.3738***	0 0.5234 ratesAJ 14.7093 (27.5605) -22.3523. (11.3873) 2.2831 (31.6272) -32.378 (69.7169) 98.5707. (52.8809) 36.4812 (98.1316) -8.2242 (12.3597) -36.4399 (28.4907) 58.8951 (49.119) 78.5986 (55.2239) 7.9833 (115.3173) -0.3552 (0.5418) 3.7786 (4.9992) 2.6962 (9.2776) -54.4616* (25.2245) 95.6128 (111.3426) 0.4311****	0 0.4521  ratesAA  -56.8643 (75.5302) 3.1219 (26.3652) -65.0849 (73.3485) -504.5734** (148.9232) 94.672 (120.9158) -92.4278 (225.8397) 16.5593 (28.7457) -109.1081 (66.521) -296.5544** (105.8827) 73.4133 (126.2923) -197.0646 (263.3566) -1.4311 (1.2379) 14.6394 (11.3958) 63.071** (19.8309) -50.1199 (57.7756) 498.4666. (250.2581) 0.6047***	0 0.3435  ratesA  -610.7355*** (117.5056) 12.529 (39.5481) -19.3482 (111.76) -852.9238*** (212.9947) 8.6312 (180.6559) 216.7334 (337.6472) 13.804 (42.9835) -57.646 (101.2467) -509.8478** (157.109) -4.9955 (188.6725) 39.5006 (393.5539) -3.043 (1.8433) 15.4617 (17.1159) 109.5375*** (28.3275) -33.0714 (86.4365) 518.6177 (373.238) 0.7357***	0.6964  ratesBBB  -1370*** (151.7) -8.244 (44.38) 151.7 (127.4) -1019*** (238) -109.9 (550. (383.3) -1.232 (48) 73.94 (114.8) -583.4** (176.5) -38.09 (211.8) 540 (444.3) -4.396* (2.071) 5.816 (19.28) 132*** (31.65) -78.64 (97.24) 131.5 (422) 0.6704***	0.8631  ratesBBBm  -727.7179*** (154.6173) -24.0701 (46.7435) 103.2575 (133.6971) -985.9521*** (249.4849) 34.8594 (213.3749) 284.9899 (402.612) -26.5671 (50.525) 50.1415 (120.743) -407.5405* (186.5392) 20.884 (222.7928) 113.6629 (467.6137) -3.5722 (2.1719) 3.5045 (20.3025) 131.8938*** (33.1596) -116.4152 (102.312) 561.9252 (445.0051) 0.5004***	0.6822 ratesALL -37.0003** (7.4369) -4.5644. (2.5569) 1.9126 (7.0936) -50.3539** (13.8457) -2.5607 (21.5314) -3.0305 (2.7929) -3.653 (6.393) -20.991* (10.0451) -0.1345 (0.1178) 1.1716 (1.0885) 6.3621*** (1.84) -14.7355** (5.5256) 40.7162. (23.8458) 0.5991****

This Table 7 summarizes the estimates of the OLS in Eq. (15) of the form  $y_{jk}(t) = \alpha_{jk} + \sum_{i=1}^{5} \beta_{ijk} v_i(t) + \gamma_{ijk} v_i(t-1) + \delta_{ijk} \left[v_i(t) - v_i(t-1)\right]^2 + \psi_k \mathbb{S}_k(t) + \varepsilon_{jk}(t)$ . The dependent variables are the risk partitions of default (Panel A) and rates (Panel B) for each of the investment grade credit rating classes AAA thru BBB- as well as the aggregation sector wide CMBX benchmark across all classes. The independent variables are the volatilities  $v_i(t)$ ,  $v_i(t-1)$ , and  $[v_i(t) - v_i(t-1)]^2$  labeled vPC#, vm1PC# and vvm1PC#, respectively. The other covariate is the observed CMBX spread for such ratings,  $\mathbb{S}_k(t)$ . The estimates are provided for each row with the standard error of the estimate immediately below in parentheses. The F-test statistic and p-value and the Adjusted R-squared are provided in the final three rows. The columns indicate the credit rating class. The significance codes of '\*\*\*, '\*\*, and '' indicate statistical significance at the 0.001, 0.01, 0.05 and 0.1 levels, respectively.

Table 8: OLS of liquidity and excess liquidity risk partitions

anel A, regular liquidity	rglqAAA	rglqAJ	rglqAA	rglqA	rglqBBB	rglqBBBm	rglqALL
alpha	18.4029***	118.9706***	1.7014	-313.2145***	-612.6711***	-688.2123***	-13.5367.
	(4.2406)	(19.9913)	(44.0622)	(88.309)	(111.1486)	(80.0271)	(7.6505)
vPC1	-4.8539*	-3.8118	3.0006	20.6221	7.3018	-25.764	-6.0858*
	(2.3134)	(8.2599)	(15.3807)	(29.7215)	(32.5034)	(24.1936)	(2.6304)
vPC2	13.5444*	-8.5059	-16.3051	-37.9445	49.0844	131.2454.	19.0093*
D.C.a	(6.4887)	(22.9411)	(42.7894)	(83.9909)	(93.3309)	(69.1991)	(7.2974)
vPC3	-12.5931		-385.2747***	-603.8999***	-510.9596**	-411.5784**	-61.4267**
vPC4	(14.0879) $6.6246$	(50.5699) $62.5189$	(86.8776) $35.5547$	(160.0719) -52.19	(174.36) -91.4001	(129.1287) $29.2656$	(14.2434) 4.6369
VI C4	(10.714)	(38.3577)	(70.5389)	(135.7683)	(148.6397)	(110.4389)	(11.889)
vPC5	6.8217	-93.1821	-64.7353	110.5509	407.0535	489.4531*	17.4923
V1 C3	(19.8867)	(71.1808)	(131.7486)	(253.7519)	(280.7463)	(208.3845)	(22.1499)
vm1PC1	-2.9833	1.9172	7.891	12.1455	11.1894	-2.9167	-4.0258
VIIIII CI	(2.4966)	(8.9652)	(16.7695)	(32.3034)	(35.157)	(26.1508)	(2.8731)
vm1PC2	0.8198	-34.084	-53.6298	-32.8496	23.6343	51.3935	3.2702
	(5.9078)	(20.666)	(38.8065)	(76.0899)	(84.0736)	(62.4943)	(6.5766)
vm1PC3	27.6438**	-43.2358	-242.5588***	-367.3343**	-300.0991*	-198.4602*	-1.4145
	(10.2771)	(35.629)	(61.769)	(118.0721)	(129.2964)	(96.5492)	(10.3337
vm1PC4	16.0564	38.2344	32.2554	-65.7412	-55.6258	60.6023	10.8392
	(11.2057)	(40.0572)	(73.6754)	(141.793)	(155.137)	(115.3134)	(12.4057
vm1PC5	-1.2835	-109.2202	-121.3679	-9.8251	353.6387	509.7061*	3.8662
	(23.5607)	(83.6466)	(153.6349)	(295.7674)	(325.4245)	(242.0282)	(25.8734
vvm1PC1	-0.2354*	-0.379	-1.0069	-2.0164	-2.2893	-2.2005.	-0.3834*
	(0.1094)	(0.393)	(0.7221)	(1.3853)	(1.517)	(1.1241)	(0.1212)
vvm1PC2	-0.7587	1.7791	7.6116	10.2662	4.0287	0.0264	-0.3405
	(1.0419)	(3.6262)	(6.648)	(12.8631)	(14.1237)	(10.5082)	(1.1198
vvm1PC3	1.0583	17.6926*	48.6955***	79.6236***	67.6857**	52.3923**	7.3681**
	(1.8623)	(6.7296)	(11.5688)	(21.289)	(23.1823)	(17.1628)	(1.8929)
vvm1PC4	1.4512	-14.8557	-11.3304	14.7181	-20.0621	-128.8652*	-2.8393
	(5.1139)	(18.2969)	(33.7047)	(64.9596)	(71.2205)	(52.9548)	(5.6844)
vvm1PC5	30.8461	186.1648*	319.9671*	399.533	41.9613	-157.6773	47.8575
	(23.1518)	(80.7635)	(145.9936)	(280.4994)	(309.0687)	(230.3264)	(24.5308
$mktsprd\_k$	0.1689***	0.1252***	0.2053***	0.2918***	0.221***	0.2394***	0.2513**
	(0.0265)	(0.0279)	(0.0276)	(0.0311)	(0.0233)	(0.0136)	(0.0177
	(0.0203)						
F-test	12.84	3.418	6.791	9.217	8.12	25.98	15.66
			6.791 0 0.51	9.217 0 0.5963	8.12 0 0.5614	25.98 0 0.8179	15.66 $0$ $0.725$
Adj. Rsq	12.84 0 0.6803	3.418 0.0002	0	0 0.5963	0	0 0.8179	0 0.725
Adj. Rsq	12.84	3.418 0.0002 0.303	0 0.51	0	0 0.5614	0 0.8179 xslqBBBm	0 0.725 xslqALL
Adj. Rsq anel B, excess liquidity alpha	12.84 0 0.6803 xslqAAA	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481)	0 0.51 xslqAA 0.1516*** (0.0196)	0 0.5963 xslqA 0.193*** (0.0173)	0 0.5614 xslqBBB 0.2314*** (0.0178)	0 0.8179 xslqBBBm 0.1223. (0.0651)	0 0.725 xslqALL 17.303 (11.2882)
Adj. Rsq	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319.	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308	0 0.51 xslqAA 0.1516*** (0.0196) -0.0108	0 0.5963 xslqA 0.193*** (0.0173) -0.0074	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063	0 0.8179 xslqBBBm 0.1223. (0.0651) -0.0306	0 0.725 xslqALL 17.303 (11.2882) 0.4606
Adj. Rsq anel B, excess liquidity alpha vPC1	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288)	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612)	0 0.51 xslqAA 0.1516*** (0.0196) -0.0108 (0.0068)	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058)	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052)	0 0.8179 xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197)	0 0.725 xslqALL 17.303 (11.2882 0.4606 (3.881)
Adj. Rsq anel B, excess liquidity alpha	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215	0 0.51 xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403*	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115	0 0.8179 xslqBBm 0.1223. (0.0651) -0.0305 (0.0197) 0.0585	0 0.725 xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245)	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699)	0 0.51 xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019)	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165)	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149)	0 0.8179 xslqBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563)	0 0.725 xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671
Adj. Rsq anel B, excess liquidity alpha vPC1	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244	0 0.51 xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889*	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736*	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068*	0 0.8179 xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254	0 0.725 xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719**
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148)	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746)	0 0.51 xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386)	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314)	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279)	0 0.8179 xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051)	0 0.725 xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611	0 0.51 xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566	0 0.725 xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266)	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842)	0 0.51 xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313)	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267)	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238)	0 0.8179  xslqBBBm 0.1223 (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899)	0 0.725 xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542)
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404	0 0.51 xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019	0 0.725 xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695)	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273)	0 0.51  xslqAA  0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585)	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498)	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449)	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696)	0 0.725 xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214 (32.6817
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152.	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497	0 0.51 xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077	0 0.725 xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191)	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664)	0 0.51  xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074)	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063)	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056)	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213)	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392)
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573	0 0.51  xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359*	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056)	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009	0 0.725 xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868)	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531)	0 0.51  xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172)	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149)	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056) 0.0121 (0.0135)	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509)	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156 (9.7037)
Adj. Rsq  anel B, excess liquidity alpha  vPC1  vPC2  vPC3  vPC4  vPC5  vm1PC1	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309	0 0.51  xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172) 0.0677*	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149) 0.0476*	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056) 0.0121 (0.0135) 0.0431*	0 0.8179  xslqBBBm 0.1223 (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156 (9.7037) -49.0566*
Adj. Rsq  anel B, excess liquidity alpha  vPC1  vPC2  vPC3  vPC4  vPC5  vm1PC1  vm1PC2  vm1PC2	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958)	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639)	0 0.51	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232)	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056) 0.0121 (0.0135) 0.0431* (0.0207)	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786)	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156 (9.7037) -49.0566* (15.2471
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958) -20.5648	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639) -0.4027	0 0.51  xslqAA  0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172) 0.0677* (0.0274) -0.0238	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232) -0.0197	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056) 0.0121 (0.0135) 0.0431* (0.0207) -0.0171	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786) 0.0589	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719*** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156 (9.7037) -49.0566* (15.2471 -16.1122
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC3	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) (3.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958) -20.5648 (23.8742)	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639) -0.4027 (0.2967)	0 0.51  xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172) 0.0677* (0.0274) -0.0238 (0.0327)	0 0.5963 xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232) -0.0197 (0.0278)	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056) 0.0121 (0.0135) 0.0431* (0.0207) -0.0171 (0.0248)	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786) 0.0589 (0.0589	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156 (9.7037) -49.0566* (15.2471 -16.1122 (18.3044
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC2	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958) -20.5648 (23.8742) -31.2948	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639) -0.4027 (0.2967) -0.1524	0 0.51	0 0.5963  xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232) -0.0197 (0.0278) 0.0375	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056) 0.0121 (0.0135) 0.0431* (0.0207) -0.0171 (0.0248) -0.0012	0 0.8179  xslqBBBm 0.1223 (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786) 0.0589 (0.0939) 0.3677.	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156 (9.7037) -49.0566* (15.2471 -16.1122 (18.3044 -52.344 -52.344
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC4	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958) -20.5648 (23.8742) -31.2948 (50.1971)	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639) -0.4027 (0.2967) -0.1524 (0.6197)	0 0.51  xslqAA  0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172) 0.0677* (0.0274) -0.0238 (0.0327) 0.0488 (0.0682)	0 0.5963  xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232) -0.0197 (0.0278) 0.0375 (0.0581)	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056) 0.0121 (0.0135) 0.0431* (0.0207) -0.0171 (0.0248) -0.0012 (0.0521)	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786) 0.0589 (0.0939) 0.3677. (0.197)	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156 (9.7037) -49.0566* (15.2471 -16.1122 (18.3044 -52.344 (38.1757
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC3	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958) -20.5648 (23.8742) -31.2948 (50.1971) 0.158	3.418 0.0002 0.303 xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639) -0.4027 (0.2967) -0.1524 (0.6197) 0.0011	0 0.51  xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172) 0.0677* (0.0274) -0.0238 (0.0327) 0.0488 (0.0682) 0.0001	0 0.5963  xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232) -0.0197 (0.0278) 0.0375 (0.0581) 0.0001	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0156) 0.0121 (0.0135) 0.0431* (0.0207) -0.00171 (0.0248) -0.0012 (0.0521)	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786) 0.0589 (0.0939) 0.3677. (0.197) 0.0002	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156 (9.7037) -49.0566* (15.2471 -16.1122 (18.3044 -52.344 (38.1757 -0.0722
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vm1PC4 vm1PC5	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958) -20.5648 (23.8742) -31.2948 (50.1971) 0.158 (0.2331)	3.418 0.0002 0.303  xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639) -0.4027 (0.2967) -0.1524 (0.6197) 0.0011 (0.0029)	0 0.51  xslqAA 0.1516*** (0.0196) -0.0108 (0.0688) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172) 0.0677* (0.0274) -0.0238 (0.0327) 0.0488 (0.0682) 0.0001 (0.0003)	0 0.5963  xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232) -0.0197 (0.0278) 0.0375 (0.0581) 0.0001 (0.0003)	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056) 0.0121 (0.0135) 0.0431* (0.0207) -0.0171 (0.0248) -0.0012 (0.0521) 0.0002 (0.0002)	0 0.8179  xslqBBBm 0.1223 (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786) 0.0589 (0.0939) 0.3677. (0.197) 0.0002 (0.0009)	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156 (9.7037) -49.0566* (15.2471 -16.1122 (18.3044 -52.344 (38.1757 -0.0722 (0.1789)
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC4	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958) -20.5648 (23.8742) -31.2948 (50.1971) 0.158 (0.2331) -0.6102	3.418 0.0002 0.303  xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639) -0.4027 (0.2967) -0.1524 (0.6197) 0.0011 (0.0029) 0.0014	0 0.51  xslqAA  0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172) 0.0677* (0.0274) -0.0238 (0.0327) 0.0488 (0.0682) 0.0001 (0.0003) -0.0003	0 0.5963  xslqA 0.193**** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232) -0.0197 (0.0278) 0.0375 (0.0581) 0.0001 (0.0003) -0.0018	0 0.5614  xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056) 0.0121 (0.0135) 0.0431* (0.0207) -0.0171 (0.0248) -0.0012 (0.02521) 0.0002 (0.0002)	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786) 0.0589 (0.0939) 0.3677. (0.197) 0.0002 (0.0009) 0.001	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719*** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156 (9.7037) -49.0566* (15.2471 -16.1122 (18.3044 (38.1757 -0.0722 (0.1789) 1.3111
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vwm1PC4 vwm1PC5 vvm1PC1 vvm1PC5 vvm1PC1 vvm1PC5	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958) -20.5648 (23.8742) -31.2948 (50.1971) 0.158 (0.2331) -0.6102 (2.2197)	3.418 0.0002 0.303  xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639) -0.4027 (0.2967) -0.1524 (0.6197) 0.0011 (0.0029) 0.0014 (0.0269)	0 0.51  xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172) 0.0677* (0.0274) -0.0238 (0.0327) 0.0488 (0.0682) 0.0001 (0.0003) -0.0033 (0.003)	0 0.5963  xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232) -0.0197 (0.0278) 0.0375 (0.0581) 0.0001 (0.0003) -0.0018 (0.0003)	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056) 0.0121 (0.0135) 0.0431* (0.0207) -0.0017 (0.0248) -0.0012 (0.0521) 0.0002 (0.0002) -0.0009 (0.0023)	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786) 0.0589 (0.0939) 0.3677. (0.197) 0.0002 (0.0009) 0.001	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671] -85.719** (21.0158] -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156 (9.7037) -49.0566* (15.2471] -16.1122 (18.3044) -52.344 (38.1757) -0.0722 (0.1789) 1.3111 (1.6522)
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vm1PC4 vm1PC5	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958) -20.5648 (23.8742) -31.2948 (50.1971) 0.158 (0.2331) -0.6102 (2.2197) -0.0805	3.418 0.0002 0.303  xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639) -0.4027 (0.2967) -0.1524 (0.6197) 0.0011 (0.0029) 0.0014 (0.0269) -0.0589	0 0.51  xslqAA  0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172) 0.0677* (0.0274) -0.0238 (0.0327) 0.0488 (0.0682) 0.0001 (0.0003) -0.0003	0 0.5963  xslqA 0.193**** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232) -0.0197 (0.0278) 0.0375 (0.0581) 0.0001 (0.0003) -0.0018	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0156) 0.0121 (0.0135) 0.0431* (0.0207) -0.0171 (0.0248) -0.0012 (0.0521) 0.0002 (0.0002) -0.0009 (0.00023) -0.0096*	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786) 0.0589 (0.0939) 0.3677. (0.197) 0.0002 (0.0009) 0.001	0 0.725  xslqALL 17.303 (11.2882' 0.4606 (3.881) -11.4069 (10.7671' -85.719*** (21.0158' -12.0873 (17.542) -31.214 (32.6817' -3.0403 (4.2392) -8.2156 (9.7037) -49.0566* (15.2471' -16.1122 (18.3044' -52.344 (38.1757' -0.0722 (0.1789) 1.3111 (1.6522) 11.0896**
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vwm1PC4 vwm1PC5 vvm1PC1 vvm1PC5 vvm1PC1 vvm1PC5	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958) -20.5648 (23.8742) -31.2948 (50.1971) 0.158 (0.2331) -0.6102 (2.2197) -0.0805 (3.9677)	3.418 0.0002 0.303  xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639) -0.4027 (0.2967) -0.1524 (0.6197) 0.0011 (0.0029) 0.0014 (0.0269) -0.05589 (0.0499)	0 0.51  xslqAA  0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172) 0.0677* (0.0274) -0.0238 (0.0327) 0.0488 (0.0682) 0.0001 (0.0003) -0.0033 (0.003) -0.0123* (0.0031)	0 0.5963  xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232) -0.0197 (0.0278) 0.0375 (0.0581) 0.0001 (0.0003) -0.0018 (0.0025) -0.0103* (0.0042)	0 0.5614  xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056) 0.0121 (0.0135) 0.0431* (0.0207) -0.0171 (0.0248) -0.0012 (0.0521) 0.0002 (0.0002) -0.0009 (0.0023) -0.0096* (0.0037)	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786) 0.0589 (0.0939) 0.3677. (0.197) 0.0002 (0.0009) 0.001 (0.0086) -0.0035 (0.014)	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719*** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156 (9.7037) -49.0566* (15.2471 -16.1122 (18.3044 (38.1757 -0.0722 (0.1789) 1.3111 (1.6522) 11.0896**
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vvm1PC4 vvm1PC5 vvm1PC5 vvm1PC1 vvm1PC5 vvm1PC1 vvm1PC5 vvm1PC1 vvm1PC5	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958) -20.5648 (23.8742) -31.2948 (50.1971) 0.158 (0.2331) -0.6102 (2.2197) -0.0805 (3.9677) 16.1625	3.418 0.0002 0.303  xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639) -0.4027 (0.2967) -0.1524 (0.6197) 0.0011 (0.0029) 0.0014 (0.0269) -0.0589 (0.0499) 0.1147	0 0.51  xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172) 0.0677* (0.0274) -0.0238 (0.0327) 0.0488 (0.0682) 0.0001 (0.0003) -0.0033 (0.003) -0.0123*	0 0.5963  xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232) -0.0197 (0.0278) 0.0375 (0.0581) 0.0001 (0.0003) -0.0018 (0.00025) -0.0103*	0 0.5614 xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0156) 0.0121 (0.0135) 0.0431* (0.0207) -0.0171 (0.0248) -0.0012 (0.0521) 0.0002 (0.0002) -0.0009 (0.00023) -0.0096*	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786) 0.0589 (0.0939) 0.3677. (0.197) 0.0002 (0.0009) 0.001 (0.0086) -0.0035	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671 -85.719** (21.0158 -12.0873 (17.542) -31.214 (32.6817 -3.0403 (4.2392) -8.2156 (9.7037) -49.0566* (15.2471 -16.1122 (18.3044 -52.344 (38.1757 -0.0722 (0.1789) 1.3111 (1.6522) 11.0896**
Adj. Rsq anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vvm1PC4 vvm1PC5 vvm1PC1 vvm1PC5 vvm1PC1 vvm1PC5 vvm1PC1 vvm1PC5 vvm1PC1	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958) -20.5648 (23.8742) -31.2948 (50.1971) 0.158 (0.2331) -0.6102 (2.2197) -0.0805 (3.9677)	3.418 0.0002 0.303  xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639) -0.4027 (0.2967) -0.1524 (0.6197) 0.0011 (0.0029) 0.0014 (0.0269) -0.05589 (0.0499)	0 0.51  xslqAA  0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172) 0.0677* (0.0274) -0.0238 (0.0327) 0.0488 (0.0682) 0.0001 (0.0003) -0.0033 (0.003) -0.0123* (0.0051) -0.0036	0 0.5963  xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232) -0.0197 (0.0278) 0.0375 (0.0581) 0.0001 (0.0003) -0.0018 (0.0025) -0.0103* (0.0042) 0.0003	0 0.5614  xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056) 0.0121 (0.0135) 0.0431* (0.0207) -0.0171 (0.0248) -0.0012 (0.00521) 0.0002 (0.0002) -0.0009 (0.0002) -0.0009 (0.00023) -0.0096* (0.0037) 0.0038	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786) 0.0589 (0.0939) 0.3677. (0.197) 0.0002 (0.0009) 0.0001 (0.0009) 0.0011	0 0.725  xslqALL 17.303 (11.2882) 0.4606 (3.881) -11.4069 (10.7671) -85.719** (21.0158) -12.0873 (17.542) -31.214 (32.6817) -3.0403 (4.2392) -8.2156 (9.7037) -49.0566* (15.2471) -16.1122 (18.3044) -52.344 (38.1757) -0.0722 (0.1789) 1.3111 (1.6522) 11.0896** (2.7929) 9.1813 (8.3871)
Adj. Rsq  anel B, excess liquidity alpha vPC1 vPC2 vPC3 vPC4 vPC5 vm1PC1 vm1PC2 vm1PC3 vm1PC4 vm1PC5 vvm1PC4 vvm1PC5 vvm1PC1 vvm1PC5 vvm1PC1 vvm1PC2 vvm1PC1 vvm1PC2 vvm1PC3 vvm1PC4	12.84 0 0.6803 xslqAAA 113.6527*** (9.0347) 9.3319. (4.9288) -22.0347 (13.8245) -0.4144 (30.0148) -7.3099 (22.8266) -55.9739 (42.3695) 9.2152. (5.3191) -13.8536 (12.5868) -6.8977 (21.8958) -20.5648 (23.8742) -31.2948 (50.1971) 0.158 (0.2331) -0.6102 (2.2197) -0.0805 (3.9677) 16.1625 (10.8953) 39.3148	3.418 0.0002 0.303  xslqAJ 0.3828* (0.1481) -0.0308 (0.0612) -0.0215 (0.1699) 0.4244 (0.3746) -0.2611 (0.2842) 0.0404 (0.5273) -0.0497 (0.0664) 0.0573 (0.1531) 0.3309 (0.2639) -0.4027 (0.2967) -0.1524 (0.6197) 0.0011 (0.0029) 0.0014 (0.0269) -0.0589 (0.0499) 0.1147 (0.1355) 0.0093	0 0.51  xslqAA 0.1516*** (0.0196) -0.0108 (0.0068) 0.0403* (0.019) 0.0889* (0.0386) -0.0178 (0.0313) 0.0289 (0.0585) -0.0097 (0.0074) 0.0359* (0.0172) 0.0677* (0.0274) -0.0238 (0.0327) 0.0488 (0.0682) 0.0001 (0.0003) -0.0033 (0.003) -0.0123* (0.0051) -0.0036 (0.0015)	0 0.5963  xslqA 0.193*** (0.0173) -0.0074 (0.0058) 0.023 (0.0165) 0.0736* (0.0314) -0.0141 (0.0267) 0.0101 (0.0498) -0.0056 (0.0063) 0.0204 (0.0149) 0.0476* (0.0232) -0.0197 (0.0278) 0.0375 (0.0581) 0.0001 (0.0003) -0.0018 (0.0025) -0.0103* (0.0042) 0.0003 (0.0042) 0.0003 (0.0128) -0.0907	0 0.5614  xslqBBB 0.2314*** (0.0178) -0.0063 (0.0052) 0.0115 (0.0149) 0.068* (0.0279) -0.0093 (0.0238) -0.0232 (0.0449) -0.0051 (0.0056) 0.0121 (0.0135) 0.0431* (0.0207) -0.0171 (0.0248) -0.0012 (0.0521) 0.0002 (0.0002) -0.0009 (0.0023) -0.0096* (0.0037) 0.0038 (0.0114) -0.0515	0 0.8179  xslqBBBm 0.1223. (0.0651) -0.0306 (0.0197) 0.0585 (0.0563) 0.0254 (0.1051) -0.0566 (0.0899) 0.1019 (0.1696) 0.0077 (0.0213) -0.009 (0.0509) -0.0252 (0.0786) 0.0589 (0.0939) 0.3677. (0.197) 0.0002 (0.0009) 0.001 (0.00086) -0.0035 (0.014) -0.018	0 0.725  xslqALL 17.303 (11.2882 0.4606 (3.881) -11.4069 (10.7671' -85.719*** (21.0158' -12.0873 (17.542) -31.214 (32.6817' -3.0403 (4.2392) -8.2156 (9.7037) -49.0566** (15.2471' -16.1122 (18.3044' (38.1757' -0.0722 (0.1789) 1.3111 (1.6522) 11.0896** (2.7929) 9.1813 (8.3871) 95.7047**
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This Table 8 summarizes the estimates of the OLS in Eq. (15) of the form  $y_{jk}(t) = \alpha_{jk} + \sum_{i=1}^{5} \beta_{ijk} v_i(t) + \gamma_{ijk} v_i(t-1) + \delta_{ijk} \left[v_i(t) - v_i(t-1)\right]^2 + \psi_k S_k(t) + \varepsilon_{jk}(t)$ . The dependent variables are the risk partitions of regular liquidity (reglq, Panel A) and excess liquidity (xslq Panel B) for each of the investment grade credit rating classes AAA thru BBB- as well as the aggregation sector wide CMBX benchmark across all classes. The independent variables are the volatilities  $v_i(t)$ ,  $v_i(t-1)$ , and  $\left[v_i(t) - v_i(t-1)\right]^2$  labeled vPC#, vmlPC# and vvmlPC#, respectively. The other covariate is the observed CMBX spread for such ratings,  $S_k(t)$ . The estimates are provided for each row with the standard error of the estimate immediately below in parentheses. The F-test statistic and p-value and the Adjusted R-squared are provided in the final three rows. The columns indicate the credit rating class. The significance codes of '\*\*\*', '\*\*', and '' indicate statistical significance at the 0.001, 0.01, 0.05 and 0.1 levels, respectively.

After determining the estimates in Eq. (15) we then predict the daily spread risk decompositions using Eq. (16) combining the estimates and 2828 daily on the run observations selected with Eq. (8). We adjust the lookback of the factor volatilities with 22 trading days equal to one month from the date of the daily observations for the updated calculations. We re-express the estimation model for the daily predicted model as follows. For all trading days, u, we compute predicted values on the left hand side based on the principal component volatilities, market spreads and estimated coefficients on the right hand side as is given by

$$\hat{y}_{jk}(u) = \alpha_{jk} + \sum_{i=1}^{5} \beta_{ijk} v_i(u) + \gamma_{ijk} v_i(u - 22) + \delta_{ijk} \left[ v_i(u) - v_i(u - 22) \right]^2 + \psi_k \mathbb{S}_k(t)$$
 (16)

with the final risk composition then computed as a proportion of the total for the bond:

$$\bar{y}_{jk}(u) = \frac{\hat{y}_{jk}(u)}{\sum_{j} \hat{y}_{jk}(u)}$$
 (17)

We calculate all four risk components as the proportions of Eq. (17) for the CMBX sector across all credits in Figure 1.

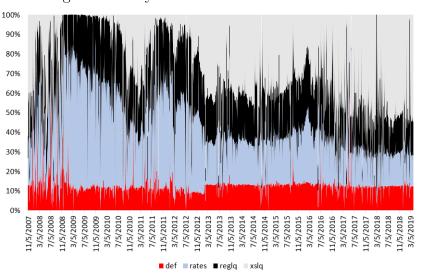


Figure 1: Daily Indexed CMBX Risk Partitions

This figure depicts the estimated risk partitions defined in Eq. (17) for all four risk components of default, interest rates, liquidity and excess liquidity on a daily basis in the plot on the left from 11/2007 thru 4/2019. These estimates are based on the monthly training set of 92 weighted observations of risk partitions for the CMBX sector overall across all credits as depicted in Fig. (9) in Christopoulos and Jarrow (2018). The x-axis capture the trading days over the sample period and the y-axis captures the proportions of risk.

The time series is a weighted average across all on-the run investment grade credit ratings classes with the weights the subordination levels as shown in Eq. (10). We see default, interest rate, liquidity availability and excess liquidity availability indices for the CMBX as introduced and defined in Christopoulos (2017). Since this paper is focused on liquidity for CMBX and REITs, as measured by effective bid-ask spreads compared with estimated reduced form liquidity measures, we extract the values for liquidity and excess liquidity depicted in Figure 1 and use them as independent variables in the evaluation of CMBX liquidity.

# 3.3 Reconciling microstructure and reduced form measures of liquidity: Validation of the Daily Model

To validate the daily estimation approach, we use the effective bid/ask spreads determined from the microstructure models discussed below as measures of CMBX liquidity from the perspective of the market and compare to the perspective revealed by the risk partitions. In this section we restrict the analysis to AAA and BBB<sup>8</sup> CMBX to correspond to the AAA and BBB corporate bond spreads used in this analysis. We incorporate that data with the daily estimated reduced form liquidity estimates from the Daily Model. We use ordinary least squares (OLS), vector autoregressive (VAR), Granger causality (Granger) and impulse response function (IRF) techniques. These analyses allow us to assess the liquidity of the CMBX sector with our approach historically and, in so doing, to validate the Daily Model approach. The explanatory factors influencing bid-ask spreads we consider are changes in US Treasuries, corporate bond spreads, the VIX volatility index and the exogenously determined reduced form liquidity indices for the CMBX sector.

#### 3.3.1 Microstructure models to generate Daily Model validation data

We implement the microstructure models applied to CMBX. In all cases, we substitute the daily mark-to-market spread,  $S_t$ , for  $P_t$  for our estimate of the bid-ask spreads of mid-market spreads as permitted by i.i.d. Thus, in all microstructure models implemented below we are computing bid/ask spreads of Spreads (as discussed in <u>Appendix Section A.1</u>) in keeping

 $<sup>^8 \</sup>rm BBB$  CMBX are often split rated based on selection for CMBX 1 thru 5 of BBB and for CMBX 6-12 BBB-. For our on the run selection, they are simply BBB.

with the way in which such fixed income spread products are traded. We adjust the price notation  $P_t$  notation in Eq. (1) to accommodate bid-ask spreads of risk premia (bid-ask spreads of Spreads),  $S_t$ .

In Model 1 (Roll), we implement Roll (1984) for end-of-day mid-market spread risk premia.

$$s_t = 2\sqrt{-\text{COV}(\Delta S_t, \Delta S_{t-1})}$$
(18)

To address positive autocovariance in the implementation we follow Harris (1990) in Eq. (2)

$$s_{t} = \begin{cases} s_{t}^{+} = -2\sqrt{\text{COV}(\Delta S_{t}, \Delta S_{t-1})} & \text{for COV}(\Delta S_{t}, \Delta S_{t-1}) > 0\\ s_{t}^{-} = 2\sqrt{-\text{COV}(\Delta S_{t}, \Delta S_{t-1})} & \text{for COV}(\Delta S_{t}, \Delta S_{t-1}) \leq 0 \end{cases}$$

$$(19)$$

which preserves the sign of autocovariance resulting in negative bid-ask spreads.

In Model 2 (Restricted Roll) we restrict Model 1, by simply dropping (or 'zeroing' in depictions, not the statistics) the observations with positive autocovariance as suggested by Harris (1990), Hasbrouck (2009) and Foucault, Pagano and Roell (2013).

In Model 3 (Absolute Roll), the Absolute Roll Measure for risk premia (aka 'Spreads') is given by

$$s_t = 2\sqrt{|-\text{COV}(\Delta S_t, \Delta S_{t-1})|}$$
(20)

following the derivations of Eq. (5) and confirming Christopoulos (2020).

In Model 4 (Thompson and Waller), we implement the model of Thompson and Waller (1987) and restate their absolute value of 5-day moving average *price* changes to 5-day moving average of changes in mid-market credit risk premia (aka 'Spreads') defined as

$$\overline{|\Delta S_t|} = \frac{1}{5} \sum_{t=1}^{5} |\Delta S_t| \tag{21}$$

with  $S_t$  the observed mid-market credit spread at time t. The bid-side spread is given by

$$B_t = S_t + \left(\frac{|\Delta S_t|}{2}\right) \tag{22}$$

and the ask-side spread<sup>9</sup> is given by

$$A_t = \max(0, S_t - (B_t - S_t)) \tag{23}$$

such that the bid-ask spread,  $s_t$ , of mid-market fixed income Spreads is given by

$$s_t = B_t - A_t \tag{24}$$

#### 3.3.2 Validation of Daily Model bid-ask spreads

Consistent with the earlier findings of Roll (1984), Harris (1990) and Hasbrouck (2009), we too find positive autocovariance to be frequently observable in our study. In our sample of 2828 observations for AAA and BBB CMBX credit tranches: 1164 (41%) of the AAA observations and 1076 (38%) of the BBB observations exhibited positive autocovariance. To give some context for the implementation of the models, we depict their implementation for the AAA CMBX in Figure 2. Figure 2a shows an example of the application of Model 1 to AAA CMBX risk premia above the risk-free rate with splits in application according to domains described in Eq. (2). The x-axis captures the range of values for the autocovariance while the y-axis captures the range of values for s. There we indeed observe negative bid-ask spreads corresponding to positive autocovariances. Model 2, drops observations that exhibit positive autocovariance in the statistical analysis as suggested in the prior literature.

Figure 2b shows an implementation of Model 2 for the same series for AAA CMBX. Dropped values are 'zeroed' for visual emphasis to the right of the origin in the graph. This implementation eliminates about 41% of the sample in the statistical analysis. Figure 2c shows the implementation of Model 3 in Eq. (5). We see a strictly positive bid-ask spread for all CMBX AAA observations, as expected. The positive autocovariance values to the right of the origin on the x-axis in Figure 2c exhibit positive bid-ask spreads on the y-axis in contrast to Figure 2a and Figure 2b. Figure 2d shows the bid-ask spreads for AAA for Thompson and Waller (1987) (Model 4) utilizing the autocovariance from the prior three

<sup>&</sup>lt;sup>9</sup>The lower boundary of zero ensures offer side spreads cannot be negative. The boundary is never reached in this study.

models as a characteristic, even though it is not included in the Model 4 structure. As is evident, the Absolute Roll Measure and the Thompson-Waller methods yield very different results at the same observation date. This is interesting.

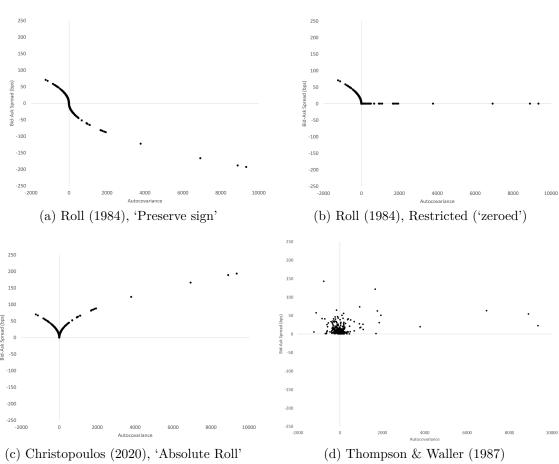


Figure 2: AAA CMBX bid-ask estimates

This figure depicts the effective bid-ask spread of risk premia (aka. bid-ask spread of 'Spreads') for on-the-run AAA CMBX tranche for 2828 daily observations of end of day mark to market values mid market spreads from 11/2007-4/2019. The x-axis for all plots show the autocovariances and the y-axis for all plots shows the effective bid-ask spread of spreads (in bps). Fig. (2a) depicts the effective bid-ask spread for Roll (1984) with the positive autocovariance preserved resulting in negative bid-ask spreads. Fig. (2b). shows the effective bid-ask spread for Roll (1984) with the restriction suggested in the prior literature of zeroing or omitting observations of positive autocovariance (we zero those observations for emphasis). Fig. (2c) shows the effective bid ask spreads using the Absolute Roll Measure of Christopoulos (2020) depicting strictly non-negative effective bid-ask spreads. Fig. (2d) shows the effective bid-ask spread using the technique of Thompson and Waller (1987). These daily values are used as the dependent variables in the OLS and VAR models described in Eq. (25) and Eq. (26), respectively.

<u>Figure 3</u> shows the time series of on-the-run AAA and BBB bid-ask spreads for Model 3 and Model 4 over the sample period. <u>Figure 3a</u> depicts the modelled bid-ask estimates for AAA while <u>Figure 3b</u> exhibits the estimates for BBB.As expected, the AAA bid-ask spreads are categorically narrower than the BBB bid-ask spreads. This is due to the fact that virtually all non-agency CMBS are structured in senior subordinate sequential pay capital structures.

As such, losses from defaults are deducted from the bottom of the capital structure with the lowest credit rated tranches being impacted first (Unrated,...,BBB,...,AAA). Since BBB securities will be impacted by losses from defaults before AAA, credit speculators betting against the sector using CMBX will opt to 'buy protection' by paying a fixed premium and receiving floating. As credit spreads widen, the short position will increase in value on a mark-to-market basis. Thus, even if defaults don't materialize, investor expectations of defaults will cause the short leg of lower rated tranches to increase in value more rapidly than higher rated tranches when credit spreads widen.<sup>10</sup>

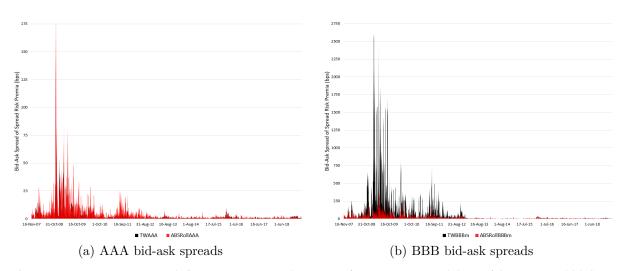


Figure 3: CMBX bid-ask spreads

This figure depicts the daily time series of effective bid-ask spread of risk premia (aka. bid-ask spread of 'Spreads') for on-the-run AAA CMBX tranche for 2828 daily observations of end of day mark to market values mid market spreads from 11/2007-4/2019. The on-the-run AAA CMBX and BBB/BBB- effective bid-ask spreads are depicted using the on-the-run selection method and modeled using the Absolute Roll Measure of Christopoulos (2020) and Thompson and Waller (1987) methods. The x-axis for all plots show the date and the y-axis for all plots shows the effective bid-ask spread of spreads (in bps). Fig. (3a) depicts AAA bid-ask spreads while Fig. (3b) depicts BBB/BBB- bid-ask spreads

#### 3.3.3 Statistical summary of the Daily Model

We construct a number of new measures in this paper which are summarized in <u>Table 9</u>. To address the regime shifts in data surrounding the halting of CMBX series issuance from 5/2008 - 1/2013, we provide statistical summary the daily public data and the Daily Model output in <u>Table 9</u> in three panels. Panel A (11/1/2007-4/17/2019) captures the entire sample. Panel B captures the beginning of the sample to the end of the temporary halt in CMBX issuance (11/1/2007-1/24/2013). Panel C captures the period 2/4/2013-4/17/2019. We use this daily data of observed values and on-the-run values in our first testing of microstructure

<sup>&</sup>lt;sup>10</sup>See An, Deng, Nichols and Sanders (2015), Riddiough and Zhu (2016), Christopoulos (2017) and ?, among others.

and risk partition liquidity measures. As expected, BBB spreads are larger (wider) than AAA spreads which are smaller (tighter). This is due to additional risk premia required by investors in subordinate BBB securities who are more exposed to loss than senior AAA counterparts.

Table 9: Daily Data, Bid-Ask, Risk Partition Models

VIX		11 <i>j</i> 25 a c	a, Bia	11011, 1		. UIUIOII IVIV		
10yr Tsy	Panel A: 11/16/07-4/2/19	mean	median	min	max	variance	stdev	n
Zyr Tsy         1.02         0.75         0.16         3.33         0.62         0.78         22           Corp Baa         284.43         274.00         156.00         616.00         6335.29         79.59         28           Corp Baa         171.01         174.00         84.00         300.00         1211.61         28           Cordix Slope (Baa-Aaa)         113.42         100.00         53.00         350.00         2755.99         52.50         28           CMBX Baa         2172.00         561.42         290.95         6924.08         438624.78         2097.29         28           CMBX CrdSlope         2013.62         488.34         214.28         6314.59         4047916.97         2011.94         28           Bid/Ask TWBaa         88.63         6.48         0.00         3161.76         63301.09         251.60         28           Bid/Ask ABSRollBaa         22.93         8.44         0.05         507.96         1504.61         38.79         22           Bid/Ask ABSRollAaa         5.20         1.70         0.03         193.37         116.00         10.77         20         10.10         10.77         20         10.10         10.77         20         10.10	VIX	19.74	17.00	9.14	80.86	91.15	9.55	2822
Tay Slope (10s-2s)	10yr Tsy	2.64	2.56	1.37	4.30	0.46	0.68	2822
Corp Baa	2yr Tsy	1.02	0.75	0.16	3.33	0.62	0.78	2822
Corp Aaa	Tsy Slope (10s-2s)	161.90	163.00	11.00	291.00	5278.17	72.65	2822
Credit Slope (Baa-Aaa)	Corp Baa	284.43	274.00	156.00	616.00	6335.29	79.59	2822
CMBX Baa         2172 00         561.42         299.95         6924.08         4398624.78         2097.29           CMBX CrdSlope         2013.62         458.34         214.28         6314.59         4047916.97         2011.94         28           Bid/Ask TWBaa         88.63         6.48         0.00         3161.76         63301.09         251.60         28           Bid/Ask ABSRollBaa         2.293         8.44         0.05         507.96         1504.61         38.79         28           Bid/Ask ABSRollBaa         2.56         0.87         0.00         142.83         44.27         6.65         28           Bid/Ask ABSRollAa         5.20         1.70         0.03         193.37         116.00         10.77         22           CJdef_pct         0.13         0.13         0.00         0.87         0.03         0.17         22           CJreglq_pct         0.26         0.25         0.00         0.97         0.01         0.11         28           CJreglq_pct         0.26         0.25         0.00         0.97         0.01         0.11         28           CJreglq_pct         0.26         0.25         0.00         0.97         0.01         0.11	Corp Aaa	171.01	174.00	84.00	300.00	1211.61	34.81	2822
CMBX CrdSlope         2013.62         458.34         214.28         6314.59         4047916.97         2011.94         22 Bid/Ask TWBaa         88.63         6.48         0.00         3161.76         63301.09         251.60         28 Bid/Ask ABSRollBaa         22.93         8.44         0.05         507.96         1504.61         38.79         28 Bid/Ask ABSRollAaa         22.93         8.44         0.05         507.96         1504.61         38.79         28 Bid/Ask ABSRollAaa         5.20         1.70         0.03         193.37         116.00         10.77         28 Bid/Ask ABSRollAaa         5.20         1.70         0.03         193.37         116.00         10.77         26 CJdef_pct         0.13         0.13         0.00         0.87         0.00         0.07         26 CJreglq_pct         0.26         0.25         0.00         0.97         0.01         0.11         22 CJrates_pct         0.26         0.25         0.00         0.97         0.01         0.11         22 CJrates_pct         0.30         0.33         0.00         0.96         0.04         0.21         28           VIX         25.52         22.44         12.43         80.86         118.41         10.88         12           10yr Tsy         2.96	Credit Slope (Baa-Aaa)	113.42	100.00	53.00	350.00	2755.99	52.50	2822
CMBX CrdSlope	CMBX Baa	2172.00	561.42	290.95	6924.08	4398624.78	2097.29	2822
Bid/Ask ABSRollBaa   22.93   8.44   0.05   507.96   1504.61   38.79   28   28   38.44   0.05   507.96   1504.61   38.79   28   38   38.44   0.05   507.96   1504.61   38.79   28   38   38.44   0.05   507.96   1504.61   38.79   28   38   38.79   28   38   38.79   28   38.79   28   38.79   28   38.79   28   38.79   28   38.79   28   38.79   28   38.79   28   38.79   28   38.79   28   38.79   28   38.79   28   38.79   38.79   28   38.79	CMBX Aaa	158.38	106.95	44.45	847.50	17164.78	131.01	2822
Bid/Ask ABSRollBaa   22.93   8.44   0.05   507.96   1504.61   38.79   28.85   Bid/Ask TWADA	CMBX CrdSlope	2013.62	458.34	214.28	6314.59	4047916.97	2011.94	2822
Bid/Ask ABSRollAaa         2.56         0.87         0.00         142.83         44.27         6.65         7         28           Bid/Ask ABSRollAaa         5.20         1.70         0.03         193.37         116.00         10.77         28           CJrates_pct         0.32         0.26         0.00         0.87         0.03         0.17         28           CJreglq_pct         0.30         0.33         0.00         0.97         0.01         0.11         28           CJxslq_pct         0.30         0.33         0.00         0.96         0.04         0.21         28           VIX         25.52         22.44         12.43         80.86         118.41         10.88         12           10yr Tsy         2.96         3.17         1.43         4.30         0.63         0.75         1.6         3.33         0.56         0.75         12           Tsy Slope (10s-2s)         203.63         198.00         82.00         291.00         2819.02         53.09         12           Corp Baa         383.02.8         360.60         226.00         616.00         7698.42         87.74         12         12         12         12         12 <t< td=""><td>Bid/Ask TWBaa</td><td>88.63</td><td>6.48</td><td></td><td>3161.76</td><td>63301.09</td><td>251.60</td><td>2822</td></t<>	Bid/Ask TWBaa	88.63	6.48		3161.76	63301.09	251.60	2822
Bid/Ask ABSRollAaa   5.20	Bid/Ask ABSRollBaa	22.93	8.44	0.05	507.96	1504.61	38.79	2822
CJdef_pct         0.13         0.13         0.00         0.87         0.00         0.07         28           CJreglq_pct         0.26         0.26         0.00         0.87         0.03         0.17         28           CJreglq_pct         0.26         0.25         0.00         0.97         0.01         0.11         28           CJxslq_pct         0.30         0.33         0.00         0.96         0.04         0.21         28           VIX         2.96         3.17         1.43         80.86         118.41         10.88         12           10yr Tsy         2.96         3.17         1.43         4.30         0.63         0.79         12           2yr Tsy         0.92         0.75         0.16         3.33         0.56         0.75         12           Tsy Slope (10s-2s)         203.63         198.00         82.00         291.00         2819.02         53.09         12           Corp Baa         330.28         306.00         226.00         616.00         7698.42         87.74         12           Cedit Slope (Ba-Aaa)         142.16         125.00         74.00         350.00         391.08         62.59         12	Bid/Ask TWAaa	2.56	0.87	0.00	142.83	44.27	6.65	2822
CJrates_pct         0.32         0.26         0.00         0.87         0.03         0.17         28           CJrsglq_pct         0.26         0.25         0.00         0.97         0.01         0.11         28           CJxslq_pct         0.30         0.33         0.00         0.96         0.04         0.21         28           VIX         2.5.52         22.44         12.43         80.86         118.41         10.88         12           VIX         2.5.52         22.44         12.43         80.86         118.41         10.88         12           10 yr Tsy         2.96         3.17         1.43         4.30         0.63         0.79         12           2yr Tsy         0.92         0.75         0.16         3.33         0.56         0.75         12           Corp Baa         330.28         306.00         226.00         616.00         7698.42         87.74         12           Corp Aaa         188.12         181.00         313.00         300.00         884.08         29.73         12           Credit Slope (Baa-Aaa)         142.16         125.00         74.00         350.00         3917.08         62.59	Bid/Ask ABSRollAaa	5.20	1.70	0.03	193.37	116.00	10.77	2822
CJreglq_pct         0.26         0.25         0.00         0.97         0.01         0.11         28           CJxslq_pct         0.30         0.33         0.00         0.96         0.04         0.21         28           Panel B: 11/16/07-1/24/13         mean         median         min         max         variance         stdev         3           VIX         25.52         22.44         12.43         80.86         118.41         10.88         12           10yr Tsy         2.96         3.17         1.43         4.30         0.63         0.79         12           2yr Tsy         0.92         0.75         0.16         3.33         0.56         0.75         12           Corp Baa         330.28         336.00         226.00         616.00         7698.42         87.74         12           Corp Baa         188.12         181.00         131.00         300.00         884.08         29.73         12           Credit Slope (Baa-Aaa)         142.16         125.00         74.00         350.00         3917.08         62.59         12           CMBX Baa         4226.50         4344.64         982.75         6894.08         1761615.77         1327.26         <		0.13	0.13	0.00	0.87	0.00	0.07	2822
CJxslq_pct	CJrates_pct	0.32	0.26	0.00	0.87	0.03	0.17	2822
Panel B: 11/16/07-1/24/13   mean   median   min   max   variance   stdev   min		0.26	0.25	0.00	0.97	0.01	0.11	2822
VIX	$CJxslq\_pct$	0.30	0.33	0.00	0.96	0.04	0.21	2822
10yr Tsy	Panel B: 11/16/07-1/24/13	mean	median	min	max	variance	stdev	n
10yr Tsy		05 50	22.44	10.40	90.90	110 41	10.00	
2yr Tsy         0.92         0.75         0.16         3.33         0.56         0.75         12           Tsy Slope (10s-2s)         203.63         198.00         82.00         291.00         2819.02         53.09         12           Corp Baa         330.28         306.00         226.00         616.00         7698.42         87.74         12           Corp Aaa         188.12         181.00         131.00         300.00         884.08         29.73         12           Credit Slope (Baa-Aaa)         142.16         125.00         74.00         350.00         3917.08         62.59         12           CMBX Baa         4226.50         4344.64         982.75         6924.08         1761615.77         1327.26         12           CMBX CrdSlope         3983.51         4121.04         924.88         6314.59         1628953.33         1276.30         12           Bid/Ask ABSRollBaa         48.67         70.15         0.00         3161.76         119352.96         345.47         12           Bid/Ask TWBaa         18.67         70.15         0.00         3161.76         119352.96         345.47         12           Bid/Ask TWBaa         4.69         1.99         0.00         1								1296
Tsy Slope (10s-2s)								1296
Corp Baa         330.28         306.00         226.00         616.00         7698.42         87.74         12           Corp Aaa         188.12         181.00         131.00         300.00         884.08         29.73         12           Credit Slope (Baa-Aaa)         142.16         125.00         74.00         350.00         3917.08         62.59         12           CMBX Baa         4226.50         4344.64         982.75         6924.08         1761615.77         1327.26         12           CMBX CrdSlope         3983.51         4121.04         924.88         6314.59         1628953.33         1276.30         12           Bid/Ask TWBaa         188.67         70.15         0.00         3161.76         119352.96         345.47         12           Bid/Ask ABSRollBaa         43.63         27.93         0.74         507.96         2462.15         49.62         12           Bid/Ask ABSRollAaa         9.94         5.41         0.07         193.37         209.99         14.49         12           CJdef_pct         0.13         0.12         0.00         0.87         0.01         0.09         12           CJrestes_pct         0.43         0.45         0.00         0.97								1296
Corp Aaa         188.12         181.00         131.00         300.00         884.08         29.73         12           Credit Slope (Baa-Aaa)         142.16         125.00         74.00         350.00         3917.08         62.59         12           CMBX Baa         4226.50         4344.64         982.75         6924.08         1761615.77         1327.26         12           CMBX CrdSlope         3983.51         4121.04         924.88         6314.59         1628953.33         1276.30         12           Bid/Ask TWBaa         188.67         70.15         0.00         3161.76         119352.96         345.47         12           Bid/Ask ABSRollBaa         43.63         27.93         0.74         507.96         2462.15         49.62         12           Bid/Ask ABSRollAaa         9.94         5.41         0.07         193.37         209.99         14.49         12           CJdef_pct         0.13         0.12         0.00         0.87         0.01         0.09         12           CJreglq_pct         0.43         0.45         0.00         0.87         0.01         0.11         12           CJxslq_pct         0.16         0.09         0.00         0.95 <t< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td>1296</td></t<>								1296
Credit Slope (Baa-Aaa)         142.16         125.00         74.00         350.00         3917.08         62.59         12           CMBX Baa         4226.50         4344.64         982.75         6924.08         176161.77         1327.26         12           CMBX Aaa         242.99         191.73         57.63         847.50         23591.11         153.59         12           CMBX CrdSlope         3983.51         4121.04         924.88         6314.59         1628953.33         1276.30         12           Bid/Ask TWBaa         188.67         70.15         0.00         3161.76         119352.96         345.47         12           Bid/Ask ABSRollBaa         43.63         27.93         0.74         507.96         2462.15         49.62         12           Bid/Ask ABSRollAaa         4.69         1.99         0.00         142.83         87.38         9.35         12           Bid/Ask ABSRollAaa         9.94         5.41         0.07         193.37         209.99         14.49         12           CJdef_pct         0.13         0.12         0.00         0.87         0.01         0.09         12           CJrates_pct         0.43         0.45         0.00         0.87 <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td>1296</td>								1296
CMBX Baa         4226.50         4344.64         982.75         6924.08         1761615.77         1327.26         12           CMBX Aaa         242.99         191.73         57.63         847.50         23591.11         153.59         12           CMBX CrdSlope         3983.51         4121.04         924.88         6314.59         1628953.33         1276.30         12           Bid/Ask TWBaa         188.67         70.15         0.00         3161.76         119352.96         345.47         12           Bid/Ask ABSRollBaa         43.63         27.93         0.74         507.96         2462.15         49.62         12           Bid/Ask ABSRollBaa         4.69         1.99         0.00         142.83         87.38         9.35         12           CJdef_pct         0.13         0.12         0.00         0.87         0.01         0.09         12           CJretsel_pct         0.43         0.45         0.00         0.87         0.01         0.09         12           CJretgl_pct         0.28         0.29         0.00         0.97         0.01         0.11         12           CJsslq_pct         0.16         0.09         0.00         0.97         0.03         <								1296
CMBX Aaa         242.99         191.73         57.63         847.50         23591.11         153.59         12           CMBX CrdSlope         3983.51         4121.04         924.88         6314.59         1628953.33         1276.30         12           Bid/Ask TWBaa         188.67         70.15         0.00         3161.76         119352.96         345.47         12           Bid/Ask ABSRollBaa         43.63         27.93         0.74         507.96         2462.15         49.62         12           Bid/Ask TWAaa         4.69         1.99         0.00         142.83         87.38         9.35         12           Bid/Ask ABSRollAaa         9.94         5.41         0.07         193.37         209.99         14.49         12           CJdef_pct         0.13         0.12         0.00         0.87         0.01         0.09         12           CJreglq_pct         0.28         0.29         0.00         0.97         0.01         0.11         12           CJsslq_pct         0.16         0.09         0.00         0.95         0.03         0.18         12           Panel C: 2/6/13-4/2/19         mean         median         min         max         variance								1296
CMBX CrdSlope         3983.51         4121.04         924.88         6314.59         1628953.33         1276.30         12           Bid/Ask TWBaa         188.67         70.15         0.00         3161.76         119352.96         345.47         12           Bid/Ask ABSRollBaa         43.63         27.93         0.74         507.96         2462.15         49.62         12           Bid/Ask ABSRollAaa         4.69         1.99         0.00         142.83         87.38         9.35         12           Bid/Ask ABSRollAaa         9.94         5.41         0.07         193.37         209.99         14.49         12           CJdef_pct         0.13         0.12         0.00         0.87         0.03         0.16         12           CJreglq_pct         0.28         0.29         0.00         0.97         0.01         0.01         11         12           CJxslq_pct         0.16         0.09         0.00         0.95         0.03         0.18         12           Panel C: 2/6/13-4/2/19         mean         median         min         max         variance         stdev         3           VIX         14.84         13.81         9.14         40.74         15.68								1296
Bid/Ask TWBaa         188.67         70.15         0.00         3161.76         119352.96         345.47         12           Bid/Ask ABSRollBaa         43.63         27.93         0.74         507.96         2462.15         49.62         12           Bid/Ask ABSRollAaa         4.69         1.99         0.00         142.83         87.38         9.35         12           Bid/Ask ABSRollAaa         9.94         5.41         0.07         193.37         209.99         14.49         12           CJdef_pct         0.13         0.12         0.00         0.87         0.01         0.09         12           CJrates_pct         0.43         0.45         0.00         0.87         0.03         0.16         12           CJreglq_pct         0.28         0.29         0.00         0.97         0.01         0.11         12           CJxslq_pct         0.16         0.09         0.00         0.95         0.03         0.18         12           VIX         14.84         13.81         9.14         40.74         15.68         3.96         15           10yr Tsy         2.37         2.37         1.37         3.24         0.17         0.41         15								1296
Bid/Ask ABSRollBaa         43.63         27.93         0.74         507.96         2462.15         49.62         12           Bid/Ask TWAaa         4.69         1.99         0.00         142.83         87.38         9.35         12           Bid/Ask ABSRollAaa         9.94         5.41         0.07         193.37         209.99         14.49         12           CJdef_pct         0.13         0.12         0.00         0.87         0.01         0.09         12           CJreglq_pct         0.43         0.45         0.00         0.87         0.03         0.16         12           CJsslq_pct         0.28         0.29         0.00         0.97         0.01         0.11         12           CJsslq_pct         0.16         0.09         0.00         0.95         0.03         0.18         12           Panel C: 2/6/13-4/2/19         mean         median         min         max         variance         stdev         1           VIX         14.84         13.81         9.14         40.74         15.68         3.96         15           10yr Tsy         2.37         2.37         1.37         3.24         0.17         0.41         18								1296 $1296$
Bid/Ask TWAaa         4.69         1.99         0.00         142.83         87.38         9.35         12           Bid/Ask ABSRollAaa         9.94         5.41         0.07         193.37         209.99         14.49         12           CJdef_pct         0.13         0.12         0.00         0.87         0.01         0.09         12           CJrates_pct         0.43         0.45         0.00         0.87         0.03         0.16         12           CJreglq_pct         0.28         0.29         0.00         0.97         0.01         0.11         12           CJxslq_pct         0.16         0.09         0.00         0.95         0.03         0.18         12           VIX         14.84         13.81         9.14         40.74         15.68         3.96         15           10yr Tsy         2.37         2.37         1.37         3.24         0.17         0.41         15           2yr Tsy         1.10         0.75         0.20         2.98         0.64         0.80         15           Tsy Slope (10s-2s)         126.45         123.00         11.00         266.00         4632.19         68.06         15								1296
Bid/Ask ABSRollAaa         9.94         5.41         0.07         193.37         209.99         14.49         12           CJdef_pct         0.13         0.12         0.00         0.87         0.01         0.09         12           CJrates_pct         0.43         0.45         0.00         0.87         0.03         0.16         12           CJreglq_pct         0.28         0.29         0.00         0.97         0.01         0.11         12           CJxslq_pct         0.16         0.09         0.00         0.95         0.03         0.18         12           Panel C: 2/6/13-4/2/19         mean         median         min         max         variance         stdev         3           VIX         14.84         13.81         9.14         40.74         15.68         3.96         15           10yr Tsy         2.37         2.37         1.37         3.24         0.17         0.41         15           2yr Tsy         1.10         0.75         0.20         2.98         0.64         0.80         15           Tsy Slope (10s-2s)         126.45         123.00         11.00         266.00         4632.19         68.06         15								1296
CJdef_pct         0.13         0.12         0.00         0.87         0.01         0.09         12           CJrates_pct         0.43         0.45         0.00         0.87         0.03         0.16         12           CJreglq_pct         0.28         0.29         0.00         0.97         0.01         0.11         12           CJxslq_pct         0.16         0.09         0.00         0.95         0.03         0.18         12           Panel C: 2/6/13-4/2/19         mean         median         min         max         variance         stdev         1           VIX         14.84         13.81         9.14         40.74         15.68         3.96         15           10yr Tsy         2.37         2.37         1.37         3.24         0.17         0.41         15           2yr Tsy         1.10         0.75         0.20         2.98         0.64         0.80         15           Tsy Slope (10s-2s)         126.45         123.00         11.00         266.00         4632.19         68.06         15           Corp Baa         245.50         241.50         156.00         363.00         1878.91         43.35         15								1296
CJrates_pct 0.43 0.45 0.00 0.87 0.03 0.16 12 CJreglq_pct 0.28 0.29 0.00 0.97 0.01 0.11 12 CJxslq_pct 0.16 0.09 0.00 0.95 0.03 0.18 12 Panel C: 2/6/13-4/2/19 mean median min max variance stdev								
CJreglq_pct 0.28 0.29 0.00 0.97 0.01 0.11 12 CJxslq_pct 0.16 0.09 0.00 0.95 0.03 0.18 12 Panel C: 2/6/13-4/2/19 mean median min max variance stdev 12 VIX 14.84 13.81 9.14 40.74 15.68 3.96 15 10yr Tsy 2.37 2.37 1.37 3.24 0.17 0.41 15 2yr Tsy 1.10 0.75 0.20 2.98 0.64 0.80 15 Tsy Slope (10s-2s) 126.45 123.00 11.00 266.00 4632.19 68.06 15 Corp Baa 245.50 241.50 1566.00 363.00 1878.91 43.35 15 Corp Aaa 156.49 162.00 84.00 226.00 1030.76 32.11 15 Credit Slope (Baa-Aaa) 89.01 87.00 53.00 154.00 473.71 21.76 15 CMBX Baa 427.15 420.79 290.95 817.99 7187.70 84.78 15 CMBX Aaa 86.53 87.85 44.45 171.49 468.80 21.65 15 CMBX CrdSlope 340.63 344.45 214.28 646.50 6205.90 78.78 15 Bid/Ask TWAaa 3.68 2.46 0.00 53.78 18.60 4.31 15 Bid/Ask TWAaa 0.75 0.56 0.00 6.92 0.55 0.74								$\frac{1296}{1296}$
CJxslq_pct         0.16         0.09         0.00         0.95         0.03         0.18         12           Panel C: 2/6/13-4/2/19         mean         median         min         max         variance         stdev         :           VIX         14.84         13.81         9.14         40.74         15.68         3.96         15           10yr Tsy         2.37         2.37         1.37         3.24         0.17         0.41         15           2yr Tsy         1.10         0.75         0.20         2.98         0.64         0.80         15           Tsy Slope (10s-2s)         126.45         123.00         11.00         266.00         4632.19         68.06         15           Corp Baa         245.50         241.50         156.00         363.00         1878.91         43.35         15           Corp Aaa         156.49         162.00         84.00         226.00         1030.76         32.11         15           Credit Slope (Baa-Aaa)         89.01         87.00         53.00         154.00         473.71         21.76         15           CMBX Baa         427.15         420.79         290.95         817.99         7187.70         84.78								
Panel C: 2/6/13-4/2/19 mean median min max variance stdev :  VIX 14.84 13.81 9.14 40.74 15.68 3.96 15 10yr Tsy 2.37 2.37 1.37 3.24 0.17 0.41 15 2yr Tsy 1.10 0.75 0.20 2.98 0.64 0.80 15 Tsy Slope (10s-2s) 126.45 123.00 11.00 266.00 4632.19 68.06 15 Corp Baa 245.50 241.50 156.00 363.00 1878.91 43.35 15 Corp Aaa 156.49 162.00 84.00 226.00 1030.76 32.11 15 Credit Slope (Baa-Aaa) 89.01 87.00 53.00 154.00 473.71 21.76 15 CMBX Baa 427.15 420.79 290.95 817.99 7187.70 84.78 15 CMBX Aaa 86.53 87.85 44.45 171.49 468.80 21.65 15 CMBX CrdSlope 340.63 344.45 214.28 646.50 6205.90 78.78 15 Bid/Ask TWBaa 3.68 2.46 0.00 53.78 18.60 4.31 15 Bid/Ask TWBaa 5.35 4.23 0.05 39.50 18.93 4.35 15 Bid/Ask TWAaa 0.75 0.56 0.00 6.92 0.55 0.74								$\frac{1296}{1296}$
VIX 14.84 13.81 9.14 40.74 15.68 3.96 15 10yr Tsy 2.37 2.37 1.37 3.24 0.17 0.41 15 2yr Tsy 1.10 0.75 0.20 2.98 0.64 0.80 15 Tsy Slope (10s-2s) 126.45 123.00 11.00 266.00 4632.19 68.06 15 Corp Baa 245.50 241.50 156.00 363.00 1878.91 43.35 15 Corp Aaa 156.49 162.00 84.00 226.00 1030.76 32.11 15 Credit Slope (Baa-Aaa) 89.01 87.00 53.00 154.00 473.71 21.76 15 CMBX Baa 427.15 420.79 290.95 817.99 7187.70 84.78 15 CMBX Aaa 86.53 87.85 44.45 171.49 468.80 21.65 15 CMBX CrdSlope 340.63 344.45 214.28 646.50 6205.90 78.78 15 Bid/Ask TWBaa 3.68 2.46 0.00 53.78 18.60 4.31 15 Bid/Ask ABSRollBaa 5.35 4.23 0.05 39.50 18.93 4.35 18 Bid/Ask TWAaa 0.75 0.56 0.00 6.92 0.55 0.74								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Panel C: 2/6/13-4/2/19	mean	median	min	max	variance	stdev	n
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$								1526
Tsy Slope (10s-2s)         126.45         123.00         11.00         266.00         4632.19         68.06         15           Corp Baa         245.50         241.50         156.00         363.00         1878.91         43.35         15           Corp Aaa         156.49         162.00         84.00         226.00         1030.76         32.11         15           Credit Slope (Baa-Aaa)         89.01         87.00         53.00         154.00         473.71         21.76         15           CMBX Baa         427.15         420.79         290.95         817.99         7187.70         84.78         15           CMBX CrdSlope         340.63         344.45         214.28         646.50         6205.90         78.78         15           Bid/Ask TWBaa         3.68         2.46         0.00         53.78         18.60         4.31         15           Bid/Ask ABSRollBaa         5.35         4.23         0.05         39.50         18.93         4.35         15           Bid/Ask TWAaa         0.75         0.56         0.00         6.92         0.55         0.74         15								1526
Corp Baa         245.50         241.50         156.00         363.00         1878.91         43.35         15           Corp Aaa         156.49         162.00         84.00         226.00         1030.76         32.11         15           Credit Slope (Baa-Aaa)         89.01         87.00         53.00         154.00         473.71         21.76         15           CMBX Baa         427.15         420.79         290.95         817.99         7187.70         84.78         15           CMBX Aaa         86.53         87.85         44.45         171.49         468.80         21.65         15           CMBX CrdSlope         340.63         344.45         214.28         646.50         6205.90         78.78         15           Bid/Ask TWBaa         3.68         2.46         0.00         53.78         18.60         4.31         15           Bid/Ask ABSRollBaa         5.35         4.23         0.05         39.50         18.93         4.35         15           Bid/Ask TWAaa         0.75         0.56         0.00         6.92         0.55         0.74         15								1526
Corp Aaa         156.49         162.00         84.00         226.00         1030.76         32.11         15           Credit Slope (Baa-Aaa)         89.01         87.00         53.00         154.00         473.71         21.76         15           CMBX Baa         427.15         420.79         290.95         817.99         7187.70         84.78         15           CMBX Aaa         86.53         87.85         44.45         171.49         468.80         21.65         15           CMBX CrdSlope         340.63         344.45         214.28         646.50         6205.90         78.78         15           Bid/Ask TWBaa         3.68         2.46         0.00         53.78         18.60         4.31         15           Bid/Ask ABSRollBaa         5.35         4.23         0.05         39.50         18.93         4.35         15           Bid/Ask TWAaa         0.75         0.56         0.00         6.92         0.55         0.74         15								1526
Credit Slope (Baa-Aaa)         89.01         87.00         53.00         154.00         473.71         21.76         15           CMBX Baa         427.15         420.79         290.95         817.99         7187.70         84.78         15           CMBX Aaa         86.53         87.85         44.45         171.49         468.80         21.65         15           CMBX CrdSlope         340.63         344.45         214.28         646.50         6205.90         78.78         15           Bid/Ask TWBaa         3.68         2.46         0.00         53.78         18.60         4.31         15           Bid/Ask ABSRollBaa         5.35         4.23         0.05         39.50         18.93         4.35         15           Bid/Ask TWAaa         0.75         0.56         0.00         6.92         0.55         0.74         15								1526
CMBX Baa         427.15         420.79         290.95         817.99         7187.70         84.78         15           CMBX Aaa         86.53         87.85         44.45         171.49         468.80         21.65         15           CMBX CrdSlope         340.63         344.45         214.28         646.50         6205.90         78.78         15           Bid/Ask TWBaa         3.68         2.46         0.00         53.78         18.60         4.31         15           Bid/Ask ABSRollBaa         5.35         4.23         0.05         39.50         18.93         4.35         15           Bid/Ask TWAaa         0.75         0.56         0.00         6.92         0.55         0.74         15	•							1526
CMBX Aaa         86.53         87.85         44.45         171.49         468.80         21.65         15           CMBX CrdSlope         340.63         344.45         214.28         646.50         6205.90         78.78         15           Bid/Ask TWBaa         3.68         2.46         0.00         53.78         18.60         4.31         15           Bid/Ask ABSRollBaa         5.35         4.23         0.05         39.50         18.93         4.35         15           Bid/Ask TWAaa         0.75         0.56         0.00         6.92         0.55         0.74         15								1526
CMBX CrdSlope         340.63         344.45         214.28         646.50         6205.90         78.78         15           Bid/Ask TWBaa         3.68         2.46         0.00         53.78         18.60         4.31         15           Bid/Ask ABSRollBaa         5.35         4.23         0.05         39.50         18.93         4.35         18           Bid/Ask TWAaa         0.75         0.56         0.00         6.92         0.55         0.74         15								1526
Bid/Ask TWBaa     3.68     2.46     0.00     53.78     18.60     4.31     15       Bid/Ask ABSRollBaa     5.35     4.23     0.05     39.50     18.93     4.35     15       Bid/Ask TWAaa     0.75     0.56     0.00     6.92     0.55     0.74     15								1526
Bid/Ask ABSRollBaa     5.35     4.23     0.05     39.50     18.93     4.35     15       Bid/Ask TWAaa     0.75     0.56     0.00     6.92     0.55     0.74     15								1526
Bid/Ask TWAaa 0.75 0.56 0.00 6.92 0.55 0.74 15								1526
								1526
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								1526
								1526
								1526
	$CJreglq\_pct$						0.10	1526
CJxslq_pct 0.42 0.41 0.00 0.96 0.02 0.14 15	$CJxslq\_pct$	0.42	0.41	0.00	0.96	0.02	0.14	1526

This table summarizes the daily data used in the paper. Panel A summarizes for the entire sample period 11/2007-4/2019. Panel B summarizes from 11/2007-1/2013. Panel C summarizes from 2/2013-4/2019. The split account for the temporary halt for 5 years of CMBX issuance from 2008 to 2013. The VIX is the CBOE volatility index. Next, 10 year and 2 year Treasury yields are captured as well as their difference in the Treasury Slope (10s-2s). Then the Corporate Bond Spreads (in bps) of Baa and AAA ratings are captured along with their difference, the Corporate Bond Credit Slope (Baa-Aaa). Then aggregations for on the CMBX Spreads (in bps) based on the selection criteria in Eq. (8) are captured for Aaa and Baa credits as well as their differences the CMBX Credit Slope (Baa-Aaa). These are followed by the effective bid-ask spreads of Spreads (in bps) for Baa CMBX using Model 4 Thompson Waller (Bid/Ask TWBaa) and then Model 3 Absolute Roll (Bid/Ask ABRSRollBaa), with the corresponding values for Aaa CMBX immediately following them. Finally, the estimated proportions of risk partitions using the Daily Model for the on-the-run CMBX sector index weighted across all CMBX credit ratings in Eq. (10) is provided for default (CJdef\_pct), interest rates (CJrates\_pct), liquidity (CJreglq\_pct), and excess liquidity (CJxslq\_pct). The columns to the right of the label report mean, median, min, max, variance, standard deviation (stdev) and the number of observations.

Additionally, there may also be embedded partitions of the risk premia associated with risks other than default for all CMBX including rate risk, liquidity availability and excess liquidity availability as discussed previously. The absolute value of the ratio of the mean to the standard deviation also suggests that AAA securities (1.21) are less volatile than BBB securities (0.96) after normalizing for the mean.

#### 3.3.4 Time series OLS for the Daily Model

For 
$$g \in \begin{cases} 1 &= \text{Roll (1984)} \\ 2 &= \text{Restricted Roll} \\ 3 &= \text{Absolute Roll} \end{cases}$$
 microstructure models and  $k \in \begin{cases} 1 &= \text{Aaa} \\ 2 &= \text{Baa} \end{cases}$  rating, let  $s_{gkt}$ , represent

the corresponding bid-ask spread determined at time t. We examine the statistical relationship between the dependent variables of bid-ask spreads,  $s_{gkt}$ , for CMBX, key benchmark market indicators, and liquidity and excess liquidity risk partitions using OLS. We verify the stationarity of all variables using the Dickey-Fuller unit root test and both the liquidity and the excess liquidity indices were found to be stationary. For the remaining independent variables, we took first differences and also confirmed their stationarity with Dickey-Fuller. We consider all models over 2828 daily observations in the sample period 1/2007-4/2019. We regress model bid-ask spreads against changes in the VIX volatility index (VIX), the Treasury Slope (10 year US Treasury yield to maturity - 2 year US Treasury yield to maturity, 'TsySlp'), the corporate credit slope (BBB-AAA, 'CrdSlp'), and nominal proportions of the liquidity availability (LQ) and excess liquidity availability (XSLQ) indices for the CMBX sector.

The estimates of the ordinary least squares (OLS) regression are determined with

$$s_{gkt} = \alpha + \beta_1 \Delta VIX_t + \beta_2 \Delta TsySlp_t + \beta_3 \Delta CrdSlp_t + \beta_4 LQ_t + \beta_5 XSLQ_t + \epsilon_t$$
 (25)

The results of the regressions are summarized in <u>Table 10</u> grouped by credit rating (AAA and BBB). Across *both* credit rating categories Model 1, with preserved autocovariance (negative bid-ask spreads) as described in Eq. (2), is statistically insignificant, while the three other

 $<sup>^{11}</sup>$ We eliminate 6 dates from 1/29/2013 thru 2/5/2013 corresponding to the 're-start' of the CMBX market with the issuance of CMBX Series 6.

	Tabl	<u>e 10: Time series O</u>	LS, AAA	
	Roll (1)	Restricted Roll (2)	ABSRoll (3)	TW (4)
Intercept	-0.36589	17.97386***	19.85028***	8.04411***
	0.95751	0.73358	0.76557	0.50276
$\operatorname{chgVIX}$	-0.1203	-0.2673**	-0.16294 .	-0.07544
_	0.11786	0.08985	0.09423	0.06188
chgTsySlp	0.09272	-0.01474	-0.11751**	-0.02223
	0.05491	0.04257	0.0439	0.02883
chgCrdSlp	-0.08124	0.19366**	0.28591***	0.08836 .
	0.09726	0.07077	0.07776	0.05107
$\operatorname{Lq}$	2.40796	-21.30327***	-24.37286***	-7.33146***
	2.55098	1.94928	2.0396	1.33945
XSLq	0.19045	-25.47087***	-28.0375***	-12.05928***
_	1.301	0.97257	1.04019	0.68312
df	2822	1658	2822	2822
F-test p-val	0.2703	0.00	0.00	0.00
$\operatorname{Adj-\hat{R}sq}$	0.0004919	0.3017	0.2114	0.1075

This table summarizes the results from the AAA OLS regression  $s_{gkt} = \alpha + \beta_1 \Delta \text{VIX}_t + \beta_2 \Delta \text{TsySlp}_t + \beta_3 \text{CrdSlp}_t + \beta_4 \text{LQ}_t + \beta_5 \text{XSLQ}_t + \epsilon_t$  as defined in Eq. (25). The dependent variable considered are the AAA effective bid-ask spreads,  $s_{gkt}$  determined using the four microstructure models of Roll (1984) with positive autocovariance preserved for observations, Roll (1984) augmented with observations of positive autocovariance eliminated, Christopoulos (2020), and Thompson and Waller (1987). The five independent variables are the change in the VIX volatility index ('chgVIX'), the change in the Treasury slope ('chgTsySlope') of 10year - 2year yields, the change in the corporate credit slope ('chgCrdSlp') of BBB-AAA risk premia, the estimated CMBX sector wide indices weighted across all ratings and tranches for liquidity ('Lq') and excess liquidity ('XSLq') as depicted in Fig. (1). The significance codes of '\*\*\*', '\*\*', '\*\*', '\*\*', '\*\*', '\*\*', '\*\*', indicate statistical significance at the 0.001, 0.01, 0.05 and 0.1 levels, respectively.

models are statistically significant as measured by the F-test.

AAA For AAA bid-ask spreads as dependent variable, wider bid-ask spreads correspond to lower volatility as measured by the VIX. This would suggest a lagging response in market pricing compared with observed volatility. This conjectured lagging relationship corresponds to intuition for the significant Models 2, 3 and 4. As bid-ask spreads widen (greater uncertainty) changes in the Treasury slope become more muted (negative) reflecting a general flight to quality. Simultaneously, the changes in the credit slope are increasing (positive), also reflecting market wide concerns over credit. Finally, the signs of both liquidity and excess liquidity indices are negative suggesting that when bid-ask spreads widen, there may be less sector-wide liquidity embedded within market prices. The Adjusted R-squared value of 0.3017 for Model 2<sup>12</sup> exhibits the best explanatory value for the bid-ask estimates, but its scope is limited. In contrast, Model 3 with its Adjusted R-squared value of 0.2114 provides consistently significant estimators for each of the covariates. Model 4 provides less insight.

<sup>&</sup>lt;sup>12</sup>Model 2 has 43% less observations than the other models due to dropped values exhibiting positive autocovariance.

Table 11: Time series OLS, BBB Roll (1) TW(4)Restricted Roll (2) ABSRoll (3) 388.1854\*\*\* Intercept 8.2623 399.7197\*\*\* 68.1094\*\*\* 7.377823.13036.998918.3606 chgVIX 0.40421.5045 -0.13840.1580.90812.82030.86152.2599chgTsySlp0.58330.38420.29170.38940.42311.2611 0.40141.0529chgCrdSlp 0.5793-0.8997 0.65-1.83482.21320.71091.865 0.7494-63.1772\*\*\* -484.008\*\*\* 2.3037 -536.5333\*\*\* Lq 61.9319 19.6558 18.6463 48.9159 -592.9525\*\*\* -86.4366\*\*\* -587.0661\*\*\* XSLq-3.86610.024430.64859.509624.94712822 df 2822 1746 2822 0..00F-test p-val 0.72380.00 0.00Adj-Rsq -0.0007627 0.18010.028430.1676

This table summarizes the results from the BBB OLS regression  $s_{gkt} = \alpha + \beta_1 \Delta \text{VIX}_t + \beta_2 \Delta \text{TsySlp}_t + \beta_3 \text{CrdSlp}_t + \beta_4 \text{LQ}_t + \beta_5 \text{XSLQ}_t + \epsilon_t$  as defined in Eq. (25). The dependent variable considered are the BBB effective bid-ask spreads,  $s_{gkt}$  determined using the four microstructure models of Roll (1984) with positive autocovariance preserved for observations, Roll (1984) augmented with observations of positive autocovariance eliminated, Christopoulos (2020), and Thompson and Waller (1987). The five independent variables are the change in the VIX volatility index ('chgVIX'), the change in the Treasury slope ('chgTsySlope') of 10year - 2year yields, the change in the corporate credit slope ('chgCrdSlp') of BBB-AAA risk premia, the estimated CMBX sector wide indices weighted across all ratings and tranches for liquidity ('Lq') and excess liquidity ('XSLq') as depicted in Fig. (1). The significance codes of '\*\*\*', '\*\*', '\*\*', '\*\*', '\*\*', and '' indicate statistical significance at the 0.001, 0.01, 0.05 and 0.1 levels, respectively.

BBB CMBX In general, the finding for the BBB OLS are worse than the AAA case. The stand-out results are the signs and significance of the liquidity and excess liquidity indices which are negative, and highly significant for Models 2, 3 and 4. The other covariates are insignificant though, in the case of Model 3 the coefficient signs are mostly similar to the AAA case. The exception is in the change of the Treasury slope which exhibits a positive sign. This is encouraging as the credit sensitive portion of the capital structure (BBB) should be less influenced by yield curve dynamics than corresponding senior (AAA) credits.

As in the AAA case, Model 2 model provides the highest explanatory value as measured by the Adjusted R-squared of 0.1801, but it again suffers from the limited sample of 38% less observations than are considered by the other three models. Interestingly, we see lower incidence of positive autocovariance in BBB than AAA. In Model 2 for AAA there are 1164 incidents (2822-1658) while in BBB there are 1082 incidents (2822-1746). This could suggest that investors have more idiosyncratic risk information about loan and bond collateral and are somewhat less apt to simply engage in follow-on pricing exhibited in the more commoditized AAA classes which are protected from default driven losses through subordination. AAA securities are categorically more liquid than BBB's which, as subordinate classes, exhibit categorically wider bid-ask spreads, wider mid-market spreads, and smaller liquidity

and excess liquidity partitions than AAA's. This may be due in part to idiosyncratic concerns over the risk of default on underlying collateral. As such, the regressions for the BBB class of CMBX suggest that other drivers are materially influencing pricing of the securities, which in turn influences the bid-ask spread estimates. It is thus not surprising that the Adjusted R-squared values for the BBB regressions are categorically lower than for AAA. It is interesting that the Adjusted-R-squared value for Model 4 of 0.16786 is higher than the Adjusted R-squared for Model 3 of 0.02843. These statistics seem to support the distinctions between the senior AAA and the subordinate BBB securities and the presence of an influence of liquidity and excess liquidity embedded within market pricing. We investigate this further in Section 3.3.5.

#### 3.3.5 VAR, Granger and IRF for the Daily Model

While the OLS results are good, they are somewhat coarse to the task of liquidity evaluation. OLS relationships are contemporaneous and do not control for autoregressive behavior amongst covariates. In contrast, VAR and IRF techniques do provide such controls and are applied here to CMBX liquidity evaluation.

VAR With VAR, we estimate the 'true' value of the bid-ask spread,  $s_t$ , as the dependent variable at time t explained by its own lagged variables,  $s_{t-n}$ , and lagged market variables,  $M_{t-n}$ . The VAR we implement is of the form

$$s_{t} = \alpha + \sum_{n=1}^{N} \beta_{n} s_{t-n} + \sum_{n=1}^{N} \gamma_{n} M_{t-n} + \epsilon_{t}$$
 (26)

The *n*-period lagged  $\sum_{n=1}^{N} \beta_n s_{t-n}$  term serves as the sum of first-differenced bid-ask spread variables while the  $\sum_{n=1}^{N} \gamma_n M_{t-n}$  term captures the sum of first differenced market variables. In all cases, the *n*-period lags are determined by Akaike Information Criteria (AIC), and we permit up to n=10 daily lags (2 weeks of trading). Each market variable has one equation. The current time t observation of each variable depends upon lagged values of bid-ask spread estimates as well as lagged values for the market variable. Ivanov and Kilian (2005) conclude that *n*-order lag selections are ultimately discretionary to the project. As our lags comport with those found in the earlier literature, we are comfortable with this

choice. In the OLS, the liquidity measures categorically exhibit statistical significance and intuitively correct signs, and so we focus on those market variables to generate the IRFs. We restrict the analysis to Model 3 and Model 4 due to their reliability across the sample. The results of the VARs are provided in the <u>Appendix Section A.2</u> in <u>Tables 21 and 22</u>. They are as expected with high Adjusted R-squared values ranging from 0.73 to 0.84 and statistical significance for lagged bid-ask dependent variable as independent variable for both models across AAA and BBB credits. Interestingly, lagged values for excess liquidity indices exhibit greater statistical significance than liquidity indices in Model 3 (AbsRoll) but less so in Model 4 (ThomsonWaller).

Granger As with the VARs, the Granger tests are restricted to Models 3 and 4 and only test relationships between bid-ask spread and liquidity measures. In Panel B, for Models 3 and 4, we find strong statistical evidence at the 0.10% significance level with excess liquidity Granger causing AAA bid-ask spreads. For BBB bid-ask spreads only Model 4 exhibits statistical significance (0.10%) for excess liquidity Granger causing BBB bid-ask spreads, while Model 3 is insignificant. We find weaker evidence of liquidity Granger causing AAA or BBB bid-ask spreads for the exact same relationship across both models in Panel A. Panels C and D exhibit strong statistical support for bid-ask spreads Granger causing liquidity and excess liquidity, which is not surprising given both liquidity and excess liquidity are residual measures. These results are summarized below in Table 12.

IRF IRFs describe a response variable's evolution over a projected time horizon following a one standard deviation exogenous random shock to the initial values of the endogenous variables in VAR using the bootstrapping method. It is a statistical assessment of sensitivity (response) to a one-standard deviation shock (impulse) within the VAR and is conducted as a post-estimation analysis. Following Lütkepohl (2005), a moving average representation (also referred to as a forecast error impulse response, or FEIR,  $\Phi_i = \sum_{m=1}^i \Phi_{m-1} A_m, i = 1, 2, ...$ ) is an iterative formulation for  $\Phi_i$  with  $\Phi_0 = I_K$  and  $A_m$  the coefficient vector for lag m. To correctly account for the contemporaneous correlation between residuals of the covariates in the VAR, which is not accounted for in the coefficient vectors  $A_i$ , we orthogonalize the symmetric positive semi-definite variance covariance matrices,  $\Sigma$ , by determining P (a lower

Table 12: Granger Causality Test Statistics

Panel	A: Liquidity~Bi	d/Ask	Panel B: Excess	Liquidity~Bid/Ask
	AAA	BBB	AAA	BBB
ABSRoll	3.4706	0.6141	17.161	1.7907
	0.01549*	0.6058	4.83e-11***	0.1468
TW	3.1354	2.7673	11.318	12.729
	0.02451*	0.04036*	2.231e-07***	2.914e-08***
Panel	C: Bid/Ask~Liq	uidity	Panel D: Bid/As	sk~Excess Liquidity
	AAA	BBB	AAA	BBB
ABSRoll	5.0702	1.1208	6.9661	7.981
	0.001675**	0.3393	0.0001145***	2.69e-05***
TW	5.449	0.329	7.6033	16.434
	0.0009886***	0.8044	4.614e-05***	1.38e-10***

This table shows the results for the Granger causality tests with F-stat and p-value reported immediately below. All panels show statistics for AAA and BBB cases in separate columns. Rows indicate which effective bid-ask spread model is being use (the Absolute Roll measure of Christopoulos (2020) or Thompson and Waller (1987)). Panel A reports the impulse as CMBX liquidity with the response variables the effective bid-ask spreads. Panel B reports the impulse as CMBX excess liquidity with the response variables the effective bid-ask spread. Panel C reports the impulse as the effective bid-ask spread with CMBX liquidity as the response variables. Panel D reports the impulse as the effective bid-ask spread with CMBX excess liquidity as the response variables. \*\*\*/\*\*/\*' correspond to 0.1%, 1%, 5% and 10% levels of significance.

triangular matrix) using the Cholesky decomposition method that satisfies  $\Sigma = PP^{-1}$ . The corresponding orthogonal IRF, which accounts for contemporaneous correlations amongst regressors, is given by

$$\Theta_i^o = \Phi_i P \tag{27}$$

When calculating the IRFs we use exogenous one standard deviation shocks to the impulse variables such that for each forward period, h, we are able to determine the forecast results as shown in Figure 4. The plots depict the cumulative percentage change (y-axis) in the bid-ask spread using Model 3 at time  $t \in [0, h]$  on the x-axis following exogenous shocks of liquidity and excess liquidity risk partitions. The upper and lower dashed lines represent the upper and lower bounds of the 80% confidence interval while the line in the center represents the cumulative value of the IRF. The interpretation is one of a cumulative moving average forecast of bid-ask spreads over  $h \in [0, 20]$  trading days (about 1 month) following the respective shocks. AAA are depicted in the top panel while and BBB are depicted in the bottom panel. The results are good. The confidence interval boundaries lie above the zero partition indicating a clear response to the signal based upon the VAR interrelationships.

<u>Figure 4a</u> shows the impact on bid-ask spreads for a one standard deviation shock in excess liquidity. There we see the cumulative percentage response of bid-ask spreads for

AAA CMBX is to tighten by about 9 bps with BBB CMBX tightening by about 45 bps over the forecast period. <u>Figure 4b</u> tells a contrasting story with the cumulative percentage response of bid-ask spreads to a one standard deviation impulse shock to the liquidity index widening for AAA CMBX by about 5 bps following with BBB CMBX widening by about 25 bps.

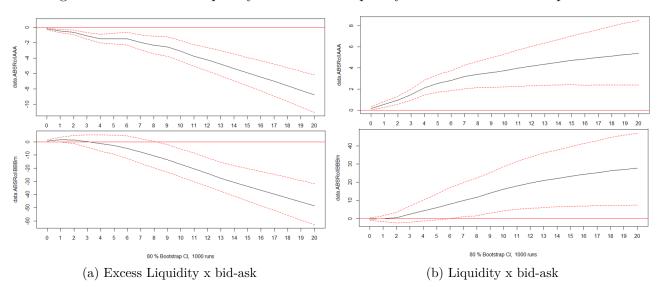


Figure 4: IRF's from Liquidity and Excess Liquidity Indices onto bid-ask spreads

This figure provides the cumulative IRFs for effective bid-ask spreads modelled with the AAA and BBB Absolute Roll Measure of Christopoulos (2020) VARs for liquidity and excess liquidity with lag order 10 periods. The upper and lower dashed lines represent the upper and lower bounds of the 80% confidence interval while the line in the center depicts the values of IRF over time. It is the moving average evolution forecast of the response variable (effective bid-ask spreads) over 20 days (about 1 trading month) years following the shock of CMBX liquidity and CMBX excess liquidity. The x-axis, shows forward days, for each of the variables. The y-axis shows the cumulative percentage change from time t=0 to t=h. The top chart of Fig. (4b) depicts the AAA CMBX effective bid-ask spread response to a 1 standard deviation shock in CMBX liquidity, while the bottom chart of Fig. (4a) depicts the AAA CMBX effective bid-ask spread response to a 1 standard deviation shock in CMBX excess liquidity, while the bottom chart of Fig. (4a) depicts the BBB CMBX effective bid-ask spread response to a 1 standard deviation shock in CMBX excess liquidity.

As liquidity and excess liquidity partitions contemplate portions of market spreads that are not accounted for by rate volatility and default risk, such liquidity partitions can be thought of as additional compensation in market spreads in excess of model articulated risks. Liquidity availability can be subsumed within observed risk premia as noted in Jarrow (2007), Bao, Pan and Wang (2011), Carr and Yu (2012) and Christopoulos (2017), among others. Excess liquidity captures the condition where total theoretical risk premia implied by simulated risk neutral prices exceeds the observed risk premia implied by market prices. Increases in excess liquidity instantaneously should correspond with tighter bid-ask spreads. And it thus makes sense in the IRF that increases in excess liquidity forecast future bid-ask spread tightening. Excess liquidity is the most extreme form of liquidity assessment and it is plausible that even if excess liquidity is not actively revealed to the market as yet, that

other signals correlated with excess liquidity are signalling to market actors, resulting in assessments that the bonds are inexpensive relative to their risks.

The more nuanced case is in revealed liquidity availability. If, as a theoretical measure, liquidity availability increases and the market is unaware of this, it can suggest that market is simply uncertain of the underlying risks of the securities. This would be consistent with the findings of Bao, O'Hara and Zhou (2018) where the impact results in more restrictive risk policy not substantiated by underlying risks. If market spreads are widening in excess of the theoretical assessment of default and rate risks then, mechanically, liquidity availability will increase. But if no one knows about the partitioning, then all the market sees is market spreads widening. It is thus plausible that the liquidity shock in the IRF will correspond to future uncertainty evidenced by projected bid-ask spread widening. Finally, we note that the Daily Model is well specified because the four elements of the Daily Model are not collinear. The proof of this is found in Appendix Section A.3.

As shown in the OLS, liquidity risk partitions play a significant role in CMBX price formation (our *first main result*). They give rise to our time series analyses with VAR, Granger and IRFs. This produces our *second main result* from the IRFs that liquidity partitions also have a significant effect on future observed CMBX liquidity as measured by projected effective bid-ask spreads. This establishes a theoretical relationship for CMBX between microstructure estimates of liquidity in effective bid-ask spreads and estimated reduced form assessments of liquidity. Together these results validate the Daily Model.

# 4 The Intraday Model

This section introduces the Intraday Model and uses all indexed investment grade CMBX classes in the validation of the risk partitions. As discussed in <u>Section 1</u>, there are no observable CMBX intraday prices (spreads). And so it is not possible to validate the risk partitions with observed market prices or, even theoretical effective bid-ask spreads. However, the theoretical underpinning of CMBX risk partitions provide insights into the related REIT sector. We disclose that relationship in this section and use it to validate with ICAPM.

# 4.1 Instantaneous changes

With the exception of CMBX market spreads, the Daily Model, validated in the previous section, is based on changes in explanatory variables in Eq. (29) which capture the economy of REITs, US Treasuries and the VIX. There is nothing in principle that prevents us from increasing the frequency of estimation for all risk components from daily, to shorter intervals intraday. In this section we increase the frequency of linear estimation from daily to 15 second intervals, *intraday*, for each trading day in the Covid-19 pandemic in our sample (the 'Intraday Model').

For the Intraday Model, all mathematics apply to all trading days u and time t is the intraday time index with  $t \in [1, 1560]$  15 second intervals from 9:30:15am to 4:15:00pm EST for each trading day u. Once the daily initial conditions have been determined, for each trading day u intraday changes in risk composition are then modelled as a zero-centered function of the evolution of the factors

$$\Delta y_{jk}(t) = \sum_{i=1}^{5} \eta_{ijk} \Delta f_i(t) + \varepsilon_{jk}^{\Delta}(t)$$
 (28)

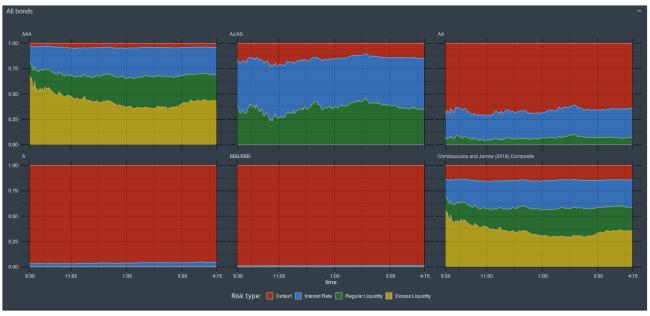
for the j-th risk partition of the k-th bond at time t. We compute a covariance matrix such that  $\eta_{ijk}$  is the covariate of the i-th factor with the corresponding bond's corresponding risk component. The coefficients  $\eta_{ijk}$  are determined through OLS and  $\varepsilon_{jk}^{\Delta}(t)$  has expected mean zero with standard deviation  $\sqrt{\eta_{0jk}}$ . We normalize the sum of the proportions for the intraday risk decomposition to 1 as was done previously for daily observations in Eq. (17).

The final risk composition is then calculated using the initial condition and the instantaneous changes:

$$y_{jk}(t) = y_{jk}(t_0) + \sum_{t'=1}^{t} \Delta y_{jk}(t')$$
(29)

where the *intraday* estimation of risk components  $y_{jk}(t)$  is the j-th component of the risk partition for bond k at time t on trading day u. The first term on the righthand side,  $y_{jk}(t_0)$ , is the initial value of the risk component intraday and the second term  $\sum_{t'=1}^{t} \Delta y_{jk}(t')$  the intraday sum of the changes in the risk component defined in Eq. (28).

Figure 5: CMBX intraday risk decomposition (15 second intervals)



(a) CMBX intraday, 20200417



(b) CMBX intraday, 20201204

This figure provides proportional intraday CMBX risk decomposition in 1560, 15 second intervals. The four components of risk modelled are default, interest rates, liquidity and excess liquidity. The x-axis capture the time intervals from 9:30:15am to 4:15:00pm.EST The y-axis captures the estimated proportion of CMBX risk embedded within CMBS spreads as determined in Eq. (17). Fig. (6a) captures the intraday evolution of CMBX proportional risk decompositions on April 17, 2020 and Fig. (6b) captures the intraday evolution of CMBX proportional risk decompositions on December 4, 2020. Separate evolutions are provided for each of the investment grade CMBX tranches, as well as for the weighted average composite index across all investment grade CMBX as shown monthly in Christopoulos and Jarrow (2018).

Although the time scales for the training data and intraday time steps of 15 seconds are vastly different, they appear to scale well. What we see in Figure 5 is the first-ever intraday evolution of risk decompositions,  $y_{jk}(t)$  as defined in Eq. (29) for CMBX over two trading days for all  $j \in [1, 4]$  risk partitions and  $k \in [1, 6]$  credit ratings. The risk partitions are observed for  $t \in [1, 1560]$  consecutive 15 second intervals in length per trading day. The first estimation occurs at or after 9:30:15 seconds following the market open; the last estimation occurs at or about 4:15:00pm. The variability at the open occurs because the implementation requires the information released at 9:30:00am, the variability at the close is due to reporting delays which may occur slightly before or slightly after 4:15:00pm. The risk partitions at the tranche level are projections based on the indexed training set computed from simulated primitives in Eq. (9). Figure 5 investment grade CMBX bond risk partitions for the investment grade classes and for the aggregate composite ('Christopoulos and Jarrow (2018) Composite').

The risk composites vary considerably across credit rating classes, days, and intraday. The rank order results by credit ratings are similar to findings of Longstaff, Mithal and Neis (2005) in the corporate bond sector regarding the proportion of the risk of default embedded in spreads varying by credit rating. The intraday decompositions reflect updated live data for 25 REITs, 4 US Treasuries, and the VIX index as previously described. Figure 6a shows the evolution for u = April 17, 2020 in the early stages of the Covid-19 global pandemic with the Dow Jones Industrial Average (Dow) closing 23537, while Figure 6b shows the evolution of the risk decomposition indices on u = December 4, 2020 with the Dow closing at 30217. The sum of all compositions on all intervals are normalized to 1. Although we show only two trading dates, these evolutions are captured intraday in 15 second intervals for all 240 trading days between April 7, 2020 and April 8, 2021 in this study. 13

As noted in Christopoulos (2017), model estimated liquidity of CMBX vary considerably across credit ratings and time. AAA CMBS securities make up about 80 percent of the CMBS market due to the senior/subordinate capital structure as noted in An, Deng, Nichols and Sanders (2015) and Riddiough and Zhu (2016) while subordinate BBB- CMBS make up less than 5 percent of the market. As BBB- securities are more immediately exposed to loss manifestation following a default event than AAA securities a smaller proportion of the

<sup>&</sup>lt;sup>13</sup>These values are available every trading day. See https://risktape.warg.wotnrisk.com/ for more details.

risk compensation above the risk free rate for BBB- securities should be associated with liquidity availability when compared with AAA. This dynamic is confirmed in Christopoulos (2017) and Christopoulos and Jarrow (2018) in indexed form from 2007-2015 in monthly simulations and is confirmed again in the results of this paper with bid-ask comparisons with such measures daily (as previously discussed), and now as evident, intraday.

# 4.2 Validation of the Intraday Model

### 4.2.1 Statistical summary for the Intraday Model

Table 13: Summary statistics of cumulative changes of intraday CMBX risk partitions

Panel A: Default	AAA	AJ	AA	A	BBB	BBB-
min max mean median variance stdev obs	$\begin{array}{c} 0.483416 \\ 1.820368 \\ 1.000102 \\ 1.000000 \\ 0.000212 \\ 0.014562 \\ 275370 \end{array}$	$\begin{array}{c} 0.338351 \\ 8.403204 \\ 1.000104 \\ 1.000000 \\ 0.000380 \\ 0.019491 \\ 275370 \end{array}$	$\begin{array}{c} 0.494514 \\ 6.036482 \\ 1.000046 \\ 1.000000 \\ 0.000156 \\ 0.012485 \\ 275370 \end{array}$	$\begin{array}{c} 0.609670 \\ 6.121692 \\ 1.000039 \\ 1.000000 \\ 0.000147 \\ 0.012127 \\ 275370 \end{array}$	$\begin{array}{c} 0.717165 \\ 1.913765 \\ 1.000012 \\ 1.000000 \\ 0.000020 \\ 0.004425 \\ 275370 \end{array}$	0.823893 1.400509 1.000005 1.000000 0.000006 0.002384 275370
Panel B: Rate risk	AAA	AJ	AA	A	BBB	BBB-
min max mean median variance stdev obs	0.702365 1.518098 1.000010 1.000000 0.000019 0.004340 275370	0.610945 1.742393 1.000137 1.000000 0.000281 0.016768 275370	0.530693 2.244835 1.000058 1.000000 0.000123 0.011092 275370	0.583500 1.871355 1.000042 1.000000 0.000086 0.009273 275370	$\begin{array}{c} 0.476037 \\ 1.976362 \\ 1.000061 \\ 1.000000 \\ 0.000123 \\ 0.011089 \\ 275370 \end{array}$	0.599777 1.469975 1.000024 1.000000 0.000041 0.006433 275370
Panel C: Liquidity	AAA	AJ	AA	A	BBB	BBB-
min max mean median variance stdev obs	$\begin{array}{c} 0.735970 \\ 1.707165 \\ 1.000036 \\ 1.000000 \\ 0.000078 \\ 0.008806 \\ 275370 \end{array}$	$\begin{array}{c} 0.330755 \\ 8.456980 \\ 1.000466 \\ 1.000000 \\ 0.001217 \\ 0.034890 \\ 275370 \end{array}$	$\begin{array}{c} 0.030144 \\ 9.348418 \\ 1.000559 \\ 1.000000 \\ 0.001370 \\ 0.037017 \\ 275370 \end{array}$	$\begin{array}{c} 0.016780 \\ 27.908990 \\ 1.000738 \\ 1.000000 \\ 0.007370 \\ 0.085848 \\ 275370 \end{array}$	$\begin{array}{c} 0.275537 \\ 2.411473 \\ 1.000176 \\ 1.000000 \\ 0.000361 \\ 0.019004 \\ 275370 \end{array}$	$\begin{array}{c} 0.134313 \\ 6.462325 \\ 1.000397 \\ 1.000000 \\ 0.000976 \\ 0.031240 \\ 275370 \end{array}$
Panel D: XS liquidity	AAA	AJ	AA	A	BBB	BBB-
min max mean median variance stdev obs	$\begin{array}{c} 0.346666 \\ 3.379393 \\ 1.000147 \\ 1.000000 \\ 0.000333 \\ 0.018239 \\ 275370 \end{array}$	$\begin{array}{c} 0.136986 \\ 7.812876 \\ 1.000329 \\ 1.000000 \\ 0.000868 \\ 0.029465 \\ 275370 \end{array}$	$\begin{array}{c} 0.508825 \\ 2.413748 \\ 1.000074 \\ 1.000000 \\ 0.000152 \\ 0.012328 \\ 275370 \end{array}$	$\begin{array}{c} 0.508825 \\ 2.413748 \\ 1.000074 \\ 1.000000 \\ 0.000152 \\ 0.012328 \\ 275370 \end{array}$	$\begin{array}{c} 0.508825 \\ 2.413748 \\ 1.000074 \\ 1.000000 \\ 0.000152 \\ 0.012328 \\ 275370 \end{array}$	$\begin{array}{c} 0.140683 \\ 6.325317 \\ 1.000184 \\ 1.000000 \\ 0.000719 \\ 0.026816 \\ 275370 \end{array}$

This table provides summary statistics of intraday CMBX risk partitions. The columns show the investment grade credit rating class and the rows the summary statistics of minimum (min), maximum (max), mean, median, variance, standard deviation (stdev), kurtosis and the number of observation (obs). Panel A summarizes for default risk, Panel B summarizes for interest rate risk, Panel C summarizes for liquidity, while Panel D summarizes for excess (XS) liquidity.

Table 13 provides a statistical summary across all observations intraday for default, rates, liquidity and excess liquidity risk partitions. The summary results generally follow intuition with some new insights and we exhibit all investment grade classes. Focusing first on intraday default risk pricing, we observe AAA CMBX appear to exhibit substantially greater volatility than BBB-, with only the AJ exhibiting greater volatility. Rates volatility pricing intraday is much calmer than default intraday pricing across most credits with the exception of the BBB class. Again, as with default, the AJ class appears to exhibit higher volatility than the AAA class. This relatively higher volatility for the AJ class compared with the AAA class repeats across all four risk measures. Finally, as we are concentrating on liquidity, the low nominal amounts of both liquidity and excess liquidity in BBB- classes should result in higher volatility estimates reflective of scarce liquidity availability. Min and max values follow intuition suggesting that the capital structure allocation concentrates mispricing in the mid-section with the endpoints of AAA and BBB- exhibiting more regular behavior.

### 4.2.2 Cross sectional visualizations for the Intraday Model

While the summary information in <u>Table 13</u> is interesting from an academic perspective, it is fundamentally limited for two reasons. First, the values estimated intraday still must use an initial set of simulated values and market spreads. The simulated risk decomposition studies of Christopoulos (2017) and Christopoulos and Jarrow (2018), reflecting actual cashflow and updated credit and prepayment profiles, end in 2015.

Second, the initialized spread value informing these evolutions are restricted to only March 18, 2020 because no additional daily CMBX pricing data was made available to us after that date. In this sense, the intraday results depicted are essentially cross-sectional intraday stress tests of the response of risk decompositions holding market spreads as of March 18, 2020 held constant. Although the limitations of the initialization restrict the validity of the intraday time series across dates, they will reveal insights in cross sectional analysis. Each day is a valid time series and the collection of all dates represents the set for cross section evaluation. At the same time, because the real time estimations are price independent, observing their changes over time yields some unique insights. One way to approach the evaluation of cross section of daily time series is through the heat map approach using binning. We want to cast the daily risk pricing data against both time and a relevant

variable. The VIX provides such a variable as a dominant explanatory variable in the previous daily historical analysis.

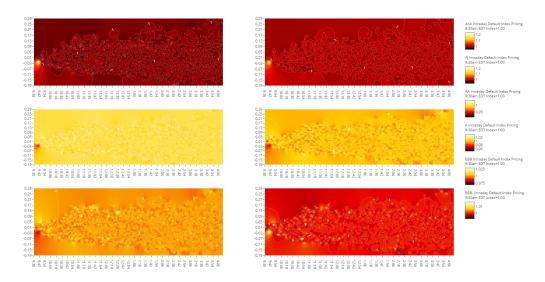


Figure 6: Default cross section (all observations)

This figure provides the cross section across all 275370 observations of default risk composition for each of the investment grade CMBX tranches from AAA (top-left) to BBB- (bottom right). The x-axes reflect 3 minute intervals binned from the 15 second interval values while the y-axes capture the log change of the VIX from the start of the trading day (with t=0, 9:30am) until close. The y-axes are partitioned in increments of 0.01. The z-axes are the heat maps for default risk with non-constant upper and lower boundaries, but identical colorscale palettes. The contour lines and hue of indicate higher or lower cumulative changes in default risk across all days in the sample period at identical times.

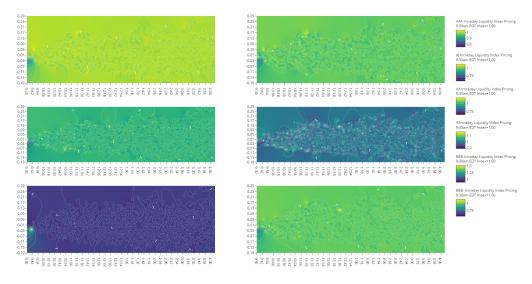


Figure 7: Liquidity cross section (all observations)

This figure provides the cross section across all 275370 observations of liquidity risk composition for each of the investment grade CMBX tranches from AAA (top-left) to BBB- (bottom right). The x-axes reflect 3 minute intervals binned from the 15 second interval values while the y-axes capture the log change of the VIX from the start of the trading day (with t=0, 9:30am) until close. The y-axes are partitioned in increments of 0.01. The z-axes are the heat maps for liquidity risk with non-constant upper and lower boundaries, but identical colorscale palettes. The contour lines and hue of indicate higher or lower cumulative changes in liquidity risk across all days in the sample period at identical times.

Figure 6 shows 275370 observations computed for each of the intraday default risk par-

tition pricings. We use a double binning method to observe. The x-axes reflect 3 minute intervals binned from the 15 second interval values while the y-axes capture the log change of the VIX from the start of the trading day (with t=0, 9:30am) until close. The y-axes are partitioned in increments of 0.01. The z-axes are the heat maps with non-constant upper and lower boundaries, but identical colorscale palettes. This is purposeful, as each of the classes may have inherently different sensitivities to market indicators. The plots represent the data for each of the CMBX classes with AAA in the upper left, AJ upper right, and so forth, with BBB- in the bottom right. The color saturation produced for each plot is interesting during the Covid period. Together they suggest somewhat lower intraday default risk pricing for AAA, AJ and BBB- classes compared with the AA, A and BBB classes. In Figure 7 we take the same vantage point but for liquidity availability. Here, we see somewhat greater intraday liquidity availability for AAA with the least liquidity available for A and BBB classes as indicated by the color palettes and contour lines.

These perspectives document some important facts in theoretical observation of CMBX risk pricing during the Covid period, one of the most interesting being an apparent regular 'spot' of volatility in the first 15 minutes of trading in the cross section. This repeats across all instruments and risk partitions in our sample. Figure 8 zooms in on this interval for each of the risk partitions for all classes to revealing more detail of the phenomenon. There we see 'peaks' as indicated by the contour lines exceeding 1, and 'valleys' as indicated by contour lines less than one clustered about 9:39am. The subplots depict risk pricing for default, liquidity, excess liquidity and rates indices for all investment grade credit rating classes. For example, consider in Figure 8 the case of intraday liquidity availability pricing in the second composite of six plots on the top right. At about 9:39am we observe considerable cross-sectional deterioration in liquidity availability for AAA, AJ, AA and BBB- classes with contour labels in 'valleys' ranging from 0.70 to 0.84. In contrast class A class shows relatively more modest deterioration in liquidity availability at about 0.94 while the BBB class shows expansion of liquidity availability of about 1.35. These types of comparisons can be made for all credit ratings classes and all estimated risk partitions generated by the Intraday Model.

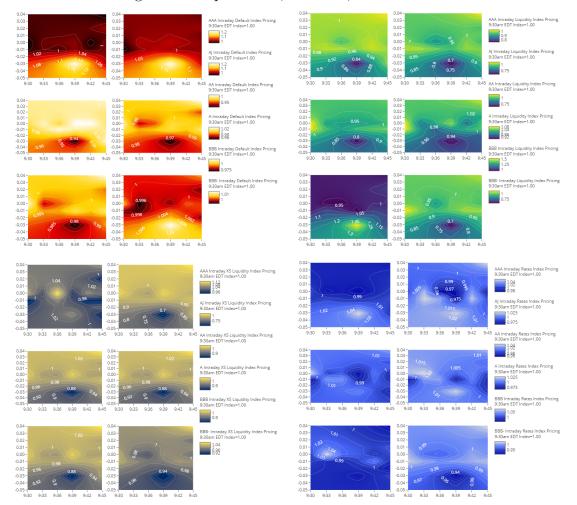


Figure 8: All partitions, all dates, 9:30:00am to 9:45:00am

This figure provides the cross section across all 275370 observations of risk composition for each of the four risk components (default, top left), liquidity (top right), excess (XS) liquidity (bottom left) and interest rates (bottom right). Each of the four risk component contain six charts depicting the investment grade CMBX tranches from AAA (top-left) to BBB- (bottom right). The x-axes reflect 3 minute intervals binned from the 15 second interval values from 9:30:15am to 9:45:00am EST. The y-axes capture the log change of the VIX from the start of the trading day (with t=0, 9:30:15am) until 9:45:00am. The y-axes are partitioned in increments of 0.01. The z-axes are the heat maps for the risk components with non-constant upper and lower boundaries, but identical colorscale palettes. The contour lines and hue of indicate higher or lower cumulative changes in liquidity risk across all days in the sample period at identical times.

In <u>Tables 14 and 15</u> we compress these statistically for two (out of 1560) points during the trading day: the opening bell values (9:30:15) and closing bell values (4:15:00), respectively across the 246 trading days in our sample. The tables corroborate the visual insights from the cross-sectional plots: The opening is indeed much more volatile than the closing, for the risk partitions as measured by the standard deviation (stdev).

Table 14: Open Summary during Covid

	Table	e 14: Opei		y during			
variable	mean	median	min	max	variance	stdev	n
VIX	26.7659	25.6000	16.5500	47.3400	31.88860	5.6470	246
IN_DRE IN_FR IN_PLD IN_SELF	$\begin{array}{c} 37.9874 \\ 41.0038 \\ 98.7801 \\ 4.0519 \end{array}$	$38.5400 \\ 41.5825 \\ 99.5750 \\ 4.0000$	$30.4000 \\ 33.1700 \\ 81.4700 \\ 3.5200$	$\begin{array}{c} 43.0600 \\ 47.3700 \\ 109.7950 \\ 5.0500 \end{array}$	6.83532 8.22299 35.65076 0.08360	$\begin{array}{c} 2.6144 \\ 2.8676 \\ 5.9708 \\ 0.2891 \end{array}$	246 246 246 246
LO_HST LO_MAR LO_WYND LO_MGM	12.8944 109.4389 37.0577 24.6343	$\begin{array}{c} 11.8875 \\ 100.5550 \\ 33.4700 \\ 22.3325 \end{array}$	$\begin{array}{c} 9.1400 \\ 72.7600 \\ 21.0900 \\ 12.1100 \end{array}$	18.4200 155.7419 51.7500 41.7300	4.94857 495.52655 93.63226 63.82471	2.2245 22.2604 9.6764 7.9890	246 246 246 246
MF_AVB MF_ELS MF_EQR MF_UDR	162.0976 62.7243 60.1919 37.7456	159.2000 62.7025 59.3700 37.4550	133.1000 55.8600 46.0100 29.9100	193.5300 68.2900 75.9600 45.6700	145.65429 5.18841 37.04669 11.21798	12.0687 2.2778 6.0866 3.3493	246 246 246 246
OF_BXP OF_CLI OF_HIW OF_SLG OF_VNO	91.4597 14.0493 37.9485 54.5778 38.3335	91.0200 13.8825 38.0200 50.6400 37.5750	70.7300 10.4000 29.4500 36.8300 29.9550	108.5900 18.5100 45.1700 77.1200 49.0300	74.19748 2.23470 10.21290 93.46684 16.31488	8.6138 1.4949 3.1958 9.6678 4.0392	246 246 246 246 246
OT_BKD OT_NNN OT_PSB OT_WPC	3.8272 $37.3254$ $133.0409$ $67.5772$	$\begin{array}{c} 3.3900 \\ 36.8075 \\ 131.7250 \\ 68.2300 \end{array}$	$\begin{array}{c} 2.4400 \\ 27.1050 \\ 110.3200 \\ 54.5500 \end{array}$	$\begin{array}{c} 6.7500 \\ 45.8552 \\ 159.8700 \\ 75.0000 \end{array}$	$\begin{array}{c} 1.36962 \\ 17.25113 \\ 106.10071 \\ 12.15876 \end{array}$	$\begin{array}{c} 1.1703 \\ 4.1534 \\ 10.3005 \\ 3.4869 \end{array}$	246 246 246 246
RT_KIM RT_REG RT_SPG RT_TCO	13.6444 45.0055 78.3857 40.0019	$\begin{array}{c} 12.6550 \\ 44.4750 \\ 69.6225 \\ 40.4050 \end{array}$	$\begin{array}{c} 8.3400 \\ 34.0300 \\ 49.7200 \\ 28.1450 \end{array}$	$\begin{array}{c} 19.7200 \\ 59.8800 \\ 120.4975 \\ 46.8000 \end{array}$	8.91863 38.80736 364.88435 13.19712	2.9864 6.2296 19.1019 3.6328	246 246 246 246
TSY_3MO TSY_5YR TSY_10YR TSY_30YR	$\begin{array}{c} 0.0854 \\ 0.4095 \\ 0.8936 \\ 1.6290 \end{array}$	$\begin{array}{c} 0.0880 \\ 0.3600 \\ 0.7735 \\ 1.5460 \end{array}$	$\begin{array}{c} 0.0030 \\ 0.2060 \\ 0.5260 \\ 1.1380 \end{array}$	$\begin{array}{c} 0.2350 \\ 0.9710 \\ 1.7490 \\ 2.4960 \end{array}$	$\begin{array}{c} 0.00149 \\ 0.02983 \\ 0.10170 \\ 0.11141 \end{array}$	$\begin{array}{c} 0.0386 \\ 0.1727 \\ 0.3189 \\ 0.3338 \end{array}$	246 246 246 246
$\begin{array}{c} AAA\_def\\ AAA\_rates\\ AAA\_reglq\\ AAA\_xslq \end{array}$	1.0131 1.0015 1.0046 1.0118	$\begin{array}{c} 1.0015 \\ 1.0001 \\ 0.9995 \\ 0.9994 \end{array}$	$\begin{array}{c} 0.6218 \\ 0.8004 \\ 0.7360 \\ 0.3467 \end{array}$	1.8204 1.5181 1.3345 3.1465	$\begin{array}{c} 0.01493 \\ 0.00313 \\ 0.00616 \\ 0.04744 \end{array}$	$\begin{array}{c} 0.1222 \\ 0.0560 \\ 0.0785 \\ 0.2178 \end{array}$	246 246 246 246
$\begin{array}{c} {\rm AJ\_def} \\ {\rm AJ\_rates} \\ {\rm AJ\_reglq} \\ {\rm AJ\_xslq} \end{array}$	1.0457 1.0023 1.0303 1.0308	$\begin{array}{c} 1.0008 \\ 0.9998 \\ 0.9959 \\ 0.9975 \end{array}$	$\begin{array}{c} 0.5545 \\ 0.8048 \\ 0.3308 \\ 0.1370 \end{array}$	8.4032 1.3263 2.8615 4.5724	$\begin{array}{c} 0.23584 \\ 0.00365 \\ 0.10486 \\ 0.11270 \end{array}$	$\begin{array}{c} 0.4856 \\ 0.0604 \\ 0.3238 \\ 0.3357 \end{array}$	246 246 246 246
$\begin{array}{c} {\rm AA\_def} \\ {\rm AA\_rates} \\ {\rm AA\_reglq} \\ {\rm AA\_xslq} \end{array}$	$\begin{array}{c} 1.0277 \\ 1.0082 \\ 1.0092 \\ 1.0087 \end{array}$	$\begin{array}{c} 1.0000 \\ 1.0003 \\ 0.9982 \\ 0.9992 \end{array}$	$\begin{array}{c} 0.5937 \\ 0.6064 \\ 0.0301 \\ 0.5088 \end{array}$	$\begin{array}{c} 6.0365 \\ 2.2448 \\ 3.0219 \\ 2.4137 \end{array}$	$\begin{array}{c} 0.10726 \\ 0.01458 \\ 0.07331 \\ 0.02058 \end{array}$	$\begin{array}{c} 0.3275 \\ 0.1207 \\ 0.2708 \\ 0.1435 \end{array}$	246 246 246 246
$\begin{array}{c} A\_\mathrm{def} \\ A\_\mathrm{rates} \\ A\_\mathrm{reglq} \\ A\_\mathrm{xslq} \end{array}$	1.0219 1.0084 1.0013 1.0087	0.9997 0.9995 1.0004 0.9992	$\begin{array}{c} 0.6108 \\ 0.7212 \\ 0.0168 \\ 0.5088 \end{array}$	6.1217 1.8714 3.4114 2.4137	$\begin{array}{c} 0.11167 \\ 0.00939 \\ 0.05614 \\ 0.02058 \end{array}$	0.3342 0.0969 0.2369 0.1435	246 246 246 246
BBB_def BBB_rates BBB_reglq BBB_xslq	$\begin{array}{c} 1.0050 \\ 1.0101 \\ 0.9934 \\ 1.0087 \end{array}$	$\begin{array}{c} 0.9999 \\ 1.0001 \\ 0.9982 \\ 0.9992 \end{array}$	$\begin{array}{c} 0.7172 \\ 0.6726 \\ 0.3555 \\ 0.5088 \end{array}$	1.9138 1.4887 1.9290 2.4137	$\begin{array}{c} 0.00514 \\ 0.00836 \\ 0.02679 \\ 0.02058 \end{array}$	$\begin{array}{c} 0.0717 \\ 0.0914 \\ 0.1637 \\ 0.1435 \end{array}$	246 246 246 246
BBBm_def BBBm_rates BBBm_reglq BBBm_xslq	1.0029 1.0012 1.0430 1.0062	1.0001 1.0000 0.9956 0.9992	0.9184 0.5998 0.1343 0.3763	1.4005 1.3887 5.0141 2.7905	0.00095 0.00533 0.15543 0.03548	0.0308 0.0730 0.3942 0.1884	246 246 246 246

This table summarizes the observations of intraday data at the open of the trading day 9:30:15ET for 246 trading days during the pandemic (4/2020 - 4/2021). The first column provides the abbreviation for the variable name. The VIX is the CBOE volatility index. This is followed by the prices of 25 REITs with the name a composite made up of the property type (industrial (IN), hotel/lodging (LO), multifamily (MF), mixed use/other (OT), office (OF) and retail (RT)) and the REIT's stock market ticker. Following the REITs are US Treasury yields with ticker representing the 4 maturities of 3 month, 5 year, 10 year and 30 year. The remaining values are the simulated risk partitions indexed in Christopoulos and Jarrow (2018) in cumulative change form. The ticker is a composite of the 4 types of risk partitions default (def), interest rates (rates), liquidity (reglq) and excess liquidity (xslq) combined with the credit rating class names of AAA, AJ, AA, A, BBB and BBB- (BBBm). Each of the columns to the right of the ticker report statistics across all 246 observations.

Table 15: Close Summary during Covid

:-1-1-	1able		e Summar				
variable	mean	median	min	max	variance	stdev	<u>n</u>
VIX	26.6096	25.6550	16.9900	45.4300	29.64890	5.4451	246
IN_DRE	38.0191	38.4550	30.4000	43.0300	6.75872	2.5998	246
IN_FR IN PLD	41.0291 $98.7703$	$41.6200 \\ 99.6100$	$33.3500 \\ 82.8500$	$\begin{array}{c} 47.4500 \\ 109.5300 \end{array}$	$8.21028 \\ 36.53448$	$2.8654 \\ 6.0444$	$\frac{246}{246}$
IN SELF	4.0505	4.0000	3.5622	5.0500	0.08343	0.2888	$\frac{240}{246}$
LO HST	12.8848	11.9275	9.4500	18.4200	4.91837	2.2177	246
LO MAR	109.2835	100.3450	75.2600	157.5000	492.77623	22.1986	246
LO_WYND	37.0491	33.2800	21.3900	51.7500	92.64766	9.6254	246
LO_MGM	24.6201	22.0400	12.6800	42.2000	63.62672	7.9766	246
${ m MF\_AVB} \ { m MF\_ELS}$	$\begin{array}{c} 161.9634 \\ 62.7417 \end{array}$	$159.0800 \\ 62.6450$	$132.7800 \\ 56.1500$	$193.6100 \\ 68.2900$	$\begin{array}{c} 143.79254 \\ 5.27037 \end{array}$	$\begin{array}{c} 11.9914 \\ 2.2957 \end{array}$	$\frac{246}{246}$
MF EQR	60.1311	59.3700	46.2300	74.9600	37.29848	6.1072	$\frac{240}{246}$
MF_UDR	37.7246	37.5050	29.6000	45.5600	11.21592	3.3490	246
OF BXP	91.4361	91.2000	71.1500	108.6600	73.53062	8.5750	246
OF_CLI	14.0223	13.8000	10.4100	18.6900	2.24609	1.4987	246
OF_HIW OF_SLG	$37.9085 \\ 54.5360$	$38.0250 \\ 51.1750$	$29.7050 \\ 36.8200$	$\begin{array}{c} 45.2300 \\ 77.7900 \end{array}$	$\begin{array}{c} 10.27220 \\ 92.16894 \end{array}$	$\frac{3.2050}{9.6005}$	$\frac{246}{246}$
OF_VNO	38.2630	37.4800	30.1900	49.0100	16.01428	4.0018	$\frac{240}{246}$
OT BKD	3.8215	3.4050	2.4350	7.0500	1.37638	1.1732	246
OT_NNN	37.3067	36.7350	27.6000	45.6000	16.87934	4.1084	246
$ \begin{array}{c} \text{OT\_PSB} \\ \text{OT WPC} \end{array} $	$\begin{array}{c} 133.0165 \\ 67.5539 \end{array}$	$131.8750 \\ 68.1400$	$110.3100 \\ 54.5600$	$159.9100 \\ 74.3100$	$\begin{array}{c} 107.41229 \\ 11.90968 \end{array}$	$10.3640 \\ 3.4510$	$\frac{246}{246}$
RT_KIM RT REG	$\begin{array}{c} 13.6380 \\ 44.9848 \end{array}$	$12.7100 \\ 44.4500$	$8.3000 \\ 34.0500$	$\begin{array}{c} 19.7000 \\ 59.6500 \end{array}$	8.91577 $38.49700$	$2.9859 \\ 6.2046$	$\frac{246}{246}$
RT SPG	78.2918	69.4800	51.2000	121.1400	363.46241	19.0647	$\frac{240}{246}$
RT_TCO	40.0404	40.4700	32.8700	46.6900	12.51065	3.5370	246
TSY_3MO	0.0850	0.0880	0.0030	0.2100	0.00149	0.0386	246
$\begin{array}{c} { m TSY\_5YR} \\ { m TSY} & 10{ m YR} \end{array}$	$0.4094 \\ 0.8942$	$0.3620 \\ 0.7630$	$0.1950 \\ 0.5150$	$0.9410 \\ 1.7460$	$0.02932 \\ 0.10130$	$0.1712 \\ 0.3183$	$\frac{246}{246}$
$TSY_{30YR}^{131}$	1.6306	1.5450	1.1620	2.4760	0.10130 $0.11075$	$0.3183 \\ 0.3328$	$\frac{240}{246}$
AAA def	0.9997	0.9999	0.9806	1.0272	0.00002	0.0039	246
AAA_rates	1.0001	1.0000	0.9971	1.0066	0.00000	0.0010	246
$AAA$ _reglq	1.0001	1.0001	0.9745	1.0138	0.00001	0.0032	246
AAA_xslq	1.0006	1.0000	0.9696	1.0326	0.00004	0.0060	246
$_{ m AJ\_def}^{ m AJ\_tes}$	$1.0001 \\ 1.0002$	$1.0000 \\ 1.0001$	$0.9913 \\ 0.9666$	$1.0217 \\ 1.0247$	$0.00001 \\ 0.00002$	$0.0026 \\ 0.0040$	$\frac{246}{246}$
AJ_reglq	1.0002	1.0001	0.9000 $0.9176$	1.0409	0.00002	0.0040 $0.0092$	$\frac{240}{246}$
$AJ_xslq$	0.9988	1.0000	0.9528	1.0172	0.00006	0.0079	246
AA_def	1.0000	1.0000	0.9866	1.0188	0.00000	0.0018	246
AA_rates	1.0004	1.0003	0.9775	1.0225	0.00002	0.0043	246
$egin{array}{l} \mathrm{AA\_reglq} \ \mathrm{AA\_xslq} \end{array}$	$0.9992 \\ 0.9995$	$1.0000 \\ 1.0000$	$0.9347 \\ 0.9776$	$\frac{1.0215}{1.0071}$	$0.00004 \\ 0.00001$	$0.0066 \\ 0.0033$	$\frac{246}{246}$
A def	1.0000	1.0000	0.9870	1.0065	0.00000	0.0014	246
A_der A rates	1.0000 $1.0003$	1.0000 $1.0002$	$0.9870 \\ 0.9824$	1.0065 $1.0169$	0.00000 $0.00001$	$0.0014 \\ 0.0034$	$\frac{240}{246}$
$A_{reglq}$	0.9998	1.0000	0.9441	1.0294	0.00003	0.0054	246
A_xslq	0.9995	1.0000	0.9776	1.0071	0.00001	0.0033	246
BBB_def	0.9999	1.0000	0.9952	1.0030	0.00000	0.0009	246
BBB_rates BBB_reglq	$1.0001 \\ 1.0000$	$ \begin{array}{c} 1.0000 \\ 0.9999 \end{array} $	$0.9827 \\ 0.9785$	$1.0273 \\ 1.0248$	$0.00002 \\ 0.00002$	$0.0042 \\ 0.0047$	$\frac{246}{246}$
BBB_xslq	0.9995	1.0000	0.9776	1.0240 $1.0071$	0.00002 $0.00001$	0.0033	$\frac{240}{246}$
BBBm def	1.0000	1.0000	0.9953	1.0029	0.00000	0.0008	246
BBBm_rates	0.9999	1.0000	0.9877	1.0059	0.00000	0.0012	246
BBBm_reglq	0.9993	1.0000	0.9467	$\frac{1.0170}{1.0002}$	0.00003	0.0056	246
BBBm_xslq	0.9996	1.0000	0.9665	1.0092	0.00001	0.0033	246

This table summarizes the observations of intraday data at the close of the trading day 4:15:00ET for 246 trading days during the pandemic (4/2020 - 4/2021). The first column provides the abbreviation for the variable name. The VIX is the CBOE volatility index. This is followed by the prices of 25 REITs with the name a composite made up of the property type (industrial (IN), hotel/lodging (LO), multifamily (MF), mixed use/other (OT), office (OF) and retail (RT)) and the REIT's stock market ticker. Following the REITs are US Treasury yields with ticker representing the 4 maturities of 3 month, 5 year, 10 year and 30 year. The remaining values are the simulated risk partitions indexed in Christopoulos and Jarrow (2018) in cumulative change form. The ticker is a composite of the 4 types of risk partitions default (def), interest rates (rates), liquidity (reglq) and excess liquidity (xslq) combined with the credit rating class names of AAA, AJ, AA, A, BBB and BBB- (BBBm). Each of the columns to the right of the ticker report statistics across all 246 observations.

Opening volatilities for the cumulative changes in proportions of all risk partitions are categorically higher than the closing volatilities for those values. Additionally, looking at the modelled economy, the VIX and interest rates also exhibit categorically higher opening volatility compared with closing volatility. Finally, REITs also exhibit mostly higher volatility at the open than the close, but not categorically with only 18 of the 25 REITs exhibiting higher volatility at the open in the cross-section with and 7 of the 25 exhibiting lower volatility at the open in the cross-section. The differences in magnitude between the theoretical risk partitions and the publicly traded securities and indices are not completely surprising. The risk partition measures represent cumulative changes in proportions from the start of the day. In contrast, the pricing for the publicly traded objects are just prices and not changes of prices. The cross-sectional insights across all intervals and at the open and close give us our third main result: During the pandemic, we find considerably greater volatility in risk partition pricing at the start of each trading day for all risk partitions compared to the end of each trading day. This finding of higher volatility of signals at the open compared with the close prompts further investigation into liquidity across the CMBX and REIT sectors.

### 4.2.3 REIT trading strategies with the Intraday Model

While of similar sizes as noted in <u>Section 9</u>, REIT and CMBX liquidities appear to differ. At a high level, public data from Securities Industry and Financial Markets Association (SIFMA) and NAREIT show that REITs in the aggregate appear to be more liquid than CMBS. <u>Table 16</u> indicates approximately 10x the dollar trading volume for REITs compared with CMBS with 4x the efficiency of turnover rates defined as average daily volume (ADV) divided outstanding issuance.

Table 16: Liquidity summary for several sectors

Sector	ADV (\$bn)	Outstanding (\$bn)	Turnover	Turnover % Tsy
US Tsys	\$565.00	\$19,300.00	2.9275%	100.0000%
US RMBS (Agency)	\$289.80	\$9,900.00	2.9273%	99.9936%
US REITs	\$8.70	\$1,300.00	0.6692%	22.8604%
US Corporates	\$27.46	\$10,600.00	0.2590%	8.8480%
US CMBS	\$0.84	\$596.40	0.1408%	4.8112%

This table provides summary issuance and trading volume for US Treasuries, US Agency backed mortgage backed securities, US REITs, US Corporate Bonds and US CMBS. The columns report the average daily trading volume (ADV) at of Q1 2021 and the outstanding issuance, in Sbillions. The Turnover is the ratio of ADV/Outstanding issuance. The Turnover % of Tsy is the ratio of Turnover/Turnover of US Treasuries. Source: SIFMA and NAREIT

Additionally, as discussed in Section 1.2.1, publicly traded REITs trade on electronic equity exchanges and thus have a similar frequency of price updates as our intraday risk measures. Finally, REITs, like CMBS and CMBX, have similar underlying exposure to commercial real estate risk, and so estimated CMBX risk partitions may carry relevance to REIT pricing in the marketplace. As previously mentioned, CMBX as an OTC product does not trade electronically. That means that the estimated risk partitions in this study update more rapidly than the pricing of actual CMBX securities and the pricing of their underlying CMBS collateral. In earlier studies the CMBX risk partitions gave many profitable insights into the buy/sell decision-making within the CMBX market. In this study, we also find that the risk partitions reveal insights into the related REIT sector intraday, with matching trading frequency.

### 4.2.4 Scope and notation for trading strategies

Note that unlike default, liquidity and excess liquidity partitions, the interest rate risk partition is a bit more difficult to interpret in the trading context with respect to REITs. Higher interest rate risk compensation for higher future rate volatility may affect REITs differently, depending on leverage and asset composition. Thus, to keep things tractable, we focus our trading strategies with REITs to the risk partitions of default, liquidity and excess liquidity. Additionally, to simplify the notation for the trading signals discussed below, for the u-th trading day the risk partition,  $W_{jkut} \equiv y_{jku}(t)$  as defined in Eq. (29) with j risk partitions of k credit rating classes, u trading days and t intraday trading times. Additionally, we are fusing the risk partition W with REITs where  $\iota \in [1, 25]$  is used to represent one of the 25 REITs in our sample.

Trading Signal 1 Let  $\Delta R_{\iota ut}$  be defined as

$$\Delta R_{\iota ut} = \frac{R_{\iota ut}}{R_{\iota t = 4:15:00pm, u - 1}} \tag{30}$$

which represents the proportion of cumulative changes in REIT prices from the close of the prior trading day t = 4:15:00 pm to the time of trade execution for the  $\iota$ -th REIT.

<sup>&</sup>lt;sup>14</sup>For further information see Appendix Section A.1.

With this, we construct the Trading Signal 1,  $L_{ijkut}^1$ , defined as

$$L_{ijkut}^{1} = |\Delta R_{iut} - W_{jkut}| \tag{31}$$

which captures the absolute value of the difference between the observed proportional cumulative change in prices for the  $\iota$ -th REIT,  $\Delta R_{\iota ut}$ , and the cumulative change in prices for one of the risk partitions,  $W_{jkut}$ .<sup>15</sup>

As an absolute value of differences in cumulative changes,  $L_{ijkut}^1$  gives the magnitude of differences. If those differences are influenced by liquidity effects we appear to capture in the cross section, trading opportunities may arise. Eq. (30) does not provide a clear direction for the trading strategy. We borrow from differences between fair value estimates and market prices where large differences may indicate buying opportunities. Large differences necessarily correspond to differences in the theoretical risk measures and perspectives on risk projected by market actors onto market prices. While there is a theoretical basis for long/short trading direction in comparisons between fair value and market prices<sup>16</sup>, the elements  $\Delta R_{tut}$  and  $W_{jkut}$  of Eq. (31) do not carry such ex-ante trade directional indications.

**Trading Signal 2** We address some arbitrariness in Trade Signal 1's lack of direction with our second trading signal:

$$L_{ijkut}^2 = \frac{\Delta R_{iut}}{W_{jkut}} \tag{32}$$

This proportion  $L_{ijkut}^2$  has several interesting interpretations and does provide clear theoretical interpretations with respect to trading direction.

As noted in Christopoulos (2017), both the liquidity and excess liquidity measures have the interpretation of liquidity availability. And thus large values for those risk neutral measures (which are then projected onto market spreads) suggest that compensation in market spreads exceeds (wider than) what is required fair compensation from the perspective of the model technology. In the case of the current technology which does not benefit from

The Recall that  $W_{jkut} \equiv y_{jk}(t)$  as defined in Eq. (29) is a cumulative proportional change in the risk partition, intraday.

<sup>&</sup>lt;sup>16</sup>See, for example, the relative value measure theta defined in Eq. (23) in Christopoulos and Jarrow (2018) where fair value prices greater/less than market prices indicate buy/sell signals, among others.

market prices to project onto, the risk composition estimated reflect cumulative intraday changes in the measure from the opening bell. As such, higher values for cumulative changes intraday in the liquidity and excess liquidity pricing measures, suggest 'cheaper' pricing for the underlying derivatives and potentially a healthier commercial real estate environment. The opposite is true for default risk pricing. There, higher cumulative values for the pricing of default indicates greater default risk while lower cumulative values suggest lower default risk. We capture the interpretation above in the proportional trading signal,  $L_{ijkut}^2$  and summarize below in Table 17 fifteen numerical examples which capture all types of changes in the components of the signal. Although the trading strategy involve the ratio of 1 the statistical analysis shows the mean and median for the ratios to be strongly clustered about 1, thereby justifying this choice.

Table 17: Trade Signal Examples

Ex#	type	$\Delta R$	W	$L = \Delta R/W$	W = XSLQ	W = LQ	W = DEF
1	$\Delta R \uparrow, W \uparrow$	1.250	1.250	1.0000	no trade	no trade	no trade
2	$\Delta R \downarrow, W \downarrow$	0.990	0.990	1.0000	no trade	no trade	no trade
3	$\Delta R \uparrow, W \uparrow$	1.250	1.200	1.0417	sell	$\operatorname{sell}$	buy
4	$\Delta R \downarrow, W \downarrow$	0.990	0.980	1.0102	sell	$\operatorname{sell}$	buy
5	$\Delta R \uparrow, W0$	1.500	1.000	1.5000	sell	$\operatorname{sell}$	buy
6	$\Delta R \uparrow, W \downarrow$	1.200	0.999	1.2012	sell	$\operatorname{sell}$	buy
7	$\Delta R0, W\downarrow$	1.000	0.900	1.1111	sell	$\operatorname{sell}$	buy
8	$\Delta R0, W0$	1.000	1.000	1.0000	no trade	no trade	no trade
9	$\Delta R0, W\uparrow$	1.000	1.500	0.6667	buy	buy	sell
10	$\Delta R \downarrow, W \uparrow$	0.800	1.500	0.5333	buy	buy	sell
11	$\Delta R \downarrow, W0$	0.900	1.000	0.9000	buy	buy	$\operatorname{sell}$
12	$\Delta R \downarrow, W \downarrow$	0.960	0.970	0.9897	buy	buy	sell
13	$\Delta R \uparrow, W \uparrow$	1.020	1.100	0.9273	buy	buy	$\operatorname{sell}$
14	$\Delta R \downarrow, W \downarrow$	0.960	0.960	1.0000	no trade	no trade	no trade
15	$\Delta R \uparrow, W \uparrow$	1.020	1.020	1.0000	no trade	no trade	no trade

This table summarizes the logic underlying the direction (long/buy or short/sell) for Trading Signal 2,  $L^2_{ijkut}$ . The 15 examples show possible trading signal impact, numerically, for different cumulative changes in REIT prices,  $\Delta R$ , and different cumulative changes in the risk partition, W. The rows capture the different examples and the columns the combination of changes (type), the individual changes ( $\Delta R$  and W) the signal  $(L = \Delta R/W)$ , and the different types of risk partition tested in the trading strategies: excess liquidity (W = XSLQ), liquidity (W = LQ), and default (W = DEF). The rowwise indication of 'no trade' indicates that no valid trade signal is observed for L at that time. The indication of 'sell' is a signal to allocate the REIT corresponding to R into the short portfolio, while an indication of 'buy' is a signal to allocate to the REIT correspond to R into the long portfolio.

For liquidity and excess liquidity measures, higher values of  $L_{ijkut}^2 > 1$  correspond to 'sell' signals while lower values of  $L_{ijkut}^2 < 1$  correspond to 'buy' signals. Values of  $L_{ijkut}^2 = 1$  indicate no trade signal. It is important to see that the relative rate of change between the numerator and denominator come into play and the signal picks up these subtleties. For example, consider in <u>Table 17</u> Examples 3 and 13,  $\Delta R \uparrow, W \uparrow$ . Both instances correspond to simultaneous increases in both the numerator and the denominator, indicated by the

upward pointing arrows. In Example 3, the cumulative proportional liquidity measure W is increasing more slowly (1.20) than the cumulative proportional REIT price change  $\Delta R$  (1.25). Since liquidity availability is lagging price increases, the trade signal suggests 'sell' as prices are moving higher than justified relative to the liquidity measure  $(L=1.25/1.20=1.0417>1\rightarrow$  'sell'). In contrast, in Example 13, also  $\Delta R\uparrow,W\uparrow$ , since liquidity (1.10) is increasing more rapidly than the cumulative price increases in the REIT (1.02), the trade signal suggests a buying opportunity  $(L=1.02/1.10=0.9273<1\rightarrow$  'buy'). Finally, while liquidity and excess liquidity availability generate the same directional signalling, the default risk measure generates exactly the opposite signal, because higher default risk decompositions correspond to higher default risk as noted in Christopoulos (2017).<sup>17</sup>

Trading Strategies with Trading Signals 1 and 2 On each day we consider the set of all 25 REITs with the Trading Signals  $L^1_{ijkut}$  and  $L^2_{ijkut}$  for all risk partitions for all credits. We 'buy' securities into the long portfolio and 'sell' securities into the short portfolio. We assume execution at mid-market prices for the REITs when we enter and exit trades and do not, in this initial study, make adjustments for bid/ask spreads of REITs which were not provided. We execute all our trading (long and short positions) at the first trade of the day at approximately t = 9:30:15 am EST. We unwind all positions at end of the day at the close of the day approximately t = 4:15:00pm EST. For all strategies we rank order the REITs based on the values of  $L^1_{ijkut}$  and  $L^2_{ijkut}$  and buy or sell them instantaneously into their respective portfolios at the price which contributes to the signals. In this paper, long and short portfolios are assumed to make price weighted contributions to the long/short portfolio components with the daily returns on long/short components equally weighted.

Trading Strategy 1 For Trading Strategy 1 we use trade signal 1,  $L_{ijkut}^1$ . We consider two alternatives: i.) an even split of 12 long and 12 short positions assumed to make and ii.) a top-3/bottom-3 strategy (close to deciles) with an even split of 3 long and 3 short positions. The selection based on the rank order of the REITs based on the signals assumes that larger differences (greater magnitude) between  $\Delta R_{iut}$  and  $W_{jkut}$  represent buying opportunities

 $<sup>^{17}</sup>$ While we also capture the rates uncertainty partition we do not focus on it in these strategies which is left to future research.

<sup>&</sup>lt;sup>18</sup>On occasion there are small differences of a few seconds due to latency. All trading times are time stamped.

(long portfolio) and smaller differences selling opportunities (short portfolio).

Trading Strategy 2 For Trading Strategy 2 we use  $L^2_{ijkut}$ . We consider the rank order of the REITs based on the signals with interpretations given in <u>Table 17</u>. For liquidity and excess liquidity risk availability portfolios, for those REITs with values of  $L^2_{ijkut} > 1$  we 'sell' those securities in the short portfolio; and for those REITs with values  $L^2_{ijkut} < 1$  we 'buy' those securities into the long portfolio. In the case of the default risk partition portfolio we buy (long) REITs with values of  $L^2_{ijkut} < 1$  and sell (short) REITs with values of  $L^2_{ijkut} > 1$ . Values of  $L^2_{ijkut} = 1$  indicate no trade signal in all cases.

It is certainly the case in this strategy that on any given day we may be 100% directionally long or short, but we are never more than 50% weighted long/short. In the instances where 100% of the values  $L_{ijkut}^2$  are in the same direction (Eg. all > 1 or all < 1), then the corresponding portfolio is allocated 50% to the direction given by the uniform signal on that day and 50% into cash (0% Return). For example, if all 25 REITs had a buy-signal based on  $L_{ijkut}^2$  then all 25 would be purchased into the long position. The return for the day would be calculated based on the change in value between 9:30:15am (when they were purchased) and 4:15:00pm (when they were sold). However, in such cases 50% of the portfolio is said to have been moved to cash with assumed 0% return for that day. On all other days, when the signals are mixed 50% of the returns are generated by the long leg of the portfolio and 50% are generated by the short leg of the portfolio, regardless of how many signals indicate long and short on such date. The risk management of the portfolio is enforced in cases where only one direction is signalled, with a 50% allocation to cash imposed. Additionally, the time horizon of mandatory unwind of all positions by the end of the day ensures that each portfolio horizon is only one trading session. The obvious artifice is the forcing trades to close at the end of the day instead exploiting the intraday changes observable in Figures 5, 6, 7 and 8. Investigation of such tactical intraday exploitation of CMBX risk partition pricing is outside the scope of this paper and left to future work.

### 4.2.5 Results from Trading Strategies 1 and 2

The trading strategies were implemented for excess liquidity, liquidity and default risk measures for all ratings classes summarized in Table 18. The best results were found with the

excess liquidity risk strategy returns of 48.74% for AAA using L1 1010 (Panel A). The worst result was -50.13% 12-month returns for A using L2 (Panel D). Sharpe ratios,  $H_{\omega}$ , for the  $\omega$ -th different trading strategies<sup>19</sup> with  $\omega \in [1, 54]$  trading strategies were calculated as

$$H_{\omega} = \frac{R_{\omega} - R_{\lambda}}{\sigma_{\omega} \times \sqrt{240}} \tag{33}$$

The square root of the 240 trading days is the required adjustment for daily standard deviations for 240 trading days in our sample period. The cumulative return for the specific day trading strategy is denoted,  $R_{\omega}$ , while  $R_{\lambda}$  is the cumulative return for the long-only portfolio. The long-only portfolio, like the day trading strategies, is also a day traded portfolio executed with buys and sells contemporaneous with the long/short portfolio. The standard deviation of the daily returns for the day trading strategy portfolio is denoted as  $\sigma_{\omega}$ .

The long-only portfolio has 100% allocation to the entire set of REITs in our sample, bought at 9:30am and sold at 4:00pm on each trading day. The return on the long-only portfolio over the sample period was -14.97%. For portfolios with positive returns, the portfolio Sharpe ratios were quite strong with values ranging from 0.98 to 5.09. In general, the Sharpe ratios for the L2 strategies were higher than either of the L1 strategies. Concentrating on L2 trading signals for the 24 REIT relative value strategies (4 per credit rating class), for excess liquidity and liquidity trading we see categorically positive returns ranging from 9.09% to 41.37% for all credit rating classes. Interestingly for the default pricing driven signals, positive returns of 11.08% and 17.08% are captured only for the AAA and AJ classes, respectively. Additionally, the only credit rating class to exhibit positive market risk signal (rates) with respect to REIT relative value is AAA (15.69%). These findings suggest that the L2 liquidity and excess liquidity trading signals with respect to REIT relative value provide more consistent and positive insights for this exercise. <sup>20</sup>

<sup>&</sup>lt;sup>19</sup>See Sharpe (1994).

 $<sup>^{20}</sup>$ Tables of all trades for all trading strategies are available upon request.

Table 18: Cumulative returns for Trading Strategies 1 and 2

Panel A: AAA	L1 5050	L1 1010	L2	Panel B: AJ	L1 5050	L1 1010	L2
XSLiquidity stdev port Sharpe Ratio	$\begin{array}{c} 19.21\% \\ 0.61\% \\ 3.61 \end{array}$	$48.74\% \\ 1.18\% \\ 3.50$	$9.09\% \ 0.78\% \ 1.99$	XSLiquidity stdev port Sharpe Ratio	$-8.22\% \ 0.63\% \ 0.69$	$^{-12.47\%}_{1.26\%}_{0.13}$	$\begin{array}{c} 41.37\% \\ 0.71\% \\ 5.09 \end{array}$
Liquidity stdev port Sharpe Ratio	$2.02\% \ 0.62\% \ 1.77$	$-5.63\% \ 1.11\% \ 0.54$	37.69% $1.09%$ $3.12$	Liquidity stdev port Sharpe Ratio	$\begin{array}{c} 6.80\% \\ 0.63\% \\ 2.24 \end{array}$	$16.93\% \ 1.23\% \ 1.67$	22.80% $1.09%$ $2.23$
Default stdev port Sharpe Ratio	-3.52% 0.63% 1.17	-18.21% 1.20% -0.17	$\begin{array}{c} 11.08\% \\ 0.80\% \\ 2.11 \end{array}$	Default stdev port Sharpe Ratio	1.53% 0.64% 1.66	-8.01% $1.28%$ $0.35$	17.08% 0.72% 2.87
Panel C: AA	L1 5050	L1 1010	L2	Panel D: A	L1 5050	L1 1010	L2
XSLiquidity stdev port Sharpe Ratio	$0.73\% \ 0.62\% \ 1.64$	-5.79% $1.22%$ $0.48$	$37.62\% \ 0.78\% \ 4.37$	XSLiquidity stdev port Sharpe Ratio	$0.73\% \ 0.62\% \ 1.64$	-5.79% $1.22%$ $0.48$	$37.62\% \ 0.78\% \ 4.37$
Liquidity stdev port Sharpe Ratio	$5.55\% \ 0.64\% \ 2.09$	$3.58\% \\ 1.22\% \\ 0.98$	$\begin{array}{c} 14.34\% \\ 0.74\% \\ 2.57 \end{array}$	Liquidity stdev port Sharpe Ratio	$\begin{array}{c} 7.14\% \\ 0.64\% \\ 2.24 \end{array}$	$\begin{array}{c} 19.81\% \\ 1.20\% \\ 1.88 \end{array}$	$34.89\% \ 0.75\% \ 4.30$
Default stdev port Sharpe Ratio	1.09% 0.63% 1.64	-0.09% $1.23%$ $0.78$	-5.23% 0.79% 0.80	Default stdev port Sharpe Ratio	$\begin{array}{c} 12.38\% \\ 0.62\% \\ 2.86 \end{array}$	6.23% 1.24% 1.10	-13.02% 0.73% 0.17
Panel E: BBB	L1 5050	L1 1010	L2	Panel F: BBB-	L1 5050	L1 1010	L2
XSLiquidity stdev port Sharpe Ratio	$0.73\% \ 0.62\% \ 1.64$	-5.79% $1.22%$ $0.48$	$37.62\% \ 0.78\% \ 4.37$	XSLiquidity stdev port Sharpe Ratio	$\begin{array}{c} 11.00\% \\ 0.61\% \\ 2.75 \end{array}$	$\begin{array}{c} 18.50\% \\ 0.97\% \\ 2.23 \end{array}$	$15.09\% \ 0.76\% \ 2.57$
Liquidity stdev port Sharpe Ratio	$\begin{array}{c} 4.32\% \\ 0.64\% \\ 1.95 \end{array}$	-2.47% $1.23%$ $0.66$	$39.95\% \ 0.77\% \ 4.63$	Liquidity stdev port Sharpe Ratio	$\begin{array}{c} -0.01\% \\ 0.63\% \\ 1.53 \end{array}$	-1.59% $1.25%$ $0.69$	21.03% $0.72%$ $3.24$
Default stdev port Sharpe Ratio	16.12% 0.61% 3.27	13.10% $1.24%$ $1.47$	-34.67% 0.84% -1.52	Default stdev port Sharpe Ratio	$6.23\% \ 0.64\% \ 2.14$	11.98% $1.20%$ $1.44$	-32.53% 0.86% -1.31

This table provides the cumulative returns over 240 consecutive trading days over the sample period for Trading Strategies 1 and 2 using the four different risk partitions of default, liquidity and excess liquidity as embedded within Eqs. (31 and 32). The columns show results for Trading Strategy 1 for upper and lower deciles (L1 1010), and Trading Strategy 2. Each of the rows within the Panels A thru E show the returns for the risk partitions in the order Excess (XS) Liquidity, Liquidity, and Default with the standard deviation for the portfolio and the Sharpe Ratio for the portfolio.\*\*\*/\*\*/\*/ correspond to 0.1%, 1%, 5% and 10% levels of significance. Panel A, shows the results for AAA, Panel B shows the results for AJ, Panel C shows the results for AA, Panel D shows the results for A, Panel E shows the results for BBB and Panel F shows the results for BBB.

#### 4.2.6 ICAPM

To test for skill in the trading strategies we use the ICAPM of Merton (1990). We choose this approach as a standard approach for equity asset pricing tests of skills. An alternative approach was introduced by Acharya and Pedersen (2005) which includes the Amihud (2002) ILLIQ measure. However, ILLIQ is dependent on observed volumes. Since no observed volumes were provided for CMBX, ILLIQ cannot be implemented as an ICAPM factor in this study. However, the key findings of Acharya and Pedersen (2005) concerning flight to liquidity do appear to be confirmed in this study, in particular in our trading strategies that exploit the estimated reduced form measures of liquidity and excess liquidity.

Following Christopoulos and Jarrow (2018) the final regression model to test for abnormal returns in our trading strategies is given by:

$$R_{\omega u} - R_{\lambda u} = \alpha + \sum_{i=2}^{M} \beta_{\omega i} (R_{iu} - r_u) + \varepsilon_u$$
(34)

with  $u \in [1, 240]$  trading days,  $R_{\omega u}$  the daily returns of the trading strategy portfolio,  $R_{\lambda u}$  the returns of the long-only trading portfolio,  $R_{iu}$  the *i*-th portfolio equity risk factor, and  $r_u$  the risk-free rate. Positive and significant  $\alpha$  implies these trading strategies generate abnormal returns. We use the standard risk factors to evaluate equity based trading strategies introduced in Fama and French (1993) including: (i) the market portfolio, (ii) the SMB equity index, and (iii) the HML index as well as the MOM risk factor introduced in Carhart (1997). We test 54 different trading strategies with results summarized in <u>Table 19</u>. For each of the six credit rating classes we conduct nine daily trading strategies across 240 trading dates from u = 4/8/2020 thru u = 3/31/2021. Trading Strategy 1 implements 50th percentile ('5050') and decile ('1010') variations.

The results are quite strong. All strategies were statistically significant overall based on the F-test. Adjusted R-squared values ranged from 0.1885 to 0.5052. All strategies produced positive  $\alpha's$ . 52 of the 54 total trading strategies (96.30%) produced statistically significant  $\alpha's$  ranging from 0.001 to 0.100 levels significance, with 35 of 54 (64.81%) producing statistically significant  $\alpha's$  ranging from 0.001 to 0.010. In all strategies the market portfolio was statistically significant at the 0.001 level and negative. The MOM risk factor was generally insignificant and varied in sign. SMB varied in sign and shown to be insignificant across all strategies. HML was categorically negative exhibiting statistical significance ranging from 0.001 to 0.010. In the aggregate 65.38% of the statistically significant  $\alpha$  strategies (34/52) also exhibited positive abnormal returns.

Table 19: ICAPM Results

Panel A, AAA	α	Mkt-Rf	MOM	SMB	HML	F	Adj-Rsq	N
L1 XS 5050	0.0021865**	-0.007037***	-0.001197	0.0003331	-0.0053299***	50.4	0.4376	240
L1_A5_0000	0.0008302	0.0007039	0.0001157 $0.0008252$	0.0010443	0.0011298	0.00	0.4010	240
L1_XS_1010	0.0040237*	-0.014177***	-0.0022281	0.0006341	-0.0100508***	47.44	0.3746	240
	(0.0016415)	(0.0013917)	(0.0016317)	(0.0020649)	(0.0022338)	0.00		
$L1\_Lq\_5050$	0.0037889*	-0.0114627***	-0.0008965	-0.0012026	-0.0078067***	38.66	0.3187	240
T1 T 1010	(0.0015924)	(0.0013502)	(0.0015829)	(0.0020032)	(0.0021671)	0.00	0.100	0.40
L1_Lq_1010	0.0029496.	-0.0107726***	-0.002226	-0.0008903	-0.0092229***	29.54	0.1885	240
L1 Def 5050	$(0.0017257) \ 0.004655**$	(0.0014632) -0.013347***	(0.0017155) $-0.001268$	(0.0021709) -0.000568	(0.0023485) -0.008402***	$0.00 \\ 48.62$	0.4092	240
L1_De1_5050	(0.001554)	(0.001318)	(0.001545)	(0.001955)	(0.002115)	0.00	0.4032	240
L1 Def 1010	0.0055647***	-0.0113874***	-0.0005711	-0.0013482	-0.0082612***	40.18	0.3037	240
	(0.0016388)	(0.0013895)	(0.0016291)	(0.0020616)	(0.0022302)	0.00		
$L2\_XS$	0.004437**	-0.011797** <sup>*</sup>	-0.001651	-0.00105	-0.008825** <sup>*</sup>	39.87	0.3187	240
	(0.001599)	(0.001355)	(0.001589)	(0.002011)	(0.002176)	0.00		
$L2\_Lq$	0.0038399*	-0.0137208***	-0.0012093	0.0007149	-0.0092415***	54.21	0.476	240
TO D 4	(0.0015339)	(0.0013006)	(0.0015248)	(0.0019296)	(0.0020874)	0.00	0.4404	0.40
L2_Def	0.003991*	-0.015079***	-0.001129	0.00106	-0.009997***	52.45	0.4191	240
	(0.001714)	(0.001454)	(0.001704)	(0.002157)	(0.002333)	0.00		
Panel B, AJ	$\alpha$	Mkt-Rf	MOM	SMB	$_{ m HML}$	F	Adj- $Rsq$	N
L1_XS_5050	0.0043294**	-0.0130814***	-0.0016926	0.0004567	-0.009509***	54.74	0.4741	240
	(0.0014628)	(0.0012403)	(0.0014541)	(0.0018402)	(0.0019907)	0.00		-
L1_XS_1010	0.005038**	-0.014427***	-0.001551	0.001179	-0.010328** <sup>*</sup>	55.11	0.4243	240
	(0.00161)	(0.001365)	(0.0016)	(0.002025)	(0.00219)	0.00		
$L1\_Lq\_5050$	0.0038897*	-0.0115571***	-0.0019515	-0.0005213	-0.0094571***	42.6	0.3557	240
T 1 T 1010	(0.0015353)	(0.0013017)	(0.0015261)	(0.0019313)	(0.0020892)	0.00	0.0000	0.40
L1_Lq_1010	0.0033418* (0.0016865)	-0.0117045*** (0.0014299)	-0.0031924.	0.0003376	-0.0109727*** (0.0022951)	$34.93 \\ 0.00$	0.2388	240
L1 Def 5050	0.0057627***	-0.0123883***	(0.0016765) $-0.0015501$	(0.0021216) $-0.0006195$	-0.00886***	43.27	0.3616	240
L1_De1_5050	(0.0037027 $(0.0015814)$	(0.0013408)	(0.0015719)	(0.0019893)	(0.002152)	0.00	0.5010	240
L1_Def_1010	0.004989**	-0.012098***	-0.001468	-0.0015334	-0.009482***	41.29	0.3222	240
	(0.001688)	(0.001431)	(0.001678)	(0.002124)	(0.002297)	0.00	0.0===	
$L2\_XS$	0.004683**	-0.011807***	-0.002287	-0.001453	-0.009541* <sup>*</sup> *	41.04	0.3391	240
	(0.001586)	(0.001345)	(0.001576)	(0.001995)	(0.002158)	0.00		
$L2\_Lq$	0.004194**	-0.01331***	-0.0009555	0.00002154	-0.008433***	53.18	0.4646	240
	(0.0015)	(0.001272)	(0.001491)	(0.001887)	(0.002041)	0.00		
L2_Def	0.004079*	-0.01402***	-0.001466	-0.00004531	-0.008893***	45.21	0.3462	240
	(0.00167)	(0.001416)	(0.00166)	(0.002101)	(0.002273)	0.00		
Panel C, AA	$\alpha$	Mkt-Rf	MOM	SMB	$_{ m HML}$	F	Adj- $Rsq$	N
L1 XS 5050	0.004027*	-0.0116518***	-0.0023509	-0.0008969	-0.0094466***	38.3	0.3151	240
11_110_0000	(0.001595)	(0.0013524)	(0.0015855)	(0.0020065)	(0.0021706)	0.00	0.0101	210
L1_XS_1010	0.004226*	-0.012386***	-0.002168	-0.001093	-0.010095***	34.81	0.2644	240
	(0.001826)	(0.001548)	(0.001815)	(0.002296)	(0.002484)	0.00		
L1_Lq_5050	0.0041002**	-0.0123558***	-0.0013576	-0.0005149	-0.0087784***	50.84	0.4356	240
	(0.0014657)	(0.0012427)	(0.0014569)	(0.0018438)	(0.0019946)	0.00		
L1_Lq_1010	0.0040813**	-0.0131186***	-0.0019544	-0.0001837	-0.0093178***	47.89	0.3429	240
I 1 Def FOTO	(0.0015437)	(0.0013088)	(0.0015345)	(0.0019419)	(0.0021007)	0.00	0.2001	240
L1_Def_5050	0.005408*** (0.0015995)	-0.0117627*** (0.0013561)	-0.0017786 (0.0015899)	-0.0001356 (0.0020121)	-0.0089674*** (0.0021766)	$38.24 \\ 0.00$	0.3021	240
L1 Def 1010	0.0015995)	(0.0013561) -0.011206***	(0.0015899)	-0.002266	-0.008399***	41.16	0.3384	240
P1_D61_1010	(0.001572)	(0.001333)	(0.001249)	(0.001978)	(0.002139)	0.00	0.5564	240
L2 XS	0.0038622*	-0.0125738***	-0.0021869	-0.0009717	-0.0098577***	41.67	0.3486	240
	(0.0016568)	(0.0014047)	(0.0016469)	(0.0020842)	(0.0022547)	0.00	0.0100	- 10
$L2\_Lq$	0.004194**	-0.01331***	-0.0009555	0.00002154	-0.008433***	53.18	0.4646	240
_	(0.0015)	(0.001272)	(0.001491)	(0.001887)	(0.002041)	0.00		
$L2\_Def$	0.004079*	-0.01402***	-0.001466	-0.00004531	-0.008893***	45.21	0.3462	240
	(0.00167)	(0.001416)	(0.00166)	(0.002101)	(0.002273)	0.00		

Panel D, A	α	Mkt-Rf	MOM	SMB	HML	F	Adj-Rsq	N
L1_XS_5050	0.0042909**	-0.0125106***	-0.0016312	-0.0002349	-0.0094443***	46.2	0.3982	240
L1_XS_1010	$(0.0015688) \\ 0.004902**$	(0.0013301) -0.012716***	(0.0015594) $-0.0009979$	(0.0019735) $-0.0001228$	(0.0021348) -0.0091501***	$0.00 \\ 39.08$	0.3026	240
L1_X5_1010	(0.0017638)	(0.0014954)	(0.0017532)	(0.0022188)	(0.0024002)	0.00	0.3026	240
L1_Lq_5050	0.00454**	-0.012023***	-0.001855	-0.001405	-0.00898***	47.11	0.4028	240
1	(0.001491)	(0.001264)	(0.001482)	(0.001876)	(0.002029)	0.00	0.1000	
L1_Lq_1010	0.004231**	-0.012184***	-0.002705.	-0.00114	-0.009916***	41.87	0.2924	240
I 1 D 6 7070	(0.00158)	(0.00134)	(0.001571)	(0.001988)	(0.002151)	0.00	0.0001	0.40
L1_Def_5050	0.005408*** (0.0015995)	-0.0117627*** (0.0013561)	-0.0017786 (0.0015899)	-0.0001356 (0.0020121)	-0.0089674*** (0.0021766)	$38.24 \\ 0.00$	0.3021	240
L1_Def_1010	0.005718***	-0.013031***	-0.002128	-0.001359	-0.010209***	47.62	0.4112	240
21_201_1010	(0.00163)	(0.001382)	(0.00162)	(0.00205)	(0.002218)	0.00	0.1112	- 10
$L2\_XS$	0.003497*	-0.012009* <sup>*</sup> *	-0.002309	-0.001462	-0.010016***	42.67	0.3593	240
T 0 T	(0.00161)	(0.001365)	(0.0016)	(0.002025)	(0.002191)	0.00	0.4040	2.40
$L2\_Lq$	0.004194**	-0.01331***	-0.0009555	0.00002154	-0.008433***	53.18	0.4646	240
L2 Def	$(0.0015) \\ 0.004079*$	(0.001272) -0.01402***	(0.001491) -0.001466	(0.001887) -0.00004531	(0.002041) -0.008893***	$0.00 \\ 45.21$	0.3462	240
LZ_Dei	(0.00167)	(0.001416)	(0.00166)	(0.002101)	(0.002273)	0.00	0.5402	240
D I E DDD	,			SMB		F	A.I. D	
Panel E, BBB	α	Mkt-Rf	MOM		HML		Adj-Rsq	
L1_XS_5050	0.0038162*	-0.0117119***	-0.0024842	0.0005267	-0.0100017***	35.93	0.2936	240
L1 XS 1010	$(0.0016434) \\ 0.003713*$	(0.0013934) -0.0120828***	(0.0016336) -0.002494	(0.0020674) $0.0006448$	(0.0022365) -0.0109529***	$0.00 \\ 31.68$	0.2385	240
L1_A5_1010	(0.003713	(0.0015908)	(0.0018651)	(0.0023603)	(0.0025533)	0.00	0.2369	240
L1 Lq 5050	0.004766**	-0.012471***	-0.00194	-0.001338	-0.00944***	50.23	0.4355	240
_ 1	(0.001503)	(0.001274)	(0.001494)	(0.00189)	(0.002045)	0.00		
L1_Lq_1010	0.0046653**	-0.0129274***	-0.0025898	-0.0009711	-0.0099328***	42.18	0.3085	240
I I D C FOFO	(0.0016414)	(0.0013917)	(0.0016316)	(0.0020649)	(0.0022337)	0.00	0.0001	0.40
L1_Def_5050	0.005408*** (0.0015995)	-0.0117627*** (0.0013561)	-0.0017786 (0.0015899)	-0.0001356	-0.0089674*** (0.0021766)	$38.24 \\ 0.00$	0.3021	240
L1 Def 1010	0.00561***	-0.011541***	-0.0013899)	(0.0020121) $-0.001621$	-0.0021700)	44.03	0.3589	240
L1_DC1_1010	(0.001526)	(0.001294)	(0.001517)	(0.001021	(0.002077)	0.00	0.0000	240
$L2\_XS$	0.0025332	-0.0120336***	-0.0023626	-0.0006994	-0.0098406***	38.99	0.3121	240
	(0.0016395)	(0.0013901)	(0.0016297)	(0.0020625)	(0.0022311)	0.00		
$L2\_Lq$	0.004575**	-0.0128342***	-0.0006617	-0.0003317	-0.0079207***	52.7	0.459	240
L2 Def	$(0.0014701) \ 0.005056**$	(0.0012464) -0.0134311***	(0.0014613) $-0.0003629$	(0.0018493) $-0.0002725$	(0.0020005) -0.0077591***	$0.00 \\ 51.39$	0.4141	240
L2_Dei	(0.0015477)	(0.0013123)	(0.0015385)	(0.001947)	(0.0021063)	0.00	0.4141	240
			,					
Panel F, BBB-	α	Mkt-Rf	MOM	SMB	HML	F	Adj-Rsq	N
L1_XS_5050	0.004217**	-0.013495***	-0.001041	0.000192	-0.008697***	58.21	0.5052	240
* . ***	(0.001453)	(0.001232)	(0.001444)	(0.001828)	(0.001977)	0.00		
L1_XS_1010	0.004322**	-0.015282***	-0.001788	0.001642	-0.009734***	56.21	0.4296	240
L1_Lq_5050	$(0.00158) \\ 0.004165**$	(0.00134) -0.011688***	(0.001571) $-0.001834$	(0.001988) $-0.001053$	(0.00215) $-0.009192***$	$0.00 \\ 40.45$	0.3382	240
L1_Lq_5050	(0.001591)	(0.001349)	(0.001582)	(0.002002)	(0.002166)	0.00	0.5502	240
L1_Lq_1010	0.0043642*	-0.0116363***	-0.0019992	-0.0008662	-0.0091518***	33.42	0.2301	240
-	(0.0017165)	(0.0014554)	(0.0017063)	(0.0021593)	(0.0023359)	0.00		
$L1\_Def\_5050$	0.0044753**	-0.0118264***	-0.0023004	-0.0003724	-0.0100502***	42.17	0.3458	240
I 1 Def 1010	(0.0015752) $0.0048238**$	(0.0013356)	(0.0015658)	(0.0019816)	(0.0021436)	$0.00 \\ 42.97$	0.2506	240
L1_Def_1010	$(0.0048238^{***})$	-0.0124841*** (0.0013405)	-0.00216 (0.0015716)	-0.0006673 (0.0019889)	-0.0094188*** (0.0021515)	$\frac{42.97}{0.00}$	0.3586	240
L2 XS	0.002663	-0.012487***	-0.003047.	-0.001407	-0.010772***	40.39	0.3351	240
_	(0.001682)	(0.001426)	(0.001672)	(0.002116)	(0.002289)	0.00		
$L2\_Lq$	0.0066207**	-0.0180265***	-0.0027309	-0.0004056	-0.0140932***	46.3	0.4231	240
	(0.0022618)	(0.0019177)	(0.0022483)	(0.0028453)	(0.003078)	0.00	0.8016	0.40
L2_Def	0.0078028*** (0.0023297)	-0.0181336*** (0.0019753)	-0.0023276 $(0.0023158)$	-0.0000474 $(0.0029307)$	-0.0137304*** (0.0031704)	$43.97 \\ 0.00$	0.3912	240
	(0.0023231)	(0.0019193)	(0.0023136)	(0.0029301)	(0.0031704)	0.00		

This table provides the results the ICAPM regressions of Merton (1990) with the four factors introduced by Fama and French (1993) (the market portfolio (Mkt-Rf), high minus low (HML), and small minus big (SMB) and the fourth factor of momentum (MOM) introduced by Carhart (1997). The form of the regression is  $R_{\omega u} - R_{\lambda u} = \alpha + \sum_{i=2}^{M} \beta_{\omega i} (R_{iu} - r_u) + \varepsilon_u$  with the difference between the trading strategy portfolio minus the long only portfolio as the dependent variable, and the four factors as independent variables. Nine strategies are tested for each credit rating class captured in the panels. Each panel presents excess liquidity (XS) for the L1 5050 and L1 1010 strategies, Liquidity for the L1 5050 and L1 1010 strategies, and Default for the L1 5050 and L1 1010 strategies. These are followed by the three L2 strategies for Excess Liquidity (L2 LOS), Liquidity (L2 LO2) and Default (L2 Def). The columns correspond to intercent alpha and each of the explanatory factors. The final three columns Liquidity (L2\_LQ) and Default (L2\_Def). The columns correspond to intercept alpha and each of the explanatory factors. The final three columns show the F-test value, the Adjusted R-squared value and the number of observations. The estimates, the F-test value, the Adjusted R-squared value and number of observations are in the row labelled with the trading strategy. The standard error of the estimates (in parentheses) are shown in the row immediately below the estimates and the p-value for the F-test immediately below the F-test statistics. Panel A, shows the results for AAA, Panel B shows the results for AJ, Panel C shows the results for AA, Panel D shows the results for A, Panel E shows the results for BBB and Panel F shows the results for BBB-.

## 4.2.7 Analysis of results

Recall of 54 total strategies, 36 were L1 and 18 were L2. Of the 36 L1 strategies, all exhibited statistically significant  $\alpha's$  (100.00%). Of the 18 L2 strategies, 16 exhibited statistically significant  $\alpha's$  (88.89%). Interestingly for the L1 strategies, it was not categorically the case that the 1010 sub-strategies (deciles) demonstrated higher statistical significance with respect to  $\alpha's$  than their corresponding 5050 strategies.

To get a better sense of the relative performance of L1 compared with L2 strategies, in Figure 9 we show the portfolio returns in Table 18 with their corresponding  $\alpha's$  significance from in Table 19. Figure 9 depicts the 52 strategies that had statistically significant and positive  $\alpha's$ . The x-axis indicates the standard statistical significance groupings of 0.001, 0.010, 0.050 and 0.100. The y-axis indicates the 12-month cumulative return earned by the strategy. From left to right, Panel 1 shows the statistically significant  $\alpha$  returns for the L1 and L2 strategies. Panel 2 shows the statistically significant  $\alpha$  returns for the L1 strategies, while Panel 3 shows the statistical significant  $\alpha$  returns for the L2 strategies. Of the significant L1 strategies, 22 of 36 showed positive returns (66.7%). In contrast, of the 16 significant L2 strategies depicted 12 showed positive returns (75.0%).

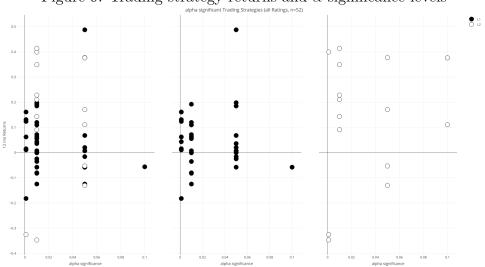


Figure 9: Trading strategy returns and  $\alpha$  significance levels

This figure depicts the 52 (out of 54 total) trading strategy returns that statistically significant and positive  $\alpha'$ s showing their  $\alpha$  significance and the returns for those those strategies. The x-axes show  $\alpha$  significance levels and the y-axes show the cumulative returns over the sample period. The black dots correspond to L1 strategies, while the white dots correspond to L2 strategies.

This comparatively greater proportion of positive returns coupled with positive and sig-

nificant  $\alpha$  is echoed when we break down returns by credit rating class as seen in Figure 10.

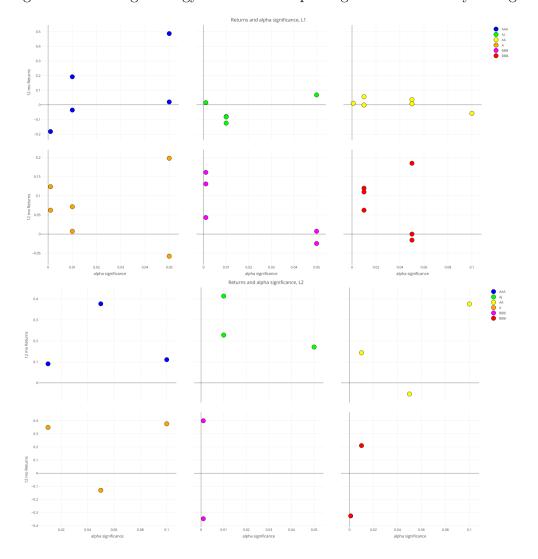


Figure 10: Trading strategy returns and alpha significance levels by ratings

This figure depicts the 52 (out of 54 total) trading strategy returns with statistically significant and positive  $\alpha'$ s showing their  $\alpha$  significance and the returns for those those strategies, broken out by credit rating class. The x-axes show  $\alpha$  significance levels and the y-axes show the cumulative returns over the sample period. The top panel of 6 sub charts capture the 36 results for the L1 trading strategies, while the bottom panel of 6 subcharts capture the 16 results for the L2 trading strategies. The credit ratings begin with AAA in the upper left corner and descend rowwise from left to right ending with BBB- in the bottom right corner.

The plots are read from left to right by descending credit rating class beginning with AAA (blue) in the top left and BBB- (red) in the bottom right. The top chart of 6 panels depict the statistically significant  $\alpha$  L1 trading strategies. The bottom chart of 6 panels depicts the statistically significant L2 trading strategies. L2 strategies for the higher credits generally outperform with respect to returns at higher  $\alpha$  significance levels for AAA, AJ, AA, and A classes. For BBB and BBB- classes, L1 appears to relatively outperform L2 in the REIT

strategies tested. Across all strategies and credits, the L2 strategies for the AJ class (green) appear to perform best while L1 strategies, also for AJ class, appear to perform worst. Additionally, L1 shows a proportionately larger number of statistically significant strategies driven by BBB and BBB- classes than L2 which relatively dominates on a proportional basis within the higher credit classes. This capital structure differences are consistent with the earlier literature<sup>21</sup> that finds idiosyncratic risk of collateral in CMBX is comparatively more important for lower credit rated tranches than higher rated tranches. Interestingly, as noted in An, Deng, Nichols and Sanders (2015) the pricing of credit risk alone is insufficient to explain subordination impact on pricing. As such, the logic underlying L2 trading strategies, previously discussed and summarized in Table 17, may be somewhat obscured for BBB and BBB- classes. While the  $W_{jkut}$  values in Eq. (32) signals are picking up risk tranching effects, and are differentiating across different types of risks, they nevertheless are not directly pricing the idiosyncratic risks of CMBX collateral with reduced form simulation and current data as shown in Christopoulos (2017) and Christopoulos and Jarrow (2018). This is a limitation to be explored in future work where computational costs and data are made available.

Table 20: Summary of L1 and L2 ICAPM strategies (all ratings)

							٠ ,		*	
Panel A: L2	>=0	<0	significant	insignificant	all	% >= & significant	avg return	median ret	min ret	max ret
XS	4	0	4	2	6	100%	31.43%	37.62%	9.09%	41.37%
$_{ m Lq}$	6	0	6	0	6	100%	28.45%	28.85%	14.34%	39.95%
Def	2	4	6	0	6	33%	-9.56%	-9.16%	-34.67%	17.08%
Panel B: L1 1010	>=0	<0	significant	insignificant	all	% >= & significant	avg return	median ret	min ret	max ret
XS	2	4	6	0	6	33%	6.23%	-5.79%	-12.47%	48.74%
$_{ m Lq}$	2	4	6	0	6	33%	0.21%	-2.03%	-12.47%	19.81%
Def	3	3	6	0	6	50%	0.83%	3.07%	-18.21%	13.10%
Panel C: L1 5050	>=0	<0	significant	insignificant	all	% >= & significant	avg return	median ret	min ret	max ret
XS	5	1	6	0	6	83%	4.03%	0.73%	-8.22%	19.21%
$_{ m Lq}$	5	1	6	0	6	83%	4.30%	4.94%	-0.01%	7.14%
Def	5	1	6	0	6	83%	5.64%	3.88%	-3.52%	16.12%
						- 370	- > - / 0		. , _ , 0	

This table summarize depicts L1 and L2 ICAPM strategies for all ratings. Each of the rows in the panel capture risk partitions of excess liquidity (XS), liquidity (Lq) and default (Def). The columns provide the counts of those strategies with non-negative returns (>=0), negative returns (<0), number of significant, insignificant, and all. Then the percentage of non-negative with significant alpha strategies are calculated for the risk partition as well as the average, median, minimum (min), and maximum (max) returns. Panel A summarizes for the L2 strategies. Panel B summarizes for the L1 1010 strategies. Panel C summarizes for the L1 5050 strategies.

Finally we compress the ICAPM significant trading strategies across all ratings in <u>Table 20</u>. There again we observe the L2 strategies outperforming the L1 1010 and L1 5050 strategies in excess liquidity and liquidity strategies compared with default. Across all ratings 100% of significant excess liquidity and liquidity strategies for L2 also exhibited positive

 $<sup>^{21}\</sup>mathrm{See}$  for example Riddiough and Zhu (2016), among others.

returns ranging from 9.09% to 41.37% for excess liquidity and 14.34% to 39.95% for liquidity strategies. In contrast, the default strategies for L2 were positive in only 33% of the cases ranging from -34.67% to 17.08%. In the case of the L1 strategies, the 1010 decile strategies performed somewhat comparatively worse than the 5050 strategies overall with 33% to 50% of the strategies positive and significant for the 1010 decile strategies compared with 83% for the 5050. The returns statistics for 5050 strategies compared with 1010 strategies were generally better overall.

CMBX liquidity and excess liquidity risk pricing by definition, as discussed in Christopoulos (2017) and Christopoulos and Jarrow (2018), provide insights into sentiments of CMBX pricing risks apart from idiosyncratic risks associated with CMBX collateral pools. This is because CMBX risk pricing of liquidity and excess liquidity are residual measures apart from explicitly modelled risks of default, loss and interest rate volatility at the loan level, aggregated to the bond level using fair value techniques. Liquidity and excess liquidity risk pricing provides insights into investor sentiment of risk apart from rate volatility and default experiences as captured in the loan level historical state transitions as discussed in Christopoulos and Barratt (2016). In this sense, at the securities level following fair value aggregation, the liquidity and excess liquidity measures articulate investor sentiment of real estate securities more broadly than the historical analysis of default and rates and their relationship in current CMBX collateral vis a vis simulation. As such, the positive and significant performance for REIT trading strategies using excess liquidity and liquidity CMBX measures makes sense, particularly for the L2 strategies.

As shown in the cross-sectional analysis, we find considerably greater volatility in risk partition pricing at the start of each trading day for all risk partitions compared to the end of each trading day, which contrast with the much more muted volatility for REITs from the start to end of the trading day. This suggests that the monthly and daily analysis supporting insights provided by the theoretical liquidity risk partitions persist at the intraday level (our third main result). The success of the trade strategies and their significance confirm that the insights of CMBX risk partitions bring valuable insights to the related REIT sector, our fourth main result. This expands the application of CMBX risk partitions, intraday, to a broader array of commercial real estate securities. Together these main and supporting results completes the validation of the Intraday Model.

# 5 Summary

All markets move, but some sectors move more rapidly than others. This is true with respect to observable differences in the frequency and volume of trading across products. It is also true with respect to observable differences in the rate of adoption of new technology and the characteristics of such technology. While it may be true that prices of individual buildings within the real estate asset class may change less frequently than interest rates, the same cannot be said of CMBS, CMBX and REITs. Equity and fixed income derivatives within capital markets change contemporaneously with changes in interest rates and risk premia. Despite their size and importance in capital markets, near real time information content for credit sensitive US fixed income has only recently come into focus in the microstructure literature. CMBX is one segment of the fixed income market where sparsity of meaningful real time data obscures insights into underlying risk pricing effects of the underlying asset class. Because of that, there is value in understanding the intraday risk composition of the \$600 billion CMBS sector and its CMBX derivatives. In this first study into CMBX microstructure we provide such intraday insights into CMBX liquidity with crossover insights into the related \$1.3 trillion REIT sector before and during the Covid-19 pandemic.

Building on previous work in the literature related to partitioning credit risk from other risks embedded in risk premia, in the two earlier studies of Christopoulos (2017) and Christopoulos and Jarrow (2018) focusing on CMBX risk partitioning, the frequency of capture is monthly. This reflected the limited availability of capital resources for computation and limited frequency of available data. Because the results in those studies were quite good, we were able to leverage them and increase the frequency of risk partition estimation to daily and then intraday pacing in this study. By addressing some of the gaps in the frequency and accuracy of risk information in the CMBX market, we advance the literature in line with more developed markets. Initially, this study provides a valuable contribution of reconciliation between classical microstructure and reduced form assessments of liquidity for the daily model. There we find projected reduced form estimates of liquidity to be significant in historic and forecasted bid-ask spreads.

With those insights at the daily level, we move to the intraday level. There, by estimating millions of intraday CMBX risk decompositions for all investment grade credits in 15 second

intervals we reveal apparent regular volatility pockets of risk partition pricing in the cross-section over the sample period. These cross-sectional characteristics reveal new insights into risk measure price sensitivity to changing market conditions. We investigate into these phenomena in the related REIT sector. By fusing the CMBX risk partition signals with REIT pricing in 54 day trading strategies, we were able to achieve significant ICAPM  $\alpha's$  in about 96% of the strategies and positive cumulative returns ranging from 0.73% to 48.74% in about 65% of the strategies during the Covid pandemic. By our results, the fusion of CMBX risk partition signals and REIT pricing, appears to capture a broader investor sentiment with respect to the pricing of real estate securities apart from the idiosyncratic risks of default and rate risks in specific collateral pools underlying CMBX.

If more broad real estate risk sentiments of investors are embedded within the CMBX residual risk partitions of liquidity and excess liquidity, it would make sense if those measures revealed pricing insights into real estate risk in securities apart from CMBX. This is certainly the case in the assessment of the relative value of REITs with CMBX risk partitions in this study. The method in this paper, which is generalizable to all fixed income securities, appears to disclose a crossover liquidity sentiment with respect to commercial real estate securities and their pricing in the mind of the market, separate from the modelled idiosyncratic risks of specific collateral underlying CMBX. To our knowledge, this is the first study of its kind to investigate projections of reduced form CMBX risk decompositions on a daily and intraday basis. Since the pace of our intraday risk partitions exceeds the typical pace of CMBX trading, our good results validate the theoretical insights of CMBX with respect to REITs.

This study begs the question as to 'What insights would the direct simulation approach of Christopoulos (2017) and Christopoulos and Jarrow (2018) provide intraday?' compared with the estimation approach we introduce in this paper. The answer to that question, depends upon the availability of highly costly comprehensive data at loan, bond and deal levels and expensive high performance computing resources, and is thus left to future research. Additionally, considering optimized trading strategies intraday across risk partition signals, would also be interesting. Given the rapid pacing of interest rates, such extensions with interest rate risk pricing partitions in conjunction with REITs would build on the extensive prior work in the literature related to interest rate term structure models. Establishing further connections between intraday risk partition pricing and actual CMBX pricing

would also be exciting, and that line of inquiry is purely an issue of data accessibility as the method in this work applies. Similarly, extending the general approach introduced here and applying it to the Corporate bond sector would too be interesting. Finally, from a policy perspective, investigating into the longer term relationship (if any) between intraday signals of risk partitions and manifestation of actual hazards in the real estate asset classes (and Corporates) would be an interesting area for exploration. Lending criteria, risk retention, and capital constraints all have links to capital markets. Research inquiries into the nature of those links, with the intraday approach we introduce, before hazards manifest, seems a natural next level of inquiry. These and other questions are left to future work.

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# A Appendix

### A.1 CMBX microstructure fundamentals

<u>Figure 11</u> as of the close of business 3/18/2020 at 4:15pm EST was generously provided by one of the world's leading money managers. CMBX does not trade on a price basis, rather in keeping with most other credit sensitive fixed income securities, CMBX trades on a spread over the relevant risk free rate (in bps). <u>Figure 11</u> depicts an end-of-day summary for actively traded CMBX Series (6-13).<sup>22</sup>

Figure 11: Closing quotes of bid-ask spreads and 1 day changes to mid-market spreads (3/18/2020)

	IKADING	C 160	The same of the sa			.12 ,01	1500 01 77.	201
This M	essage is Firm	n-forwa	rdable					
TNDY	10 CMRY 1	3 CHG	18 CMBX 1	2 CHG	17 CMBX.1	1 CHG	16 CMBX.1	O CHG
AAA	144/134	+19	133/123	+19	122/111	+18	112/102	+18
AS	255/205	+51	235/185	+44	220/170	+42	205/165	+37
AA	330/280	+66	305/265	+65	310/260	+72	300/260	+76
Δ.	460/390			+84	410/360	+83	405/355	+89
BBB-	815/755	4	790/750		740/690	+117	720/670	+104
	1200/1050		1350/1100		1150/1000		1200/1050	+207
	1200/1030		1000/ 1100					
TNDX	15 CMBX.9	CHG	14 CMBX.8	3 CHG	13 CMBX.7	CHG	12 CMBX.6	CHO
AAA	103/93	+18	96/86	+18	86/86	+22	78/68	+15
AS	200/150	+43	185/135	+43	170/120	+41	150/120	+30
AA	285/235	+69	280/230	+84	255/205	+78	260/210	+65
A	390/340	+95	415/365	+120	375/325	+88	485/435	+88
BBB-		+105	810/760		800/750	+140	1395/1265	+233

This screenshot shows a Bloomberg post on 3/18/2020 for the quoted bid-ask spreads for CMBX Series 6 through 13 across AAA through BB tranches for Series 10 through 13 and AAA through BBB- for Series 6 through 15. The bid side is on the left of the '/' and the offered side on the right. Bid and Ask are depicted in basis points (bps). The column 'CHG' indicates the change from the prior end of mark to market mid-market spread, and is also quoted in bps..

For each column the year of issuance (expressed in two digits, so 19 is 2019, 18 is 2018, etc.) of the CMBX Series and the CMBX Series name are provided. For example, in the top left, 19 CMBX.13 refers to CMBX Series 13 issued in 2019 ('19'). Below each Series column heading are the bid-side and the ask-side of the bid-ask spread,  $s_t$ , which bound the midmarket risk premium,  $S_t$ , for each of the tranches (AAA through Ba) in the corresponding credit rating rows. Immediately to the right under each column is the 'CHG' which is the

<sup>&</sup>lt;sup>22</sup>While this information on bid-ask spreads is posted in Bloomberg from dealers to investors, it is not recorded in a central repository with Markit. This is one motivation for our paper.

change in mid-market spread,  $\Delta S_t$ , day over day at the close, where  $\Delta S_t = S_t - S_{t-1}$ . These quotes are for fixed-income risk premia from the market-maker's perspective.

In OTC fixed-income markets, pricing (bid-side, ask-side and mid-market) is typically quoted in terms of risk premia above the relevant risk-free rate. As described in Fabozzi (2016), for amortizing securities, the relevant risk-free rate is a linearly interpolated benchmark risk-free rate (treasuries or interest rate swaps spreads) corresponding to the weighted average life (WAL) of the security being priced described below, where

$$wal_{jk}(t) = \begin{cases} \frac{\left(\frac{\sum_{t=s}^{T} t \hat{\mathbb{A}}_{jk}(t)}{\sum_{t=s}^{T} \hat{\mathbb{A}}_{jk}(t)}\right)}{12}, & \text{for } \sum_{t=1}^{T} F_{jk}(t) > 0, \text{ and} \\ 0, & \text{otherwise} \end{cases}$$
(35)

is the weighted average time (in years) to the receipt of the promised monthly principal cashflows,  $F_{jk}(t)$ , received at month t, of the k-th bond/rating cohort in the j-th CMBX Series.

Example 1. For end-of-day 3/18/2020, the market-maker's bid-side,  $B_t$ , for CMBX 13 AAA is 144 bps over the risk free rate, while the market maker's ask-side,  $A_t$ , is 134 bps over the risk free rate. Thus total bid-ask spread,  $s_t$  is the difference between the bid-side and the offer-side,  $s_t = B_t - A_t$  which in this example 10 bps (144-134). The mid-market spread for 3/18/2020,  $S_t$ , is 139 bps which is the midpoint between the bid-side and the offer side,  $S_t = \frac{(B_t + A_t)}{2}$ . Finally from the change in mid market spread column for each Series, we note that  $S_t$  is 19 bps wider than  $S_{t-1}$  the prior day's (3/17/2020) close, and so  $S_{t-1} = S_t - 19 = 120$  bps for this example.

In OTC fixed-income markets, bid-ask spreads are sometimes expressed in conjunction with 'sizes' (quoted face amounts in currency) though they are not always recorded.<sup>23</sup> Such sizes for which the bid-ask spread quotes are valid, indicate the 'depth' of the quote and, in the aggregate, the depth of the market (or sector) overall. Quotes of the bid and ask risk premia (and corresponding sizes) are temporal. Thus, even in the absence of requests for execution, the bid-ask spread between bid-side and ask-side risk premia (spreads), and corresponding sizes, may change reflecting the market-maker's perception of risk due to a

 $<sup>^{23}</sup>$ As for example in our time series which only includes spreads, and as shown in the post in Figure 11.

variety of factors including changing market conditions and inventories. Bid-ask spreads equal to zero are referred to as 'locked-markets' where the market-maker is willing to buy and sell at the same spread, such that the bid-side and ask-side of the bid-ask spread are equal to one another.

CMBX trading frequency had at one point been roughly 10x the frequency observed in the cash CMBS market as noted by SIFMA. The recording of trading in CRE derivatives is increasing the flow of information as noted in Hollified, Nekyudov and Spatt (2017). Nevertheless, during Covid and the concomitant deterioration in CRE, CMBX has too deteriorated in terms of its actual (not-modelled) liquidity. Information digestion is wide and trading execution directly in the screens make such digestion immediate. When execution is done dealer to client, the digestion of information is much longer as only the market making desk that executes would have "real time" info.

Interestingly, despite some advances in information flow, the CMBX market still does not provide reliable intraday recorded bid-ask spreads, mid-market spreads, corresponding trade execution prices, transaction volumes, or, importantly, risk decomposition monitoring in real time. As such, the information content available for CMBX is still limited and is consistent with the earlier period in the literature in which Roll (1984) and Thompson and Waller (1987) introduce their models. Those models and their adaptations are thus appropriate for CMBX daily bid-ask estimation and provide insight in conjunction with our increased frequency estimation of indexed risk decomposition.

# A.2 VAR Tables

Table 21: VAR AAA CMBX

		G. ID	D (5 1/1)		-		G. ID	D (5 141)	G.
ADCD HAAAT1	Estimate	StdError	Pr(> t )	Sig ***	ADCD HAAATI	Estimate	StdError	Pr(> t )	Sig
ABSRollAAA.L1	0.57265	0.01881	<2.00E-16	**	ABSRollAAA.L1	0.569389	0.018874	<2.00E-16	
CJlq.L1	3.46923	1.10395	0.001692		CJxslq.L1	-1.417582	0.816753	0.082739	
ABSRollAAA.L2	0.02048	0.0217	0.34554		ABSRollAAA.L2	0.025181	0.021722	0.246456	
CJlq.L2	0.17021	1.17189	0.884529	***	CJxslq.L2	0.391611	0.887517	0.659071	***
ABSRollAAA.L3	0.36228	0.0217	<2.00E-16	***	ABSRollAAA.L3	0.356316	0.02165	<2.00E-16	*
CJlq.L3	1.88855	1.17416	0.107854	***	CJxslq.L3	-1.876339	0.890014	0.035101	**
ABSRollAAA.L4	0.07374	0.02237	0.000992	***	ABSRollAAA.L4	0.062477	0.022652	0.005852	**
CJlq.L4	0.86971	1.17343	0.458652	***	CJxslq.L4	0.821246	0.887263	0.354736	***
ABSRollAAA.L5	-0.23068	0.02237	<2.00E-16	***	ABSRollAAA.L5	-0.24152	0.02266	<2.00E-16	**
CJlq.L5	-2.03651	1.17257	0.082533	*	CJxslq.L5	2.559536	0.888143	0.003983	*
ABSRollAAA.L6	0.04481	0.02177	0.039601	*	ABSRollAAA.L6	0.052903	0.022629	0.019467	*
CJlq.L6	-1.32114	1.17077	0.259232		CJxslq.L6	0.061837	0.889057	0.944554	
ABSRollAAA.L7	-0.02312	0.02178	0.288464		ABSRollAAA.L7	-0.009097	0.022607	0.687434	***
CJlq.L7	0.36954	1.16785	0.751703	ale ale ale	CJxslq.L7	-3.042457	0.886945	0.000612	
ABSRollAAA.L8	0.08763	0.01883	3.40E-06	***	ABSRollAAA.L8	0.093711	0.021572	1.45E-05	**
CJlq.L8	-1.24547	1.1027	0.258794		CJxslq.L8	-0.04969	0.889555	0.955458	
			0.863177		ABSRollAAA.L9	0.011963	0.021642	0.580472	
					CJxslq.L9	0.655737	0.88623	0.459413	
					ABSRollAAA.L10	-0.055848	0.018825	0.003036	**
				_	CJxslq.L10	-1.75708	0.814223	0.031014	*
const	-0.07769	0.45078			const	1.791993	0.291729	9.27E-10	**
F-stat p-value	< 2.2e-16				F-stat p-value	< 2.2e-16			
Adj. Rsq	0.7307				Adj. Rsq	0.7318			
$^{ m df}$	2803				df	2797			
Panel C: CJ Lie	quidity_AAA	VAR with T	hompson Wal	ler	Panel D: CJ Exces	ss Liquidity_A	AA VAR with	n Thompson W	aller
Panel C: CJ Lie	quidity_AAA	VAR with T	Chompson Wal	ler	Panel D: CJ Exces	ss Liquidity_A	AA VAR with	Thompson W	aller Si
Panel C: CJ Lie					Panel D: CJ Exces		-	-	Si
	Estimate	StdError	Pr(> t ) <2.00E-16	Sig	TWAAA.L1	Estimate	StdError	Pr(> t ) <2.00E-16	Si
TWAAA.L1	Estimate 0.937575	StdError 0.018911	Pr(> t )	Sig ***		Estimate 0.9254143	StdError 0.0188643	Pr(> t )	
TWAAA.L1 CJlq.L1 TWAAA.L2	Estimate 0.937575 1.923353	StdError 0.018911 0.690751	Pr(> t ) <2.00E-16 0.005398	Sig ***	TWAAA.L1 CJxslq.L1 TWAAA.L2	Estimate 0.9254143 -0.7926893	StdError 0.0188643 0.510231	Pr(> t ) <2.00E-16 0.120396	Si; **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2	Estimate 0.937575 1.923353 -0.263708 -1.330626	StdError 0.018911 0.690751 0.025932 0.731897	Pr(> t ) <2.00E-16 0.005398 <2.00E-16 0.069163	Sig ***	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908	StdError 0.0188643 0.510231 0.0257194 0.5551738	Pr(> t ) <2.00E-16 0.120396 <2.00E-16 0.029073	Si; **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619	StdError 0.018911 0.690751 0.025932 0.731897 0.026325	Pr(> t ) <2.00E-16 0.005398 <2.00E-16 0.069163 0.000213	Sig *** ** **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432	$\begin{array}{c} \Pr(> \mathbf{t} ) \\ < 2.00\text{E-}16 \\ 0.120396 \\ < 2.00\text{E-}16 \\ 0.029073 \\ 0.000267 \end{array}$	Si; **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776	Pr(> t ) <2.00E-16 0.005398 <2.00E-16 0.069163 0.000213 0.004007	Sig *** ** ***	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731	$\begin{array}{c} \Pr(> t ) \\ < 2.00E\text{-}16 \\ 0.120396 \\ < 2.00E\text{-}16 \\ 0.029073 \\ 0.000267 \\ 0.058841 \end{array}$	Si; **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395	Pr(> t ) <2.00E-16 0.005398 <2.00E-16 0.069163 0.000213 0.004007 0.658618	Sig *** ** ***	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038	$\begin{array}{c} \Pr(> \mathbf{t} ) \\ < 2.00E\text{-}16 \\ 0.120396 \\ < 2.00E\text{-}16 \\ 0.029073 \\ 0.000267 \\ 0.058841 \\ 0.462628 \end{array}$	Si; **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.733637	Pr(> t ) <2.00E-16 0.005398 <2.00E-16 0.069163 0.000213 0.004007 0.658618 0.001993	Sig *** ** *** ***	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548	Pr(> t ) <2.00E-16 0.120396 <2.00E-16 0.029073 0.000267 0.058841 0.462628 0.17062	Si; **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4 TWAAA.L5	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.733637 0.026373	Pr(> t ) <2.00E-16 0.005398 <2.00E-16 0.069163 0.000213 0.004007 0.658618 0.001993 0.118773	Sig *** ** *** ***	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955	Pr(> t ) <2.00E-16 0.120396 <2.00E-16 0.029073 0.000267 0.058841 0.462628 0.17062 0.220419	Si **
TWAAA.L1 CJIq.L1 TWAAA.L2 CJIq.L2 TWAAA.L3 CJIq.L3 TWAAA.L4 CJIq.L4 TWAAA.L5 CJIq.L5	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152 -2.319467	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.733637 0.026373 0.735903	Pr(> t ) <2.00E-16 0.005398 <2.00E-16 0.069163 0.000213 0.004007 0.658618 0.001993 0.118773 0.001639	Sig *** ** ** ** ** **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L5	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.5558235	Pr(> t ) <2.00E-16 0.120396 <2.00E-16 0.029073 0.000267 0.058841 0.462628 0.17062 0.220419 0.010592	Si ** ** **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4 TWAAA.L5 CJlq.L5 TWAAA.L6	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152 -2.319467 0.043547	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.733637 0.026373 0.735903 0.026321	Pr(> t ) <2.00E-16 0.005398 <2.00E-16 0.069163 0.000213 0.004007 0.658618 0.001993 0.118773 0.001639 0.098144	Sig ***  **  **  **  **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L5 TWAAA.L5	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787 0.0498144	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.5558235 0.0260796	Pr(> t ) <2.00E-16 0.120396 <2.00E-16 0.029073 0.000267 0.058841 0.462628 0.17062 0.220419 0.010592 0.056224	Si ** ** **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4 TWAAA.L5 CJlq.L5 TWAAA.L6 CJlq.L6	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152 -2.319467 0.043547 1.580418	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.733637 0.026373 0.735903 0.026321 0.73711	$\begin{array}{c} \Pr(> t ) \\ < 2.00E\text{-}16 \\ 0.005398 \\ < 2.00E\text{-}16 \\ 0.069163 \\ 0.000213 \\ 0.004007 \\ 0.658618 \\ 0.001993 \\ 0.118773 \\ 0.001639 \\ 0.098144 \\ 0.032113 \end{array}$	Sig *** ** ** ** ** **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L5 TWAAA.L6 CJxslq.L6	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787 0.0498144 -0.3272787	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.5558235 0.0260796 0.5563596	Pr(> t ) <2.00E-16 0.120396 <2.00E-16 0.029073 0.000267 0.058841 0.462628 0.17062 0.220419 0.010592 0.056224 0.556412	Si ** ** **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4 TWAAA.L5 CJlq.L5 TWAAA.L6 CJlq.L6	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.26999 0.041152 -2.319467 0.043547 1.580418 0.004757	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.733637 0.026373 0.735903 0.026321 0.73711	Pr(> t ) <2.00E-16 0.005398 <2.00E-16 0.069163 0.000213 0.004007 0.658618 0.001993 0.118773 0.001639 0.098144 0.032113 0.856347	Sig *** ** ** ** ** **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L5 TWAAA.L6 CJxslq.L6 TWAAA.L7	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787 0.0498144 -0.3272787 0.0002499	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.5558235 0.0260796 0.5563596 0.0260945	$\begin{array}{c} \Pr(> t ) \\ < 2.00E-16 \\ 0.120396 \\ < 2.00E-16 \\ 0.029073 \\ 0.000267 \\ 0.058841 \\ 0.462628 \\ 0.17062 \\ 0.220419 \\ 0.010592 \\ 0.056224 \\ 0.556412 \\ 0.99236 \end{array}$	Si ** ** **
TWAAA.L1 CJIq.L1 TWAAA.L2 CJIq.L2 TWAAA.L3 CJIq.L3 TWAAA.L4 CJIq.L4 TWAAA.L5 CJIq.L5 TWAAA.L6 CJIq.L6 TWAAA.L6 CJIq.L6 TWAAA.L7 CJIq.L7	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152 -2.319467 0.043547 1.580418 0.004757 0.046257	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.733637 0.026373 0.735903 0.026321 0.73711 0.026276 0.735759	$\begin{array}{c} \Pr(> t ) \\ < 2.00E\text{-}16 \\ 0.005398 \\ < 2.00E\text{-}16 \\ 0.069163 \\ 0.000213 \\ 0.004007 \\ 0.658618 \\ 0.001993 \\ 0.118773 \\ 0.001639 \\ 0.098144 \\ 0.032113 \\ 0.856347 \\ 0.949875 \end{array}$	Sig *** ** ** ** ** **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L5 TWAAA.L6 CJxslq.L6 TWAAA.L7 CJxslq.L7	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787 0.0498144 -0.3272787 0.0002499 -0.0756219	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.5558235 0.0260796 0.5563596 0.0260945 0.5549253	Pr(> t ) <2.00E-16 0.120396 <2.00E-16 0.029073 0.000267 0.058841 0.462628 0.17062 0.220419 0.010592 0.056224 0.556412 0.99236 0.891614	Si **  **  **  .
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4 TWAAA.L5 CJlq.L6 TWAAA.L6 CJlq.L6 TWAAA.L7 CJlq.L6	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152 -2.319467 0.043547 1.580418 0.004757 0.046257 0.120366	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.733637 0.026373 0.026373 0.026321 0.73711 0.026276 0.735759 0.026173	$\begin{array}{c} \Pr(> t ) \\ < 2.00E\text{-}16 \\ 0.005398 \\ < 2.00E\text{-}16 \\ 0.069163 \\ 0.000213 \\ 0.004007 \\ 0.658618 \\ 0.001993 \\ 0.118773 \\ 0.001639 \\ 0.098144 \\ 0.032113 \\ 0.856347 \\ 0.949875 \\ 4.44E\text{-}06 \end{array}$	Sig ***  **  **  **  **  **  **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L5 TWAAA.L6 CJxslq.L6 TWAAA.L7 CJxslq.L6 TWAAA.L7 CJxslq.L7 TWAAA.L8	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787 0.0498144 -0.3272787 0.0002499 -0.0756219 0.1238949	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.5558235 0.0260796 0.5563596 0.0260945 0.5549253 0.0260181	Pr(> t ) <2.00E-16 0.120396 <2.00E-16 0.029073 0.000267 0.058841 0.462628 0.17062 0.220419 0.010592 0.0566224 0.556412 0.99236 0.891614 2.02E-06	Si **  **  **  **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4 TWAAA.L5 CJlq.L5 TWAAA.L6 CJlq.L6 TWAAA.L7 CJlq.L7 TWAAA.L7 CJlq.L1	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152 -2.319467 0.043547 1.580418 0.004757 0.046257 0.046257 0.120366 -0.280125	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.733637 0.026373 0.026321 0.73711 0.026276 0.735759 0.026173	$\begin{array}{c} \Pr(> t ) \\ < 2.00E\text{-}16 \\ 0.005398 \\ < 2.00E\text{-}16 \\ 0.069163 \\ 0.000213 \\ 0.004007 \\ 0.658618 \\ 0.001993 \\ 0.118773 \\ 0.001639 \\ 0.098144 \\ 0.032113 \\ 0.856347 \\ 0.949875 \\ 4.44E\text{-}06 \\ 0.703353 \end{array}$	Sig ***  **  **  **  **  **  **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L5 TWAAA.L6 CJxslq.L6 TWAAA.L6 CJxslq.L7 TWAAA.L7 CJxslq.L7	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787 0.0498144 -0.3272787 0.0002499 -0.0756219 0.1238949 0.7700658	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.5558235 0.0260796 0.5563596 0.0260945 0.5549253 0.0260181 0.5554689	$\begin{array}{c} \Pr(> \mathbf{t} ) \\ < 2.00E-16 \\ 0.120396 \\ < 2.00E-16 \\ 0.029073 \\ 0.000267 \\ 0.058841 \\ 0.462628 \\ 0.17062 \\ 0.220419 \\ 0.010592 \\ 0.056224 \\ 0.556412 \\ 0.99236 \\ 0.891614 \\ 2.02E-06 \\ 0.165755 \end{array}$	Si; ***  **  **  **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4 TWAAA.L5 CJlq.L5 TWAAA.L6 CJlq.L6 TWAAA.L7 CJlq.L7 TWAAA.L8 CJlq.L8 TWAAA.L8 CJlq.L8	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152 -2.319467 0.043547 1.580418 0.004757 0.120366 -0.280125 -0.032026	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.733637 0.026373 0.026321 0.026321 0.026321 0.026321 0.026276 0.735759 0.026173 0.735551 0.025815	Pr(> t ) <2.00E-16 0.005398 <2.00E-16 0.069163 0.000213 0.004007 0.658618 0.001993 0.118773 0.001639 0.098144 0.032113 0.856347 0.949875 4.44E-06 0.703353 0.214853	Sig ***  **  **  **  **  **  **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L5 TWAAA.L6 CJxslq.L6 TWAAA.L7 CJxslq.L7 TWAAA.L8 CJxslq.L8 TWAAA.L8	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787 0.0498144 -0.3272787 0.0002499 -0.0756219 0.1238949 0.7700658 -0.0341029	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.5558235 0.0260796 0.5563596 0.5260945 0.5549253 0.0260181 0.5554689 0.0256475	Pr(> t ) <2.00E-16 0.120396 <2.00E-16 0.029073 0.000267 0.058841 0.462628 0.17062 0.220419 0.010592 0.056224 0.556412 0.99236 0.891614 2.02E-06 0.165755 0.183732	Si; ** ** **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4 TWAAA.L5 CJlq.L5 TWAAA.L6 CJlq.L6 TWAAA.L6 CJlq.L6 TWAAA.L7 CJlq.L7 TWAAA.L8 CJlq.L8 TWAAA.L8 CJlq.L8	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152 -2.319467 0.043547 1.580418 0.004757 0.120366 -0.280125 -0.032026 0.558292	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.733637 0.026373 0.026373 0.735903 0.026321 0.73711 0.026276 0.735759 0.026173 0.735551 0.025815 0.733437	$\begin{array}{c} \Pr(> t ) \\ < 2.00E\text{-}16 \\ 0.005398 \\ < 2.00E\text{-}16 \\ 0.069163 \\ 0.000213 \\ 0.004007 \\ 0.658618 \\ 0.001993 \\ 0.118773 \\ 0.001639 \\ 0.098144 \\ 0.032113 \\ 0.856347 \\ 0.949875 \\ 4.44E\text{-}06 \\ 0.703353 \\ 0.214853 \\ 0.446602 \end{array}$	Sig *** **  ***  ***  **  **  **  **  **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L6 TWAAA.L6 CJxslq.L6 TWAAA.L7 CJxslq.L7 TWAAA.L8 CJxslq.L8 TWAAA.L9 CJxslq.L9	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787 0.0498144 -0.3272787 0.0002499 -0.0756219 0.1238949 0.7700658 -0.0341029 -1.0670362	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.5558235 0.0260796 0.5563596 0.0260945 0.5554689 0.0260475 0.05534818	$\begin{array}{c} \Pr(> \mathbf{t} ) \\ < 2.00E-16 \\ 0.120396 \\ < 2.00E-16 \\ 0.029073 \\ 0.000267 \\ 0.058841 \\ 0.462628 \\ 0.17062 \\ 0.220419 \\ 0.010592 \\ 0.056224 \\ 0.556412 \\ 0.99236 \\ 0.891614 \\ 2.02E-06 \\ 0.165755 \\ 0.183732 \\ 0.053973 \end{array}$	Si **  **  **  **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4 TWAAA.L5 CJlq.L6 TWAAA.L6 CJlq.L6 TWAAA.L7 CJlq.L7 TWAAA.L8 CJlq.L8 TWAAA.L8 CJlq.L8 TWAAA.L9 CJlq.L9 TWAAA.L9 CJlq.L9	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152 -2.319467 0.043547 1.580418 0.004757 0.046257 0.120366 -0.280125 -0.032026 0.558292 -0.057352	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.733637 0.026373 0.026371 0.73511 0.026276 0.735759 0.026173 0.735551 0.025815 0.733437 0.018837	$\begin{array}{c} \Pr(> \mathbf{t} ) \\ < 2.00 \text{E} \text{-}16 \\ 0.005398 \\ < 2.00 \text{E} \text{-}16 \\ 0.069163 \\ 0.000213 \\ 0.004007 \\ 0.658618 \\ 0.001993 \\ 0.118773 \\ 0.001639 \\ 0.098144 \\ 0.032113 \\ 0.856347 \\ 0.949875 \\ 4.44 \text{E} \text{-}06 \\ 0.703353 \\ 0.214853 \\ 0.446602 \\ 0.002352 \\ \end{array}$	Sig ***  **  **  **  **  **  **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L6 TWAAA.L6 CJxslq.L6 TWAAA.L7 CJxslq.L7 TWAAA.L8 CJxslq.L7 TWAAA.L8 CJxslq.L8 TWAAA.L9 CJxslq.L9 TWAAA.L10	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787 0.0042499 -0.0756219 0.1238949 0.7700658 -0.0341029 -1.0670362 -0.0691792	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.02609796 0.5563596 0.0260945 0.5549253 0.0260181 0.5554689 0.0256475 0.5534818 0.0188248	Pr(> t ) <2.00E-16 0.120396 <2.00E-16 0.029973 0.000267 0.058841 0.462628 0.17062 0.220419 0.010592 0.056224 0.556412 0.99236 0.891614 2.02E-06 0.165755 0.183732 0.053973 0.000242	Si ***  **  **  **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4 TWAAA.L5 CJlq.L5 TWAAA.L6 CJlq.L6 TWAAA.L7 CJlq.L7 TWAAA.L8 CJlq.L8 TWAAA.L8 CJlq.L8 TWAAA.L9 CJlq.L9 TWAAA.L10 CJlq.L10	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152 -2.319467 0.043547 1.580418 0.004757 0.046257 0.120366 -0.280125 -0.032026 0.558292 -0.057352 0.296099	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.735903 0.026373 0.735903 0.026321 0.73711 0.026276 0.735759 0.026173 0.735551 0.025815 0.733437 0.018837 0.691674	$\begin{array}{l} \Pr(> \mathbf{t} ) \\ < 2.00 \text{E-}16 \\ 0.005398 \\ < 2.00 \text{E-}16 \\ 0.069163 \\ 0.000213 \\ 0.004007 \\ 0.658618 \\ 0.001993 \\ 0.118773 \\ 0.001639 \\ 0.098144 \\ 0.032113 \\ 0.856347 \\ 0.949875 \\ 4.44 \text{E-}06 \\ 0.703353 \\ 0.214853 \\ 0.446602 \\ 0.002352 \\ 0.668618 \end{array}$	Sig *** **  ***  ***  **  **  **  **  **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L5 TWAAA.L6 CJxslq.L6 TWAAA.L6 CJxslq.L6 TWAAA.L7 CJxslq.L7 TWAAA.L8 CJxslq.L7 TWAAA.L8 CJxslq.L9 TWAAA.L9 CJxslq.L9 TWAAA.L10 CJxslq.L10	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787 0.0498144 -0.3272787 0.002499 -0.0756219 0.1238949 0.7700658 -0.0341029 -1.0670362 -1.0670362 -0.0691792 -0.591579	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.5558235 0.0260796 0.5563596 0.0260945 0.5540253 0.0260181 0.55534618 0.0256475 0.5534818 0.0188248 0.0188248	$\begin{array}{c} \Pr(> \mathbf{t} ) \\ < 2.00E-16 \\ 0.120396 \\ < 2.00E-16 \\ 0.029073 \\ 0.000267 \\ 0.058841 \\ 0.462628 \\ 0.17062 \\ 0.220419 \\ 0.010592 \\ 0.056224 \\ 0.556412 \\ 0.99236 \\ 0.891614 \\ 2.02E-06 \\ 0.165755 \\ 0.183732 \\ 0.053973 \\ 0.000242 \\ 0.244874 \end{array}$	Sii ***  ***  **  **  **  ***
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4 TWAAA.L5 CJlq.L6 TWAAA.L6 CJlq.L6 TWAAA.L7 CJlq.L7 TWAAA.L8 CJlq.L8 TWAAA.L9 CJlq.L9 TWAAA.L10 CJlq.L10 const	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152 -2.319467 0.043547 1.580418 0.004757 0.046257 0.120366 -0.280125 -0.032026 0.558292 -0.057352 0.296099 0.143671	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.733637 0.026373 0.026371 0.73511 0.026276 0.735759 0.026173 0.735551 0.025815 0.733437 0.018837	$\begin{array}{c} \Pr(> \mathbf{t} ) \\ < 2.00 \text{E} \text{-} 16 \\ 0.005398 \\ < 2.00 \text{E} \text{-} 16 \\ 0.069163 \\ 0.000213 \\ 0.004007 \\ 0.658618 \\ 0.001993 \\ 0.118773 \\ 0.001639 \\ 0.098144 \\ 0.032113 \\ 0.856347 \\ 0.949875 \\ 4.44 \text{E} \text{-} 06 \\ 0.703353 \\ 0.214853 \\ 0.446602 \\ 0.002352 \end{array}$	Sig *** **  ***  ***  **  **  **  **  **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L5 TWAAA.L6 CJxslq.L6 TWAAA.L6 CJxslq.L7 TWAAA.L7 CJxslq.L7 TWAAA.L8 CJxslq.L9 TWAAA.L9 CJxslq.L9 TWAAA.L10 CJxslq.L10 const	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787 0.0498144 -0.3272787 0.0002499 -0.0756219 0.1238949 0.7700658 -0.0341029 -1.0670362 -0.0691792 -0.591579 0.9798136	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.02609796 0.5563596 0.0260945 0.5549253 0.0260181 0.5554689 0.0256475 0.5534818 0.0188248	Pr(> t ) <2.00E-16 0.120396 <2.00E-16 0.029973 0.000267 0.058841 0.462628 0.17062 0.220419 0.010592 0.056224 0.556412 0.99236 0.891614 2.02E-06 0.165755 0.183732 0.053973 0.000242	Si ***  **  **  **
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4 TWAAA.L5 CJlq.L5 TWAAA.L6 CJlq.L6 TWAAA.L7 CJlq.L7 TWAAA.L7 CJlq.L7 TWAAA.L8 CJlq.L9 TWAAA.L9 CJlq.L9 TWAAA.L10 CJlq.L10 const F-stat p-value	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152 -2.319467 0.043547 1.580418 0.004757 0.102366 -0.280125 -0.032026 0.558292 -0.057352 0.296099 0.143671 <<2.2e-16	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.735903 0.026373 0.735903 0.026321 0.73711 0.026276 0.735759 0.026173 0.735551 0.025815 0.733437 0.018837 0.691674	$\begin{array}{l} \Pr(> \mathbf{t} ) \\ < 2.00 \text{E-}16 \\ 0.005398 \\ < 2.00 \text{E-}16 \\ 0.069163 \\ 0.000213 \\ 0.004007 \\ 0.658618 \\ 0.001993 \\ 0.118773 \\ 0.001639 \\ 0.098144 \\ 0.032113 \\ 0.856347 \\ 0.949875 \\ 4.44 \text{E-}06 \\ 0.703353 \\ 0.214853 \\ 0.446602 \\ 0.002352 \\ 0.668618 \end{array}$	Sig *** **  ***  ***  **  **  **  **  **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L5 TWAAA.L6 CJxslq.L6 TWAAA.L6 CJxslq.L6 TWAAA.L7 CJxslq.L7 TWAAA.L8 CJxslq.L7 TWAAA.L8 CJxslq.L9 TWAAA.L9 CJxslq.L9 TWAAA.L10 CJxslq.L10 const F-stat p-value	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787 0.0498144 -0.3272787 0.0002499 -0.0756219 0.1238949 0.7700658 -0.0341029 -1.0670362 -0.0691792 -0.591579 0.9798136	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.5558235 0.0260796 0.5563596 0.0260945 0.5540253 0.0260181 0.55534618 0.0256475 0.5534818 0.0188248 0.0188248	$\begin{array}{c} \Pr(> \mathbf{t} ) \\ < 2.00E-16 \\ 0.120396 \\ < 2.00E-16 \\ 0.029073 \\ 0.000267 \\ 0.058841 \\ 0.462628 \\ 0.17062 \\ 0.220419 \\ 0.010592 \\ 0.056224 \\ 0.556412 \\ 0.99236 \\ 0.891614 \\ 2.02E-06 \\ 0.165755 \\ 0.183732 \\ 0.053973 \\ 0.000242 \\ 0.244874 \end{array}$	Sii ***  ***  **  **  **  ***
TWAAA.L1 CJlq.L1 TWAAA.L2 CJlq.L2 TWAAA.L3 CJlq.L3 TWAAA.L4 CJlq.L4 TWAAA.L5 CJlq.L6 TWAAA.L6 CJlq.L6 TWAAA.L7 CJlq.L8 TWAAA.L7 CJlq.L8 TWAAA.L8 CJlq.L8 TWAAA.L9 CJlq.L9 TWAAA.L10 CJlq.L10 const	Estimate 0.937575 1.923353 -0.263708 -1.330626 0.097619 -2.113251 -0.011663 2.269999 0.041152 -2.319467 0.043547 1.580418 0.004757 0.046257 0.120366 -0.280125 -0.032026 0.558292 -0.057352 0.296099 0.143671	StdError 0.018911 0.690751 0.025932 0.731897 0.026325 0.733776 0.026395 0.735903 0.026373 0.735903 0.026321 0.73711 0.026276 0.735759 0.026173 0.735551 0.025815 0.733437 0.018837 0.691674	$\begin{array}{l} \Pr(> \mathbf{t} ) \\ < 2.00 \text{E-}16 \\ 0.005398 \\ < 2.00 \text{E-}16 \\ 0.069163 \\ 0.000213 \\ 0.004007 \\ 0.658618 \\ 0.001993 \\ 0.118773 \\ 0.001639 \\ 0.098144 \\ 0.032113 \\ 0.856347 \\ 0.949875 \\ 4.44 \text{E-}06 \\ 0.703353 \\ 0.214853 \\ 0.446602 \\ 0.002352 \\ 0.668618 \end{array}$	Sig *** **  ***  ***  **  **  **  **  **	TWAAA.L1 CJxslq.L1 TWAAA.L2 CJxslq.L2 TWAAA.L3 CJxslq.L3 TWAAA.L4 CJxslq.L4 TWAAA.L5 CJxslq.L5 TWAAA.L6 CJxslq.L6 TWAAA.L6 CJxslq.L7 TWAAA.L7 CJxslq.L7 TWAAA.L8 CJxslq.L9 TWAAA.L9 CJxslq.L9 TWAAA.L10 CJxslq.L10 const	Estimate 0.9254143 -0.7926893 -0.2539046 1.2122908 0.0950697 1.053332 -0.0191766 -0.760877 0.031985 -1.4215787 0.0498144 -0.3272787 0.0002499 -0.0756219 0.1238949 0.7700658 -0.0341029 -1.0670362 -0.0691792 -0.591579 0.9798136	StdError 0.0188643 0.510231 0.0257194 0.5551738 0.0260432 0.5572731 0.0261038 0.5551548 0.0260955 0.5558235 0.0260796 0.5563596 0.0260945 0.5540253 0.0260181 0.55534618 0.0256475 0.5534818 0.0188248 0.0188248	$\begin{array}{c} \Pr(> \mathbf{t} ) \\ < 2.00E-16 \\ 0.120396 \\ < 2.00E-16 \\ 0.029073 \\ 0.000267 \\ 0.058841 \\ 0.462628 \\ 0.17062 \\ 0.220419 \\ 0.010592 \\ 0.056224 \\ 0.556412 \\ 0.99236 \\ 0.891614 \\ 2.02E-06 \\ 0.165755 \\ 0.183732 \\ 0.053973 \\ 0.000242 \\ 0.244874 \end{array}$	Si ***  **  **  **  **  **

This table shows the results for the VAR with the daily AAA CMBX bid-ask estimates as the endogenous variables and liquidity (CJ Liquidity) and excess liquidity (CJ xslq) as the exogenous variables. The lags, L#, are determined by the Akaike Information Criteria (AIC) to a maximum of 10 lags. Estimates are provided with standard errors, probabilities and statistical significance. All panels capture the lagged effective bid-ask spread for the labelled model. Panels A and B report the estimates using the Absolute Roll measure of Christopoulos (2020) for AAA effective bid-ask spreads with the lagged liquidity (CJIq, Panel A) and excess liquidity (CJxslq, Panel B). Panels C and D report the estimates using the effective bid-ask measure of Thompson and Waller (1987) for AAA effective bid-ask spreads with the lagged liquidity (CJIq, Panel C) and excess liquidity (CJxslq, Panel D). The F-test p-value and the value of the VAR's Adjusted R-squared and degrees of freedom are reported at the bottom of each panel. \*\*\*/\*\*/\*/' correspond to 0.1%, 1%, 5% and 10% levels of significance.

Table 22: VAR BBB CMBX

Panel A: CJ	Liquidity_BE	BB VAR with	Absolute Rol	l	Panel B: CJ Exce	ess Liquidity_	BBB VAR w	rith Absolute I	Roll
ABSRollBBB.L1	Estimate 0.98165	StdError 0.01869	Pr(> t ) <2.00E-16	Sig ***	ABSRollBBB.L1	Estimate 0.974638	StdError 0.018902	Pr(> t ) <2.00E-16	Sig ***
CJlq.L1 ABSRollBBB.L2	5.238883 -0.108892	$\begin{array}{c} 9.400263 \\ 0.026028 \end{array}$	0.5774 2.96E-05	***	CJxslq.L1 $ABSRollBBB.L2$	3.808602 -0.108012	6.963996 $0.026256$	0.5845 4.01E-05	***
CJlq.L2 ABSRollBBB.L3	2.002425 $0.066317$	9.96197 $0.0261$	0.8407 $0.0111$	*	CJxslq.L2 ABSRollBBB.L3	-9.990817 0.06384	7.591396 $0.026026$	0.1883 $0.0142$	*
CJlq.L3 ABSRollBBB.L4	12.806762 -0.525612	9.980923 $0.02613$	0.1996 <2.00E-16	***	CJxslq.L3 ABSRollBBB.L4	-5.195364 -0.526175	7.617645 $0.026044$	0.4953 <2.00E-16	***
CJlq.L4	-7.447551	9.974604	0.4553	***	CJxslq.L4	4.416655	7.585277	0.5604	***
ABSRollBBB.L5 CJlq.L5	0.420097 $2.422779$	0.026801 $9.99648$	<2.00E-16 0.8085		ABSRollBBB.L5 CJxslq.L5	0.417218 $0.896584$	0.027874 $7.594219$	<2.00E-16 0.906	
ABSRollBBB.L6 CJlq.L6	-0.008049 6.362776	0.026127 $9.972082$	0.758 $0.5235$		ABSRollBBB.L6 CJxslq.L6	-0.009913 -8.464498	0.027874 $7.592601$	$0.7221 \\ 0.265$	
ABSRollBBB.L7 CJlq.L7	0.035015 $3.355688$	0.026087 $9.976895$	0.1796 0.7366		ABSRollBBB.L7 CJxslq.L7	0.033203 -7.166614	0.02605 $7.575375$	0.2026 $0.3442$	
ABSRollBBB.L8	-0.213281	0.026012 9.954828	3.64E-16	***	ABSRollBBB.L8	-0.213458	0.026026	3.57E-16	***
CJlq.L8 ABSRollBBB.L9	-1.770599 $0.147624$	0.01868	0.8588 3.89E-15	***	CJxslq.L8 ABSRollBBB.L9	3.646027 $0.147282$	7.582864 $0.02625$	0.6307 2.21E-08	***
CJlq.L9	5.24658	9.3903	0.5764		CJxslq.L9 ABSRollBBB.L10 CJxslq.L10	0.88437 -0.006246 -9.164495	7.555367 0.018888 6.932413	0.9068 0.7409 0.1863	
const	-1.905478	3.957207	0.6302	-	const	13.769115	2.034755	1.60E-11	***
F-stat p-value Adj. Rsq df	<2.2E-16 0.7105 2800				F-stat p-value Adj. Rsq df	<2.2E-16 0.7126 2797			
Panel C: CJ Li	·				Panel D: CJ Excess	· ·		h Thompson V	Valler
TWBBB.L1	Estimate 1.0877	StdError 0.01888	$\Pr(> t )$ <2.00E-16	Sig ***		Estimate		To (1.15)	<i>a</i> .
$_{\mathrm{CJlq.L1}}^{\mathrm{CJlq.L1}}$	-5.92985		<2.00L-10		TWBBB.L1	1.07463	StdError 0.01886	$\Pr(> t )$ <2.00E-16	Sig ***
		19.62361 0.02786	0.762538	***	CJxslq.L1	1.07463 -18.46408	0.01886 $14.48756$	<2.00E-16 0.2026	Sig ***
CJlq.L2	-0.15956 -3.42982	0.02786 $20.8086$	0.762538 1.13E-08 0.869092		CJxslq.L1 TWBBB.L2 CJxslq.L2	1.07463 -18.46408 -0.15629 13.63989	0.01886 $14.48756$ $0.02766$ $15.77238$	<2.00E-16 0.2026 1.75E-08 0.387225	***
TWBBB.L3 CJlq.L3	-0.15956 -3.42982 -0.1258 13.72369	0.02786 $20.8086$ $0.02799$ $20.85119$	0.762538 1.13E-08 0.869092 7.28E-06 0.510481	***	CJxslq.L1 TWBBB.L2 CJxslq.L2 TWBBB.L3 CJxslq.L3	1.07463 -18.46408 -0.15629 13.63989 -0.12526 -13.66792	0.01886 14.48756 0.02766 15.77238 0.02776 15.82018	<2.00E-16 0.2026 1.75E-08 0.387225 6.70E-06 0.387687	***
TWBBB.L3	-0.15956 -3.42982 -0.1258	0.02786 $20.8086$ $0.02799$	0.762538 1.13E-08 0.869092 7.28E-06		CJxslq.L1 TWBBB.L2 CJxslq.L2 TWBBB.L3	1.07463 -18.46408 -0.15629 13.63989 -0.12526	0.01886 $14.48756$ $0.02766$ $15.77238$ $0.02776$	<2.00E-16 0.2026 1.75E-08 0.387225 6.70E-06	***
TWBBB.L3 CJlq.L3 TWBBB.L4 CJlq.L4 TWBBB.L5	-0.15956 -3.42982 -0.1258 13.72369 0.18595 10.90645 -0.31908	0.02786 $20.8086$ $0.02799$ $20.85119$ $0.02808$ $20.83589$ $0.02794$	0.762538 1.13E-08 0.869092 7.28E-06 0.510481 4.20E-11 0.600706 <2.00E-16	***	CJxslq.L1 TWBBB.L2 CJxslq.L2 TWBBB.L3 CJxslq.L3 TWBBB.L4 CJxslq.L4 TWBBB.L5	1.07463 -18.46408 -0.15629 13.63989 -0.12526 -13.66792 0.17938 -25.79096 -0.32091	0.01886 14.48756 0.02766 15.77238 0.02776 15.82018 0.02785 15.75685 0.0277	<2.00E-16 0.2026 1.75E-08 0.387225 6.70E-06 0.387687 1.40E-10 0.101783 <2.00E-16	***
TWBBB.L3 CJlq.L3 TWBBB.L4 CJlq.L4 TWBBB.L5 CJlq.L5 TWBBB.L6	-0.15956 -3.42982 -0.1258 13.72369 0.18595 10.90645 -0.31908 -12.92307 0.23683	0.02786 20.8086 0.02799 20.85119 0.02808 20.83589 0.02794 20.86593 0.02794	0.762538 1.13E-08 0.869092 7.28E-06 0.510481 4.20E-11 0.600706 <2.00E-16 0.535744 <2.00E-16	***	CJxslq.L1 TWBBB.L2 CJxslq.L2 TWBBB.L3 CJxslq.L3 TWBBB.L4 CJxslq.L4 TWBBB.L5 CJxslq.L5 TWBBB.L6	1.07463 -18.46408 -0.15629 13.63989 -0.12526 -13.66792 0.17938 -25.79096 -0.32091 -11.01383 0.23369	0.01886 14.48756 0.02766 15.77238 0.02776 15.82018 0.02785 15.75685 0.0277 15.77891 0.0277	<2.00E-16 0.2026 1.75E-08 0.387225 6.70E-06 0.387687 1.40E-10 0.101783 <2.00E-16 0.485229 <2.00E-16	***
TWBBB.L3 CJlq.L3 TWBBB.L4 CJlq.L4 TWBBB.L5 CJlq.L5	-0.15956 -3.42982 -0.1258 13.72369 0.18595 10.90645 -0.31908 -12.92307	0.02786 20.8086 0.02799 20.85119 0.02808 20.83589 0.02794 20.86593	0.762538 1.13E-08 0.869092 7.28E-06 0.510481 4.20E-11 0.600706 <2.00E-16 0.535744	***	CJxslq.L1 TWBBB.L2 CJxslq.L2 TWBBB.L3 CJxslq.L3 TWBBB.L4 CJxslq.L4 TWBBB.L5 CJxslq.L5	1.07463 -18.46408 -0.15629 13.63989 -0.12526 -13.66792 0.17938 -25.79096 -0.32091 -11.01383	$\begin{array}{c} 0.01886 \\ 14.48756 \\ 0.02766 \\ 15.77238 \\ 0.02776 \\ 15.82018 \\ 0.02785 \\ 15.75685 \\ 0.0277 \\ 15.77891 \end{array}$	<2.00E-16 0.2026 1.75E-08 0.387225 6.70E-06 0.387687 1.40E-10 0.101783 <2.00E-16 0.485229	***
TWBBB.L3 CJlq.L3 TWBBB.L4 CJlq.L4 TWBBB.L5 CJlq.L5 TWBBB.L6 CJlq.L6 TWBBB.L7 CJlq.L7	-0.15956 -3.42982 -0.1258 13.72369 0.18595 10.90645 -0.31908 -12.92307 0.23683 18.37461 0.05064 10.14835	0.02786 20.8086 0.02799 20.85119 0.02808 20.83589 0.02794 20.86593 0.02794 20.86065 0.02807 20.8232	$\begin{array}{c} 0.762538 \\ 1.13E-08 \\ 0.869092 \\ 7.28E-06 \\ 0.510481 \\ 4.20E-11 \\ 0.600706 \\ < 2.00E-16 \\ 0.535744 \\ < 2.00E-16 \\ 0.378488 \\ 0.07134 \\ 0.626043 \end{array}$	***	CJxslq.L1 TWBBB.L2 CJxslq.L2 TWBBB.L3 CJxslq.L3 TWBBB.L4 CJxslq.L4 TWBBB.L5 CJxslq.L5 TWBBB.L6 CJxslq.L6 TWBBB.L7 CJxslq.L6	1.07463 -18.46408 -0.15629 13.63989 -0.12526 -13.66792 0.17938 -25.79096 -0.32091 -11.01383 0.23369 14.18664 0.04891 -7.14949	0.01886 14.48756 0.02766 15.77238 0.02778 15.82018 0.02775 15.75685 0.0277 15.77891 0.0277 15.77523 0.02784 15.74004	<2.00E-16 0.2026 1.75E-08 0.387225 6.70E-06 0.387687 1.40E-10 0.101783 <2.00E-16 0.485229 <2.00E-16 0.368571 0.079033 0.649704	***
TWBBB.L3 CJlq.L3 TWBBB.L4 CJlq.L4 TWBBB.L5 CJlq.L5 TWBBB.L6 CJlq.L6 TWBBB.L7 CJlq.L7 TWBBB.L8	-0.15956 -3.42982 -0.1258 13.72369 0.18595 10.90645 -0.31908 -12.92307 0.23683 18.37461 0.05064 10.14835 -0.07936 -16.04993	0.02786 20.8086 0.02799 20.85119 0.02808 20.83589 0.02794 20.86593 0.02794 20.86665 0.02807 20.8232 0.02799 20.8232	$\begin{array}{c} 0.762538 \\ 1.13E-08 \\ 0.869092 \\ 7.28E-06 \\ 0.510481 \\ 4.20E-11 \\ 0.600706 \\ <2.00E-16 \\ 0.535744 \\ <2.00E-16 \\ 0.378488 \\ 0.07134 \\ 0.626043 \\ 0.00461 \\ 0.440956 \end{array}$	***  ***  ***  ***	CJxslq.L1 TWBBB.L2 CJxslq.L2 TWBBB.L3 CJxslq.L3 TWBBB.L4 CJxslq.L4 TWBBB.L5 CJxslq.L5 TWBBB.L6 CJxslq.L6 TWBBB.L7 CJxslq.L7 TWBBB.L8 CJxslq.L7	1.07463 -18.46408 -0.15629 13.63989 -0.12526 -13.66792 0.17938 -25.79096 -0.32091 -11.01383 0.23369 14.18664 0.04891 -7.14949 -0.08079 9.99069	0.01886 14.48756 0.02776 15.7238 0.02776 15.82018 0.0277 15.77891 0.0277 15.77523 0.02784 415.74004 0.02775 15.75457	<2.00E-16 0.2026 1.75E-08 0.387225 6.70E-06 0.387687 1.40E-10 0.101783 <2.00E-16 0.485229 <2.06E-16 0.368571 0.079033 0.649704 0.003633 0.526037	***
TWBBB.L3 CJIq.L3 TWBBB.L4 CJIq.L4 TWBBB.L5 CJIq.L6 TWBBB.L6 CJIq.L6 TWBBB.L7 CJIq.L7 TWBBB.L8 CJIq.L8 TWBBB.L9 CJIq.L8 TWBBB.L9 CJIq.L8	-0.15956 -3.42982 -0.1258 13.72369 0.18595 10.90645 -0.31908 -12.92307 0.23683 18.37461 0.05064 10.14835 -0.07936 -16.04993 0.0961 53.52448	0.02786 20.8086 0.02799 20.85119 0.02808 20.83589 20.86593 0.02794 20.86065 0.02807 20.8232 0.02799 20.82542 20.82542 20.76675	$\begin{array}{c} 0.762538\\ 1.13E-08\\ 0.869092\\ 7.28E-06\\ 0.510481\\ 4.20E-11\\ 0.600706\\ <2.00E-16\\ 0.535744\\ <2.00E-16\\ 0.378488\\ 0.07134\\ 0.626043\\ 0.00461\\ 0.440956\\ 0.000572\\ 0.010005\\ \end{array}$	***  ***  ***  ***  ***  ***	CJxslq.L1 TWBBB.L2 CJxslq.L2 TWBBB.L3 CJxslq.L3 TWBBB.L4 CJxslq.L4 TWBBB.L5 CJxslq.L5 TWBBB.L6 CJxslq.L6 TWBBB.L7 CJxslq.L7 TWBBB.L8 CJxslq.L8 TWBBB.L9 CJxslq.L8 TWBBB.L9 CJxslq.L9	1.07463 -18.46408 -0.15629 13.63989 -0.12526 -13.66792 0.17938 -25.79096 -0.32091 -11.01383 0.23369 14.18664 0.04891 -7.14949 -0.08079 9.99069 0.09769 -30.32073	0.01886 14.48756 0.02776 15.77238 0.02776 15.82018 0.02775 15.75685 0.0277 15.77891 0.0277 15.77523 0.02784 15.74004 0.02775 15.75457 0.02763 15.7029	<2.00E-16 0.2026 1.75E-08 0.387225 6.70E-06 0.387687 1.40E-10 0.101783 <2.00E-16 0.485229 <2.00E-16 0.368571 0.079033 0.649704 0.003633 0.526037 0.000413 0.053596	***  ***  ***  ***
TWBBB.L3 CJIq.L3 TWBBB.L4 CJIq.L4 TWBBB.L5 CJIq.L5 TWBBB.L6 CJIq.L6 TWBBB.L7 CJIq.L7 TWBBB.L8 CJIq.L8 TWBBB.L9	-0.15956 -3.42982 -0.1258 13.72369 0.18595 10.90645 -0.31908 -12.92307 0.23683 18.37461 0.05064 10.14835 -0.07936 -16.04993 0.0961	0.02786 20.8086 0.02799 20.85119 0.02808 20.83589 0.02794 20.86065 0.02807 20.8232 0.02799 20.82542 0.02787	$\begin{array}{c} 0.762538 \\ 1.13E-08 \\ 0.869092 \\ 7.28E-06 \\ 0.510481 \\ 4.20E-11 \\ 0.600706 \\ < 2.00E-16 \\ 0.535744 \\ < 2.00E-16 \\ 0.378488 \\ 0.07134 \\ 0.626043 \\ 0.00461 \\ 0.400956 \\ 0.000572 \\ \end{array}$	***  ***  ***  ***	CJxslq.L1 TWBBB.L2 CJxslq.L2 TWBBB.L3 CJxslq.L3 TWBBB.L4 CJxslq.L4 TWBBB.L5 CJxslq.L5 TWBBB.L6 CJxslq.L6 TWBBB.L7 CJxslq.L7 TWBBB.L8 CJxslq.L7 TWBBB.L8 CJxslq.L8 TWBBB.L9	1.07463 -18.46408 -0.15629 13.63989 -0.12526 -13.66792 0.17938 -25.79096 -0.32091 -11.01383 0.23369 14.18664 0.04891 -7.14949 -0.08079 9.99069 0.09769	0.01886 14.48756 0.02766 15.77238 0.02776 15.82018 0.02785 15.75685 0.0277 15.775891 0.0277 15.77523 0.027784 15.74004 0.02775 15.75457 0.02763	<2.00E-16 0.2026 1.75E-08 0.387225 6.70E-06 0.387687 1.40E-10 0.101783 <2.00E-16 0.485229 <2.00E-16 0.368571 0.079033 0.526037 0.000413	***  ***  ***  ***  ***
TWBBB.L3 CJlq.L4 TWBBB.L4 CJlq.L4 TWBBB.L5 CJlq.L6 TWBBB.L6 CJlq.L6 TWBBB.L7 CJlq.L7 TWBBB.L8 CJlq.L8 TWBBB.L9 CJlq.L9 TWBBB.L10 CJlq.L10 const	-0.15956 -3.42982 -0.1258 13.72369 0.18595 10.90645 -0.31908 -12.92307 0.23683 18.37461 0.05064 10.14835 -0.07936 -16.04993 0.0961 53.52448 -0.0609 -7.09095	0.02786 20.8086 20.8086 0.02799 20.85119 0.02808 20.83589 0.02794 20.86593 0.02794 20.86665 0.02807 20.8232 0.02799 20.82542 0.02787 20.76675 0.01887	$\begin{array}{c} 0.762538 \\ 1.13E-08 \\ 0.869092 \\ 7.28E-06 \\ 0.510481 \\ 4.20E-11 \\ 0.600706 \\ <2.00E-16 \\ 0.535744 \\ <2.00E-16 \\ 0.378488 \\ 0.07134 \\ 0.626043 \\ 0.00461 \\ 0.440956 \\ 0.000572 \\ 0.010005 \\ 0.001263 \end{array}$	***  ***  ***  ***  ***  ***	CJxslq.L1 TWBBB.L2 CJxslq.L2 TWBBB.L3 CJxslq.L3 TWBBB.L4 CJxslq.L4 TWBBB.L5 CJxslq.L5 TWBBB.L6 CJxslq.L6 TWBBB.L7 CJxslq.L6 TWBBB.L7 CJxslq.L7 TWBBB.L8 CJxslq.L8 TWBBB.L9 CJxslq.L9 TWBBB.L10 CJxslq.L10	1.07463 -18.46408 -0.15629 13.63989 -0.12526 -13.66792 0.17938 -25.79096 -0.32091 -11.01383 0.23369 14.18664 0.04891 -7.14949 -0.08079 9.99069 0.09769 -30.32073 -0.07402 -13.48859	0.01886 14.48756 0.02776 15.77238 0.02776 15.82018 0.02785 15.75685 0.0277 15.77891 0.0277 15.77523 0.02784 15.74004 0.02775 15.75457 0.02763 15.7029 0.01883	<2.00E-16 0.2026 1.75E-08 0.387225 6.70E-06 0.387687 1.40E-10 0.101783 <2.00E-16 0.368571 0.079033 0.649704 0.003633 0.526037 0.000413 0.053596 8.69E-05	***  ***  ***  ***
TWBBB.L3 CJIq.L4 TWBBB.L5 CJIq.L4 TWBBB.L5 CJIq.L6 TWBBB.L6 CJIq.L6 TWBBB.L7 CJIq.L7 TWBBB.L8 CJIq.L8 TWBBB.L9 CJIq.L9 TWBBB.L10 CJIq.L10	-0.15956 -3.42982 -0.1258 13.72369 0.18595 10.90645 -0.31908 -12.92307 0.23683 18.37461 0.05564 10.14835 -0.07936 -16.04993 0.0961 53.52448 -0.0609 -7.09095	0.02786 20.8086 0.02799 20.85119 0.02808 20.83589 0.02794 20.86065 0.02807 20.8232 0.02799 20.82542 0.02787 20.76675 0.01887 19.60909	$\begin{array}{c} 0.762538\\ 1.13E-08\\ 0.869092\\ 7.28E-06\\ 0.510481\\ 4.20E-11\\ 0.600706\\ <2.00E-16\\ 0.535744\\ <2.00E-16\\ 0.378488\\ 0.07134\\ 0.626043\\ 0.00461\\ 0.440956\\ 0.000572\\ 0.010005\\ 0.001263\\ 0.717667\\ \end{array}$	***  ***  ***  ***  ***  ***	CJxslq.L1 TWBBB.L2 CJxslq.L2 TWBBB.L3 CJxslq.L3 TWBBB.L4 CJxslq.L4 TWBBB.L5 CJxslq.L5 TWBBB.L6 CJxslq.L6 TWBBB.L7 CJxslq.L7 TWBBB.L8 CJxslq.L8 TWBBB.L9 CJxslq.L9 TWBBB.L10 CJxslq.L10	1.07463 -18.46408 -0.15629 13.63989 -0.12526 -13.66792 0.17938 -25.79096 -0.32091 -11.01383 0.23369 14.18664 0.04891 -7.14949 -0.08079 9.99069 0.09769 -30.32073 -0.07402 -13.48859	0.01886 14.48756 0.02776 15.77238 0.02776 15.82018 0.0277 15.77581 0.0277 15.77523 0.02784 15.74004 0.02775 15.75457 0.02763 15.7029 0.01883 14.43483	<2.00E-16 0.2026 1.75E-08 0.387225 6.70E-06 0.387687 1.40E-10 0.101783 <2.00E-16 0.368571 0.079033 0.549704 0.003633 0.526037 0.000413 0.053596 8.69E-05 0.350154	***  ***  ***  ***  ***  ***  ***  ***

This table shows the results for the VAR with the daily BBB CMBX bid-ask estimates as the endogenous variables and liquidity (CJ Liquidity) and excess liquidity (CJ xslq) as the exogenous variables. The lags, L#, are determined by the Akaike Information Criteria (AIC) to a maximum of 10 lags. Estimates are provided with standard errors, probabilities and statistical significance. All panels capture the lagged effective bid-ask spread for the labeled model. Panels A and B report the estimates using the Absolute Roll measure of Christopoulos (2020) for BBB effective bid-ask spreads with the lagged liquidity (CJIq, Panel A) and excess liquidity (CJxslq, Panel B). Panels C and D report the estimates using the effective bid-ask measure of Thompson and Waller (1987) for BBB effective bid-ask spreads with the lagged liquidity (CJIq, Panel C) and excess liquidity (CJxslq, Panel D). The F-test p-value and the value of the VAR's Adjusted R-squared and degrees of freedom are reported at the bottom of each panel. \*\*\*/\*\*/\*/ correspond to 0.1%, 1%, 5% and 10% levels of significance.

# A.3 Proper specification of the Daily Model

One might consider whether the Daily Model has some collinearity in its terms. To address this, consider the first three terms of the model from Section 3:

$$v_t \equiv [f_t - f_{t-1}]^2 = f_t^2 - 2f_t f_{t-1} + f_{t-1}^2 \tag{36}$$

$$v_{t-1} \equiv [f_{t-1} - f_{t-2}]^2 = f_{t-1}^2 - 2f_{t-1}f_{t-2} + f_{t-2}^2$$
(37)

$$[v_t - v_{t-1}]^2 = v_t^2 - 2v_t v_{t-1} + v_{t-1}^2$$
(38)

We know that for two linearly independent terms, their squared difference is also linearly independent of the former two. Substituting the right-hand terms of the equation for  $v_t$ , Eq. (36), and for  $v_{t-1}$ , Eq. (37), into the right-hand side terms for Eq. (38), we get the following expansion for the PCA factors.

$$= (f_t^2 - 2f_t f_{t-1} + f_{t-1}^2)^2 - 2(f_t^2 - 2f_t f_{t-1} + f_{t-1}^2)(f_{t-1}^2 - 2f_{t-1} f_{t-2} + f_{t-2}^2) + (f_{t-1}^2 - 2f_{t-1} f_{t-2} + f_{t-2}^2)^2$$

$$= (f_t^4 - 4f_t^3 f_{t-1} + 6f_t^2 f_{t-1}^2 - 4f_t f_{t-1}^3 + f_{t-1}^4) - (2f_t^2 f_{t-1}^2 - 4f_t^2 f_{t-1} f_{t-2} + 2f_t^2 f_{t-2}^2 - 4f_t f_{t-1}^3 + 8f_t f_{t-1}^2 f_{t-2} - 4f_t f_{t-1} f_{t-2}^2 + 2f_{t-1}^4 - 4f_{t-1}^3 f_{t-2} + 2f_{t-1}^2 f_{t-2}^2) + (f_{t-1}^4 - 4f_t^3 f_{t-1} + 6f_t^2 f_{t-2}^2 - 4f_{t-1} f_{t-2}^3 + f_{t-2}^4)$$

$$= (f_t^4 - 4f_t^3 f_{t-1} + 6f_t^2 f_{t-1}^2 - 4f_t f_{t-1}^3 + f_{t-1}^4) - (2f_t^2 f_{t-1}^2 - 4f_t^2 f_{t-1} f_{t-2} + 2f_t^2 f_{t-2}^2 - 4f_t f_{t-1}^3 f_{t-2} + 2f_t^2 f_{t-1}^2 - 4f_t f_{t-1}^3 + f_{t-1}^4) - (2f_t^2 f_{t-1}^2 - 4f_t^2 f_{t-1} f_{t-2} + 2f_t^2 f_{t-1}^2 - 4f_t f_{t-1}^3 f_{t-2} + 2f_t^2 f_{t-2}^2 - 4f_t f_{t-1}^3 f_{t-2}^2 + 2f_t^2 f_{t-2}^2 - 4f_t f_{t-1}^3 f_{t-2}^2 + 2f_t^2 f_{t-2}^2 - 4f_t f_t^3 f_{t-2} + 2f_t^2 f_t^2 f_{t-2}^2 - 4f_t f_t^3 f_{t-2} + 2f_t^2 f_t^2 f_{t-2}^2 - 4f_t f_t^3 f_{t-2} + 2f_t^2 f_t^2 f_{t-2}^2 - 4f_t f_t^3 f_{t-2}^2 + 2f_t^2 f_t^2 f_$$

The model is well specified if all the terms of the model are non-collinear. All the terms in Eqs. (36, 37, 38 and 39) are linearly independent, and therefore these first three terms of the Daily Model are non-collinear. Additionally, the fourth term of the Daily Model (the market spread) is a direct empirical observation and therefore independent of the first three. Since all four terms of the Daily Model are non-collinear, the Daily Model is well specified.■